

# INSTRUCTOR'S SOLUTIONS MANUAL SINGLE VARIABLE

ELKA BLOCK

FRANK PURCELL

## THOMAS' CALCULUS EARLY TRANSCENDENTALS THIRTEENTH EDITION

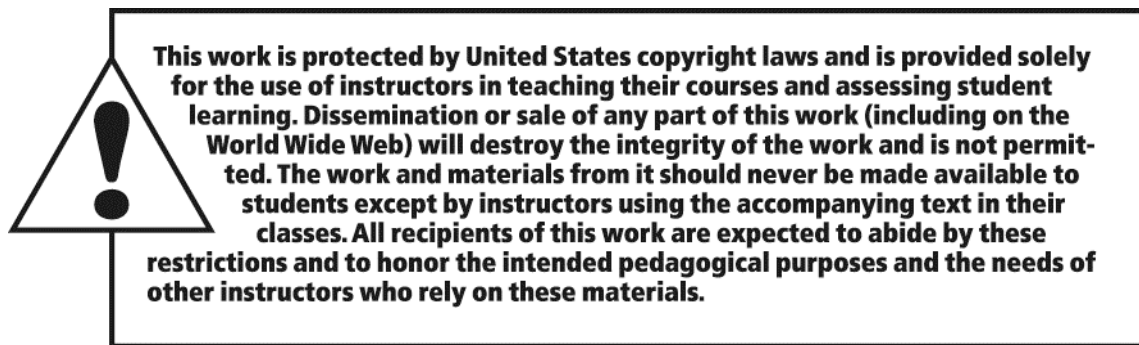
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