

## PARTICLE PHYSICS AND COSMOLOGY

- 44.1. IDENTIFY and SET UP:** By momentum conservation the two photons must have equal and opposite momenta. Then  $E = pc$  says the photons must have equal energies. Their total energy must equal the rest mass energy  $E = mc^2$  of the pion. Once we have found the photon energy we can use  $E = hf$  to calculate the photon frequency and use  $\lambda = c/f$  to calculate the wavelength.

**EXECUTE:** The mass of the pion is  $270m_e$ , so the rest energy of the pion is  $270(0.511 \text{ MeV}) = 138 \text{ MeV}$ . Each photon has half this energy, or  $69 \text{ MeV}$ .

$$E = hf \text{ so } f = \frac{E}{h} = \frac{(69 \times 10^6 \text{ eV})(1.602 \times 10^{-19} \text{ J/eV})}{6.626 \times 10^{-34} \text{ J}\cdot\text{s}} = 1.7 \times 10^{22} \text{ Hz.}$$

$$\lambda = \frac{c}{f} = \frac{2.998 \times 10^8 \text{ m/s}}{1.7 \times 10^{22} \text{ Hz}} = 1.8 \times 10^{-14} \text{ m} = 18 \text{ fm.}$$

**EVALUATE:** These photons are in the gamma ray part of the electromagnetic spectrum.

- 44.2. IDENTIFY:** The energy (rest mass plus kinetic) of the muons is equal to the energy of the photons.

**SET UP:**  $\gamma + \gamma \rightarrow \mu^+ + \mu^-$ ,  $E = hc/\lambda$ .  $K = (\gamma - 1)mc^2$ .

**EXECUTE: (a)**  $\gamma + \gamma \rightarrow \mu^+ + \mu^-$ . Each photon must have energy equal to the rest mass energy of a  $\mu^+$  or

$$\text{a } \mu^-: \frac{hc}{\lambda} = 105.7 \times 10^6 \text{ eV. } \lambda = \frac{(4.136 \times 10^{-15} \text{ eV}\cdot\text{s})(2.998 \times 10^8 \text{ m/s})}{105.7 \times 10^6 \text{ eV}} = 1.17 \times 10^{-14} \text{ m} = 0.0117 \text{ pm.}$$

Conservation of linear momentum requires that the  $\mu^+$  and  $\mu^-$  move in opposite directions with equal speeds.

**(b)**  $\lambda = \frac{0.0117 \text{ pm}}{2}$  so each photon has energy  $2(105.7 \text{ MeV}) = 211.4 \text{ MeV}$ . The energy released in the reaction is  $2(211.4 \text{ MeV}) - 2(105.7 \text{ MeV}) = 211.4 \text{ MeV}$ . The kinetic energy of each muon is half this,

$$105.7 \text{ MeV. Using } K = (\gamma - 1)mc^2 \text{ gives } \gamma - 1 = \frac{K}{mc^2} = \frac{105.7 \text{ MeV}}{105.7 \text{ MeV}} = 1. \quad \gamma = 2. \quad \gamma = \frac{1}{\sqrt{1 - v^2/c^2}}.$$

$$\frac{v^2}{c^2} = 1 - \frac{1}{\gamma^2}. \quad v = \sqrt{\frac{3}{4}}c = 0.866c = 2.60 \times 10^8 \text{ m/s.}$$

**EVALUATE:** The muon speeds are a substantial fraction of the speed of light, so special relativity must be used.

- 44.3. IDENTIFY:** The energy released is the energy equivalent of the mass decrease that occurs in the decay.

**SET UP:** The mass of the pion is  $m_{\pi^+} = 270m_e$  and the mass of the muon is  $m_{\mu^+} = 207m_e$ . The rest energy of an electron is  $0.511 \text{ MeV}$ .

**EXECUTE: (a)**  $\Delta m = m_{\pi^+} - m_{\mu^+} = 270m_e - 207m_e = 63m_e \Rightarrow E = 63(0.511 \text{ MeV}) = 32 \text{ MeV}$ .

**EVALUATE: (b)** A positive muon has less mass than a positive pion, so if the decay from muon to pion was to happen, you could always find a frame where energy was not conserved. This cannot occur.

- 44.4. IDENTIFY:** In the annihilation the total energy of the proton and antiproton is converted to the energy of the two photons.

**SET UP:** The rest energy of a proton or antiproton is 938.3 MeV. Conservation of linear momentum requires that the two photons have equal energies. The energy of a photon is  $E = hf$ , and  $f\lambda = c$ .

**EXECUTE:** (a) The energy will be the proton rest energy, 938.3 MeV, so  $hf = 938.3$  MeV. Solving for  $f$  gives  $f = (938.3 \times 10^6 \text{ eV}) / (4.136 \times 10^{-15} \text{ eV} \cdot \text{s}) = 2.27 \times 10^{23}$  Hz. The wavelength is

$$\lambda = c/f = 1.32 \times 10^{-15} \text{ m} = 1.32 \text{ fm.}$$

(b) The energy of each photon will be  $938.3 \text{ MeV} + 620 \text{ MeV} = 1558 \text{ MeV}$ , so  $f = (1558 \text{ MeV})/h = 3.77 \times 10^{23}$  Hz.  $\lambda = c/f = 7.96 \times 10^{-16} \text{ m} = 0.796 \text{ fm}$ .

**EVALUATE:** When the initial kinetic energy of the proton and antiproton increases, the wavelength of the photons decreases.

- 44.5. IDENTIFY:** The kinetic energy of the alpha particle is due to the mass decrease.

**SET UP and EXECUTE:**  ${}^1_0\text{n} + {}^{10}_5\text{B} \rightarrow {}^7_3\text{Li} + {}^4_2\text{He}$ . The mass decrease in the reaction is

$m({}^1_0\text{n}) + m({}^{10}_5\text{B}) - m({}^7_3\text{Li}) - m({}^4_2\text{He}) = 1.008665 \text{ u} + 10.012937 \text{ u} - 7.016005 \text{ u} - 4.002603 \text{ u} = 0.002994 \text{ u}$  and the energy released is  $E = (0.002994 \text{ u})(931.5 \text{ MeV/u}) = 2.79 \text{ MeV}$ . Assuming the initial momentum

is zero,  $m_{\text{Li}}v_{\text{Li}} = m_{\text{He}}v_{\text{He}}$  and  $v_{\text{Li}} = \frac{m_{\text{He}}}{m_{\text{Li}}}v_{\text{He}}$ .  $\frac{1}{2}m_{\text{Li}}v_{\text{Li}}^2 + \frac{1}{2}m_{\text{He}}v_{\text{He}}^2 = E$  becomes

$$\frac{1}{2}m_{\text{Li}}\left(\frac{m_{\text{He}}}{m_{\text{Li}}}\right)^2v_{\text{He}}^2 + \frac{1}{2}m_{\text{He}}v_{\text{He}}^2 = E \quad \text{and} \quad v_{\text{He}} = \sqrt{\frac{2E}{m_{\text{He}}}\left(\frac{m_{\text{Li}}}{m_{\text{Li}} + m_{\text{He}}}\right)}. \quad E = 4.470 \times 10^{-13} \text{ J.}$$

$$m_{\text{He}} = 4.002603 \text{ u} - 2(0.0005486 \text{ u}) = 4.0015 \text{ u} = 6.645 \times 10^{-27} \text{ kg.}$$

$$m_{\text{Li}} = 7.016005 \text{ u} - 3(0.0005486 \text{ u}) = 7.0144 \text{ u.} \quad \text{This gives } v_{\text{He}} = 9.26 \times 10^6 \text{ m/s.}$$

**EVALUATE:** The speed of the alpha particle is considerably less than the speed of light, so it is not necessary to use the more complicated relativistic formulas.

- 44.6. IDENTIFY:** The range is limited by the lifetime of the particle, which itself is limited by the uncertainty principle.

**SET UP:**  $\Delta E \Delta t = \hbar/2$ .

**EXECUTE:**  $\Delta t = \frac{\hbar}{2\Delta E} = \frac{(4.136 \times 10^{-15} \text{ eV} \cdot \text{s}/2\pi)}{2(783 \times 10^6 \text{ eV})} = 4.20 \times 10^{-25} \text{ s}$ . The range of the force is

$$c\Delta t = (2.998 \times 10^8 \text{ m/s})(4.20 \times 10^{-25} \text{ s}) = 1.26 \times 10^{-16} \text{ m} = 0.126 \text{ fm.}$$

**EVALUATE:** This range is less than the diameter of an atomic nucleus.

- 44.7. IDENTIFY:** The antimatter annihilates with an equal amount of matter.

**SET UP:** The energy of the matter is  $E = (\Delta m)c^2$ .

**EXECUTE:** Putting in the numbers gives

$$E = (\Delta m)c^2 = (400 \text{ kg} + 400 \text{ kg})(3.00 \times 10^8 \text{ m/s})^2 = 7.2 \times 10^{19} \text{ J.}$$

This is about 70% of the annual energy use in the U.S.

**EVALUATE:** If this huge amount of energy were released suddenly, it would blow up the *Enterprise*!

Getting useable energy from matter-antimatter annihilation is not so easy to do!

- 44.8. IDENTIFY:** With a stationary target, only part of the initial kinetic energy of the moving electron is available. Momentum conservation tells us that there must be nonzero momentum after the collision, which means that there must also be leftover kinetic energy. Therefore not all of the initial energy is available.

**SET UP:** The available energy is given by  $E_a^2 = 2mc^2(E_m + mc^2)$  for two particles of equal mass when one is initially stationary. In this case, the initial kinetic energy ( $30.0 \text{ GeV} = 30,000 \text{ MeV}$ ) is much more than the rest energy of the electron ( $0.511 \text{ MeV}$ ), so the formula for available energy reduces to  $E_a = \sqrt{2mc^2E_m}$ .

**EXECUTE:** (a) Using the formula for available energy gives

$$E_a = \sqrt{2mc^2E_m} = \sqrt{2(0.511 \text{ MeV})(30.0 \text{ GeV})} = 175 \text{ MeV.}$$

(b) For colliding beams of equal mass, each particle has half the available energy, so each has 87.5 MeV. The *total* energy is twice this, or 175 MeV.

**EVALUATE:** Colliding beams provide considerably more available energy to do experiments than do beams hitting a stationary target. With a stationary electron target in part (a), we had to give the moving electron 30,000 MeV of energy to get the same available energy that we got with only 175 MeV of energy with the colliding beams.

**44.9. IDENTIFY and SET UP:** The angular frequency is  $\omega = |q|B/m$  so  $B = m\omega/|q|$ . And since  $\omega = 2\pi f$ , this becomes  $B = 2\pi mf/|q|$ .

**EXECUTE: (a)** A deuteron is a deuterium nucleus ( ${}^2_1\text{H}$ ). Its charge is  $q = +e$ . Its mass is the mass of the neutral  ${}^2_1\text{H}$  atom (Table 43.2) minus the mass of the one atomic electron:

$$m = 2.014102 \text{ u} - 0.0005486 \text{ u} = 2.013553 \text{ u} (1.66054 \times 10^{-27} \text{ kg/1 u}) = 3.344 \times 10^{-27} \text{ kg}.$$

$$B = \frac{2\pi mf}{|q|} = \frac{2\pi(3.344 \times 10^{-27} \text{ kg})(9.00 \times 10^6 \text{ Hz})}{1.602 \times 10^{-19} \text{ C}} = 1.18 \text{ T}.$$

(b) Eq. (44.8):  $K = \frac{q^2 B^2 R^2}{2m} = \frac{[(1.602 \times 10^{-19} \text{ C})(1.18 \text{ T})(0.320 \text{ m})]^2}{2(3.344 \times 10^{-27} \text{ kg})}$ .

$$K = 5.471 \times 10^{-13} \text{ J} = (5.471 \times 10^{-13} \text{ J})(1 \text{ eV}/1.602 \times 10^{-19} \text{ J}) = 3.42 \text{ MeV}.$$

$$K = \frac{1}{2}mv^2 \text{ so } v = \sqrt{\frac{2K}{m}} = \sqrt{\frac{2(5.471 \times 10^{-13} \text{ J})}{3.344 \times 10^{-27} \text{ kg}}} = 1.81 \times 10^7 \text{ m/s}.$$

**EVALUATE:**  $v/c = 0.06$ , so it is ok to use the nonrelativistic expression for kinetic energy.

**44.10. IDENTIFY:** The radius is  $r = mv/|q|B$ , and angular frequency is  $\omega = |q|B/m$ .  $f = \frac{\omega}{2\pi}$ . In part (c) apply conservation of energy.

**SET UP:** The relativistic form for the kinetic energy is  $K = (\gamma - 1)mc^2$ . A proton has mass  $1.67 \times 10^{-27} \text{ kg}$ .

**EXECUTE: (a)**  $2f = \frac{\omega}{\pi} = \frac{eB}{m\pi} = 5.19 \times 10^7 \text{ /s}$ .

(b)  $v = \omega r = \frac{eBr}{m} = 4.08 \times 10^7 \text{ m/s}$ .

(c) For three-figure precision, the relativistic form of the kinetic energy must be used,  $eV = (\gamma - 1)mc^2$ , so  $eV = (\gamma - 1)mc^2$ , so  $V = \frac{(\gamma - 1)mc^2}{e} = 8.80 \times 10^6 \text{ V}$ .

**EVALUATE:** The kinetic energy of the protons in part (c) is 8.80 MeV. This is 0.94% of their rest energy. If the nonrelativistic expression for the kinetic energy is used, we obtain  $V = 8.7 \times 10^6 \text{ V}$ .

**44.11. IDENTIFY and SET UP:** The masses of the target and projectile particles are equal, so we can use the equation  $E_a^2 = 2mc^2(E_m + mc^2)$ .  $E_a$  is specified; solve for the energy  $E_m$  of the beam particles.

**EXECUTE: (a)** Solve for  $E_m$ :  $E_m = \frac{E_a^2}{2mc^2} - mc^2$ .

The mass for the alpha particle can be calculated by subtracting two electron masses from the  ${}^4_2\text{He}$  atomic mass:

$$m = m_{\alpha} = 4.002603 \text{ u} - 2(0.0005486 \text{ u}) = 4.001506 \text{ u}.$$

$$\text{Then } mc^2 = (4.001506 \text{ u})(931.5 \text{ MeV/u}) = 3.727 \text{ GeV}.$$

$$E_m = \frac{E_a^2}{2mc^2} - mc^2 = \frac{(16.0 \text{ GeV})^2}{2(3.727 \text{ GeV})} - 3.727 \text{ GeV} = 30.6 \text{ GeV}.$$

(b) Each beam must have  $\frac{1}{2}E_a = 8.0$  GeV.

**EVALUATE:** For a stationary target the beam energy is nearly twice the available energy. In a colliding beam experiment all the energy is available and each beam needs to have just half the required available energy.

**44.12. IDENTIFY and SET UP:** The nonrelativistic cyclotron angular frequency is  $\omega_{\text{nr}} = \frac{|q|B}{m}$  and the relativistic version is  $\omega_r = \frac{|q|B}{m} \sqrt{1 - v^2/c^2}$ . In this case,  $\omega_r = 0.90\omega_{\text{nr}}$ .

**EXECUTE: (a)** Using  $\omega_r = 0.90\omega_{\text{nr}}$ , we have  $\frac{|q|B}{m} \sqrt{1 - v^2/c^2} = 0.90 \frac{|q|B}{m}$ . Solving for  $v$  gives  $v = 0.4359c = 1.307 \times 10^8$  m/s, which rounds to  $1.31 \times 10^8$  m/s.

(b)  $K = \frac{1}{2}mv^2 = \frac{1}{2}(1.673 \times 10^{-27} \text{ kg})(1.307 \times 10^8 \text{ m/s})^2 = 1.43 \times 10^{-11} \text{ J} = 89.2 \text{ MeV}$ .

**EVALUATE:** The answer for part (b) is somewhat approximate, since we should use the relativistic kinetic energy formula because  $v$  is over 40% the speed of light.

**44.13. IDENTIFY:**  $E = \gamma mc^2$ , where  $\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$ . The relativistic formula for the angular frequency is

$$\omega = \frac{|q|B}{m\gamma}.$$

**SET UP:** A proton has rest energy  $mc^2 = 938.3$  MeV.

**EXECUTE: (a)**  $\gamma = \frac{E}{mc^2} = \frac{1000 \times 10^3 \text{ MeV}}{938.3 \text{ MeV}} = 1065.8$ , so  $v = 0.999999559c$ .

(b) **Nonrelativistic:**  $\omega = \frac{eB}{m} = 3.83 \times 10^8$  rad/s.

**Relativistic:**  $\omega = \frac{eB}{m} \frac{1}{\gamma} = 3.59 \times 10^5$  rad/s.

**EVALUATE:** The relativistic expression gives a smaller value for  $\omega$ .

**44.14. IDENTIFY and SET UP:** To create the  $\eta^0$ , the minimum available energy must be equal to the rest mass energy of the products, which in this case is the  $\eta^0$  plus two protons. In a collider, all of the initial energy is available, so the beam energy is the available energy.

**EXECUTE:** The minimum amount of available energy must be rest mass energy

$$E_a = 2m_p + m_\eta = 2(938.3 \text{ MeV}) + 547.3 \text{ MeV} = 2420 \text{ MeV}.$$

Each incident proton has half of the rest mass energy, or  $1210 \text{ MeV} = 1.21 \text{ GeV}$ .

**EVALUATE:** As Problem 44.15 shows, we would need much more initial energy if one of the initial protons were stationary. The result here (1.21 GeV) is the *minimum* amount of energy needed; the original protons could have more energy and still trigger this reaction.

**44.15. (a) IDENTIFY and SET UP:** For a proton beam on a stationary proton target, and since  $E_a$  is much larger than the proton rest energy, we can use the equation  $E_a^2 = 2mc^2E_m$ .

**EXECUTE:**  $E_m = \frac{E_a^2}{2mc^2} = \frac{(77.4 \text{ GeV})^2}{2(0.938 \text{ GeV})} = 3200 \text{ GeV}$ .

(b) **IDENTIFY and SET UP:** For colliding beams the total momentum is zero and the available energy  $E_a$  is the total energy for the two colliding particles.

**EXECUTE:** For proton-proton collisions the colliding beams each have the same energy, so the total energy of each beam is  $\frac{1}{2}E_a = 38.7 \text{ GeV}$ .

**EVALUATE:** For a stationary target less than 3% of the beam energy is available for conversion into mass. The beam energy for a colliding beam experiment is a factor of (1/83) times smaller than the required energy for a stationary target experiment.

- 44.16. IDENTIFY and SET UP:** For the reaction  $p + p \rightarrow p + p + p + \bar{p}$ , the two incident protons must have enough kinetic energy to produce a  $p$  and a  $\bar{p}$ , plus any kinetic energy of the products. If they have the minimum kinetic energy, the products are at rest. The proton and antiproton have equal masses. The available energy for two equal-mass particles is  $E_a^2 = 2mc^2(E_m + mc^2)$ , where  $E_m = K + mc^2$ .

**EXECUTE: (a)** In a head-on collision with equal speeds, the laboratory frame is the center-of-momentum frame. For the minimum kinetic energy of the incident protons, the products are all at rest. In that case, the incident protons need only enough kinetic energy to produce a proton and an antiproton. Since the incident protons have equal energy, each one must have kinetic energy equal to the rest energy of a proton, which is 938 MeV.

**(b)** In this case, the target proton is at rest. Since 4 particles are produced, each of mass  $m$ , the available energy  $E_a$  must be at least equal to  $4mc^2$ . Therefore  $E_a^2 = 2mc^2(E_m + mc^2) = (4mc^2)^2 = 16m^2c^4$ , which gives  $E_m = 7mc^2$ . Using  $E_m = K + mc^2$ , we get  $K = 6mc^2 = 6(938 \text{ MeV}) = 5630 \text{ MeV}$ .

**EVALUATE:** When the two protons collide head-on with equal speeds, they need only 938 MeV of kinetic energy each, for a total of 1879 MeV. But when the target is stationary, the kinetic energy needed is 5630 MeV, which is 3 times as much as for a head-on collision.

- 44.17. IDENTIFY:** The kinetic energy comes from the mass decrease.

**SET UP:** Table 44.3 gives  $m(K^+) = 493.7 \text{ MeV}/c^2$ ,  $m(\pi^0) = 135.0 \text{ MeV}/c^2$ , and  $m(\pi^\pm) = 139.6 \text{ MeV}/c^2$ .

**EXECUTE: (a)** Charge must be conserved, so  $K^+ \rightarrow \pi^0 + \pi^+$  is the only possible decay.

**(b)** The mass decrease is

$m(K^+) - m(\pi^0) - m(\pi^+) = 493.7 \text{ MeV}/c^2 - 135.0 \text{ MeV}/c^2 - 139.6 \text{ MeV}/c^2 = 219.1 \text{ MeV}/c^2$ . The energy released is 219.1 MeV.

**EVALUATE:** The  $\pi$  mesons do not share this energy equally since they do not have equal masses.

- 44.18. IDENTIFY:** The energy is due to the mass difference.

**SET UP:** The energy released is the energy equivalent of the mass decrease. From Table 44.3, the  $\mu^-$  has mass  $105.7 \text{ MeV}/c^2$  and the  $e^-$  has mass  $0.511 \text{ MeV}/c^2$ .

**EXECUTE:** The mass decrease is  $105.7 \text{ MeV}/c^2 - 0.511 \text{ MeV}/c^2 = 105.2 \text{ MeV}/c^2$  and the energy equivalent is 105.2 MeV.

**EVALUATE:** The electron does not get all of this energy; the neutrinos also get some of it.

- 44.19. IDENTIFY:** Table 44.1 gives the mass in units of  $\text{GeV}/c^2$ . This is the value of  $mc^2$  for the particle.

**SET UP:**  $m(Z^0) = 91.2 \text{ GeV}/c^2$ .

**EXECUTE:**  $E = 91.2 \times 10^9 \text{ eV} = 1.461 \times 10^{-8} \text{ J}$ ;  $m = E/c^2 = 1.63 \times 10^{-25} \text{ kg}$ ;  $m(Z^0)/m(p) = 97.2$

**EVALUATE:** The rest energy of a proton is 938 MeV; the rest energy of the  $Z^0$  is 97.2 times as great.

- 44.20. IDENTIFY:** The energy of the photon equals the difference in the rest energies of the  $\Sigma^0$  and  $\Lambda^0$ . For a photon,  $p = E/c$ .

**SET UP:** Table 44.3 gives the rest energies to be 1193 MeV for the  $\Sigma^0$  and 1116 MeV for the  $\Lambda^0$ .

**EXECUTE: (a)** We shall assume that the kinetic energy of the  $\Lambda^0$  is negligible. In that case we can set the value of the photon's energy equal to  $Q$ :

$$Q = (1193 - 1116) \text{ MeV} = 77 \text{ MeV} = E_{\text{photon}}$$

**(b)** The momentum of this photon is

$$p = \frac{E_{\text{photon}}}{c} = \frac{(77 \times 10^6 \text{ eV})(1.60 \times 10^{-18} \text{ J/eV})}{(3.00 \times 10^8 \text{ m/s})} = 4.1 \times 10^{-20} \text{ kg} \cdot \text{m/s}.$$

**EVALUATE:** To justify our original assumption, we can calculate the kinetic energy of a  $\Lambda^0$  that has this value of momentum

$$K_{\Lambda^0} = \frac{p^2}{2m} = \frac{E^2}{2mc^2} = \frac{(77 \text{ MeV})^2}{2(1116 \text{ MeV})} = 2.7 \text{ MeV} \ll Q = 77 \text{ MeV}.$$

Thus, we can ignore the momentum of the  $\Lambda^0$  without introducing a large error.

**44.21. IDENTIFY and SET UP:** Find the energy equivalent of the mass decrease.

**EXECUTE:** The mass decrease is  $m(\Sigma^+) - m(p) - m(\pi^0)$  and the energy released is

$mc^2(\Sigma^+) - mc^2(p) - mc^2(\pi^0) = 1189 \text{ MeV} - 938.3 \text{ MeV} - 135.0 \text{ MeV} = 116 \text{ MeV}$ . (The  $mc^2$  values for each particle were taken from Table 44.3.)

**EVALUATE:** The mass of the decay products is less than the mass of the original particle, so the decay is energetically allowed and energy is released.

**44.22. IDENTIFY:** If the initial and final rest mass energies were equal, there would be no leftover energy for kinetic energy. Therefore the kinetic energy of the products is the difference between the mass energy of the initial particles and the final particles.

**SET UP:** The difference in mass is  $\Delta m = M_{\Omega^-} - m_{\Lambda^0} - m_{K^-}$ .

**EXECUTE:** Using Table 44.3, the energy difference is

$$E = (\Delta m)c^2 = 1672 \text{ MeV} - 1116 \text{ MeV} - 494 \text{ MeV} = 62 \text{ MeV}.$$

**EVALUATE:** There is less rest mass energy after the reaction than before because 62 MeV of the initial energy was converted to kinetic energy of the products.

**44.23. IDENTIFY and SET UP:** The lepton numbers for the particles are given in Table 44.2.

**EXECUTE:** (a)  $\mu^- \rightarrow e^- + \nu_e + \bar{\nu}_\mu \Rightarrow L_\mu: +1 \neq -1, L_e: 0 \neq +1 + 1$ , so lepton numbers are not conserved.

(b)  $\tau^- \rightarrow e^- + \bar{\nu}_e + \nu_\tau \Rightarrow L_e: 0 = +1 - 1, L_\tau: +1 = +1$ , so lepton numbers are conserved.

(c)  $\pi^+ \rightarrow e^+ + \gamma$ . Lepton numbers are not conserved since just one lepton is produced from zero original leptons.

(d)  $n \rightarrow p + e^- + \bar{\nu}_e \Rightarrow L_e: 0 = +1 - 1$ , so the lepton numbers are conserved.

**EVALUATE:** The decays where lepton numbers are conserved are among those listed in Tables 44.2 and 44.3.

**44.24. IDENTIFY and SET UP:** The p and n have baryon number +1 and the antiproton  $\bar{p}$  has baryon number

-1.  $e^+, e^-, \bar{\nu}_e$ , and  $\gamma$  all have baryon number zero. Baryon number is conserved if the total baryon number of the products equals the total baryon number of the reactants.

**EXECUTE:** (a) reactants:  $B = 1 + 1 = 2$ . Products:  $B = 1 + 0 = 1$ . Not conserved.

(b) reactants:  $B = 1 + 1 = 2$ . Products:  $B = 0 + 0 = 0$ . Not conserved.

(c) reactants:  $B = +1$ . Products:  $B = 1 + 0 + 0 = +1$ . Conserved.

(d) reactants:  $B = 1 - 1 = 0$ . Products:  $B = 0$ . Conserved.

**EVALUATE:** Even though a reaction obeys conservation of baryon number it may still not occur spontaneously, if it is not energetically allowed or if other conservation laws are violated.

**44.25. IDENTIFY and SET UP:** Compare the sum of the strangeness quantum numbers for the particles on each side of the decay equation. The strangeness quantum numbers for each particle are given in Table 44.3.

**EXECUTE:** (a)  $K^+ \rightarrow \mu^+ + \nu_\mu; S_{K^+} = +1, S_{\mu^+} = 0, S_{\nu_\mu} = 0$ .

$S = 1$  initially;  $S = 0$  for the products;  $S$  is not conserved.

(b)  $n + K^+ \rightarrow p + \pi^0; S_n = 0, S_{K^+} = +1, S_p = 0, S_{\pi^0} = 0$ .

$S = 1$  initially;  $S = 0$  for the products;  $S$  is not conserved.

(c)  $K^+ + K^- \rightarrow \pi^0 + \pi^0; S_{K^+} = +1, S_{K^-} = -1, S_{\pi^0} = 0$ .

$S = +1 - 1 = 0$  initially;  $S = 0$  for the products;  $S$  is conserved.

(d)  $p + K^- \rightarrow \Lambda^0 + \pi^0; S_p = 0, S_{K^-} = -1, S_{\Lambda^0} = -1, S_{\pi^0} = 0$ .

$S = -1$  initially;  $S = -1$  for the products;  $S$  is conserved.

**EVALUATE:** Strangeness is not a conserved quantity in weak interactions, and strangeness nonconserving reactions or decays can occur.

**44.26. IDENTIFY:** Quark combination produce various particles.

**SET UP:** The properties of the quarks are given in Table 44.5. An antiquark has charge and quantum numbers of opposite sign from the corresponding quark.

**EXECUTE:** (a)  $Q/e = \frac{2}{3} + \frac{2}{3} + (-\frac{1}{3}) = +1$ .  $B = \frac{1}{3} + \frac{1}{3} + \frac{1}{3} = 1$ .  $S = 0 + 0 + (-1) = -1$ .  $C = 0 + 0 + 0 = 0$ .

(b)  $Q/e = \frac{2}{3} + \frac{1}{3} = +1$ .  $B = \frac{1}{3} + (-\frac{1}{3}) = 0$ .  $S = 0 + 1 = 1$ .  $C = 1 + 0 = 1$ .

(c)  $Q/e = \frac{1}{3} + \frac{1}{3} + (-\frac{2}{3}) = 0$ .  $B = -\frac{1}{3} + (-\frac{1}{3}) + (-\frac{1}{3}) = -1$ .  $S = 0 + 0 + 0 = 0$ .  $C = 0 + 0 + 0 = 0$ .

(d)  $Q/e = -\frac{2}{3} + (-\frac{1}{3}) = -1$ .  $B = -\frac{1}{3} + \frac{1}{3} = 0$ .  $S = 0 + 0 = 0$ .  $C = -1 + 0 = -1$ .

**EVALUATE:** The charge must always come out to be a whole number.

**44.27. IDENTIFY and SET UP:** Each value for the combination is the sum of the values for each quark. Use Table 44.4.

**EXECUTE:** (a) uds:

$$Q = \frac{2}{3}e - \frac{1}{3}e - \frac{1}{3}e = 0$$

$$B = \frac{1}{3} + \frac{1}{3} + \frac{1}{3} = 1$$

$$S = 0 + 0 - 1 = -1$$

$$C = 0 + 0 + 0 = 0$$

(b) cū:

The values for  $\bar{u}$  are the negative for those for  $u$ .

$$Q = \frac{2}{3}e - \frac{2}{3}e = 0$$

$$B = \frac{1}{3} - \frac{1}{3} = 0$$

$$S = 0 + 0 = 0$$

$$C = +1 + 0 = +1$$

(c) ddd:

$$Q = -\frac{1}{3}e - \frac{1}{3}e - \frac{1}{3}e = -e$$

$$B = \frac{1}{3} + \frac{1}{3} + \frac{1}{3} = +1$$

$$S = 0 + 0 + 0 = 0$$

$$C = 0 + 0 + 0 = 0$$

(d) d $\bar{c}$ :

$$Q = -\frac{1}{3}e - \frac{2}{3}e = -e$$

$$B = \frac{1}{3} - \frac{1}{3} = 0$$

$$S = 0 + 0 = 0$$

$$C = 0 - 1 = -1$$

**EVALUATE:** The charge, baryon number, strangeness, and charm quantum numbers of a particle are determined by the particle's quark composition.

**44.28. IDENTIFY:** The decrease in the rest energy of the particles that exist before and after the decay equals the energy that is released.

**SET UP:** The upsilon has rest energy 9460 MeV and each tau has rest energy 1777 MeV.

**EXECUTE:**  $(m_\Upsilon - 2m_\tau)c^2 = (9460 \text{ MeV} - 2(1777 \text{ MeV})) = 5906 \text{ MeV}$ .

**EVALUATE:** Over half of the rest energy of the upsilon is released in the decay.

**44.29. IDENTIFY:** The charge, baryon number, and strangeness of the particles are the sums of these values for their constituent quarks.

**SET UP:** The properties of the six quarks are given in Table 44.5.

**EXECUTE:** (a)  $S = 1$  indicates the presence of one  $\bar{s}$  antiquark and no  $s$  quark. To have baryon number 0 there can be only one other quark, and to have net charge  $+e$  that quark must be a  $u$ , and the quark content is  $u\bar{s}$ .

(b) The particle has an  $\bar{s}$  antiquark, and for a baryon number of  $-1$  the particle must consist of three antiquarks. For a net charge of  $-e$ , the quark content must be  $\bar{d}\bar{d}\bar{s}$ .

(c)  $S = -2$  means that there are two  $s$  quarks, and for baryon number 1 there must be one more quark. For a charge of 0 the third quark must be a  $u$  quark and the quark content is  $uss$ .

**EVALUATE:** The particles with baryon number zero are mesons and consist of a quark-antiquark pair. Particles with baryon number 1 consist of three quarks and are baryons. Particles with baryon number  $-1$  consist of three antiquarks and are antibaryons.

- 44.30. IDENTIFY and SET UP:** The mass of a proton is  $938 \text{ MeV}/c^2$ , and the mass of the Higgs boson is  $125 \text{ GeV}/c^2 = 125 \times 10^3 \text{ MeV}/c^2$ .

**EXECUTE:**  $m_{\text{Higgs}}/m_p = (125 \times 10^3 \text{ MeV}/c^2)/(938 \text{ MeV}/c^2) = 133$ .

**EVALUATE:** Since the Higgs particle is 133 times as massive as the proton, it takes a great deal of energy to create one. This is the reason that high-energy particle accelerators are needed to test for the existence of the Higgs boson.

- 44.31. (a) IDENTIFY and SET UP:** First calculate the speed  $v$ . Then use that in Hubble's law to find  $r$ .

$$\text{EXECUTE: } v = \left[ \frac{(\lambda_0/\lambda_S)^2 - 1}{(\lambda_0/\lambda_S)^2 + 1} \right] c = \left[ \frac{(658.5 \text{ nm}/590 \text{ nm})^2 - 1}{(658.5 \text{ nm}/590 \text{ nm})^2 + 1} \right] c = 0.1094c$$

$$v = (0.1094)(2.998 \times 10^8 \text{ m/s}) = 3.28 \times 10^7 \text{ m/s. } v = rH_0.$$

**(b) IDENTIFY and SET UP:** Use Hubble's law to calculate  $r$ .

$$\text{EXECUTE: } r = \frac{v}{H_0} = \frac{3.28 \times 10^4 \text{ km/s}}{[(67.3 \text{ km/s})/\text{Mpc}](1 \text{ Mpc}/3.26 \text{ Mly})} = 1590 \text{ Mly} = 1.59 \times 10^9 \text{ ly.}$$

**EVALUATE:** The red shift  $\lambda_0/\lambda_S - 1$  for this galaxy is 0.116. It is therefore about twice as far from earth as the galaxy in Examples 44.8 and 44.9, that had a red shift of 0.053.

- 44.32. IDENTIFY:** The observed wavelength is greater than the wavelength emitted. Apply Hubble's law.

**SET UP:** First find the speed of the quasar using  $v = \frac{(\lambda_0/\lambda_S)^2 - 1}{(\lambda_0/\lambda_S)^2 + 1} c$ . Then apply Hubble's law

$$v = H_0 r \text{ to find } r, \text{ using the Hubble constant } H_0 = (67.3 \text{ km/s})/\text{Mpc}.$$

**EXECUTE:** First find  $v$ :

$$v = \frac{(\lambda_0/\lambda_S)^2 - 1}{(\lambda_0/\lambda_S)^2 + 1} c = \frac{(563.9/486.1)^2 - 1}{(563.9/486.1)^2 + 1} c = 0.14738c = 4.4185 \times 10^7 \text{ m/s.}$$

Now use Hubble's law and solve for  $r$ :

$$r = v/H_0 = (4.4185 \times 10^7 \text{ m/s})/[(67,300 \text{ m/s})/\text{Mpc}] = 656.5 \text{ Mpc.}$$

Using  $3.26 \text{ ly} = 1 \text{ pc}$ , this converts to  $2.14 \times 10^9 \text{ ly}$ .

**EVALUATE:** Since  $\lambda_0 > \lambda_S$ , the quasar is moving away from us with a speed of around 15% the speed of light. This result is consistent with the expanding universe.

- 44.33. (a) IDENTIFY and SET UP:** Hubble's law is  $v = H_0 r$ , with  $H_0 = (67.3 \text{ km/s})/(\text{Mpc})$ .  $1 \text{ Mpc} = 3.26 \text{ Mly}$ .

**EXECUTE:**  $r = 5210 \text{ Mly}$ , so

$$v = H_0 r = [(67.3 \text{ km/s})/\text{Mpc}](1 \text{ Mpc}/3.26 \text{ Mly})(5210 \text{ Mly}) = 1.08 \times 10^5 \text{ km/s} = 1.08 \times 10^8 \text{ m/s.}$$

**(b) IDENTIFY and SET UP:** Use  $v$  from part (a) in  $\lambda_0 = \lambda_S \sqrt{\frac{c+v}{c-v}} = \sqrt{\frac{1+v/c}{1-v/c}}$ .

$$\text{EXECUTE: } \frac{\lambda_0}{\lambda_S} = \sqrt{\frac{c+v}{c-v}} = \sqrt{\frac{1+v/c}{1-v/c}}.$$

$$\frac{v}{c} = \frac{1.08 \times 10^8 \text{ m/s}}{2.998 \times 10^8 \text{ m/s}} = 0.3602, \text{ so } \frac{\lambda_0}{\lambda_S} = \sqrt{\frac{1+0.3602}{1-0.3602}} = 1.46.$$

**EVALUATE:** The galaxy in Examples 44.8 and 44.9 is 710 Mly away so has a smaller recession speed and redshift than the galaxy in this problem.

**44.34. IDENTIFY:** In Example 44.8,  $z$  is defined as  $z = \frac{\lambda_0 - \lambda_S}{\lambda_S}$ . Apply  $\lambda_0 = \lambda_S \sqrt{\frac{c+v}{c-v}} = \sqrt{\frac{1+v/c}{1-v/c}}$  to solve for  $v$ . Hubble's law is given by  $v = H_0 r$ .

**SET UP:** The Hubble constant has a value of  $H_0 = 6.73 \times 10^4 \frac{\text{m/s}}{\text{Mpc}}$ .

**EXECUTE: (a)**  $1+z = 1 + \frac{(\lambda_0 - \lambda_S)}{\lambda_S} = \frac{\lambda_0}{\lambda_S}$ . Now we use  $\lambda_0 = \lambda_S \sqrt{\frac{c+v}{c-v}} = \sqrt{\frac{1+v/c}{1-v/c}}$  to obtain

$$1+z = \sqrt{\frac{c+v}{c-v}} = \sqrt{\frac{1+v/c}{1-v/c}} = \sqrt{\frac{1+\beta}{1-\beta}}$$

**(b)** Solving the above equation for  $\beta$  we obtain  $\beta = \frac{(1+z)^2 - 1}{(1+z)^2 + 1} = \frac{1.7^2 - 1}{1.7^2 + 1} = 0.4859$ . Thus,

$$v = 0.4859c = 1.46 \times 10^8 \text{ m/s.}$$

**(c)** We can use Hubble's law to find the distance to the given galaxy,

$$r = \frac{v}{H_0} = \frac{(1.46 \times 10^8 \text{ m/s})}{(6.73 \times 10^4 \text{ m/s/Mpc})} = 2.17 \times 10^3 \text{ Mpc.}$$

**EVALUATE:**  $1 \text{ pc} = 3.26 \text{ ly}$ , so the distance in part (c) is  $7.07 \times 10^9 \text{ ly}$ .

**44.35. IDENTIFY:** The reaction energy  $Q$  is defined in Chapter 43 as  $Q = (M_A + M_B - M_C - M_D)c^2$  and is the energy equivalent of the mass change in the reaction. When  $Q$  is negative the reaction is endoergic. When  $Q$  is positive the reaction is exoergic.

**SET UP:** Use the particle masses given in Section 43.1.  $1 \text{ u}$  is equivalent to  $931.5 \text{ MeV}$ .

**EXECUTE:**  $\Delta m = m_e + m_p - m_n - m_{\nu_e}$  so assuming  $m_{\nu_e} \approx 0$ ,

$$\Delta m = 0.0005486 \text{ u} + 1.007276 \text{ u} - 1.008665 \text{ u} = -8.40 \times 10^{-4} \text{ u}$$

$$\Rightarrow E = (\Delta m)c^2 = (-8.40 \times 10^{-4} \text{ u})(931.5 \text{ MeV/u}) = -0.783 \text{ MeV} \text{ and is endoergic.}$$

**EVALUATE:** The energy consumed in the reaction would have to come from the initial kinetic energy of the reactants.

**44.36. IDENTIFY:** The energy released in the reaction is the energy equivalent of the mass decrease that occurs in the reaction.

**SET UP:**  $1 \text{ u}$  is equivalent to  $931.5 \text{ MeV}$ . The neutral atom masses are given in Table 43.2.

**EXECUTE:**  $3m(^4\text{He}) - m(^{12}\text{C}) = 7.80 \times 10^{-3} \text{ u}$ , or  $7.27 \text{ MeV}$ .

**EVALUATE:** The neutral atom masses include 6 electrons on each side of the reaction equation. The electron masses cancel and we obtain the same mass change as would be calculated using nuclear masses.

**44.37. IDENTIFY and SET UP:** The Wien displacement law  $\lambda_m T = 2.90 \times 10^{-3} \text{ m} \cdot \text{K}$  says that  $\lambda_m T$  equals a constant. Use this to relate  $\lambda_{m,1}$  at  $T_1$  to  $\lambda_{m,2}$  at  $T_2$ .

**EXECUTE:**  $\lambda_{m,1} T_1 = \lambda_{m,2} T_2$ .

$$\lambda_{m,1} = \lambda_{m,2} \left( \frac{T_2}{T_1} \right) = 1.062 \times 10^{-3} \text{ m} \left( \frac{2.728 \text{ K}}{3000 \text{ K}} \right) = 966 \text{ nm.}$$

**EVALUATE:** The peak wavelength was much less when the temperature was much higher.

**44.38. IDENTIFY:** The reaction energy  $Q$  is defined in Chapter 43 as  $Q = (M_A + M_B - M_C - M_D)c^2$  and is the energy equivalent of the mass change in the reaction. When  $Q$  is negative the reaction is endoergic. When  $Q$  is positive the reaction is exoergic.

**SET UP:**  $1 \text{ u}$  is equivalent to  $931.5 \text{ MeV}$ . Use the neutral atom masses that are given in Table 43.2.

**EXECUTE:**  $m_{^{12}\text{C}} + m_{^4\text{He}} - m_{^8\text{O}} = 7.69 \times 10^{-3} \text{ u}$ , or  $7.16 \text{ MeV}$ , an exoergic reaction.

**EVALUATE:**  $7.16 \text{ MeV}$  of energy is released in the reaction.

**44.39. IDENTIFY:** The energy comes from a mass decrease.

**SET UP:** A charged pion decays into a muon plus a neutrino. The muon in turn decays into an electron or positron plus two neutrinos.

**EXECUTE:** (a)  $\pi^- \rightarrow \mu^- + \text{neutrino} \rightarrow e^- + \text{three neutrinos}$ .

(b) If we neglect the mass of the neutrinos, the mass decrease is

$$m(\pi^-) - m(e^-) = 273m_e - m_e = 272m_e = 2.480 \times 10^{-28} \text{ kg.}$$

$$E = mc^2 = 2.23 \times 10^{-11} \text{ J} = 139 \text{ MeV.}$$

(c) The total energy delivered to the tissue is  $(50.0 \text{ J/kg})(10.0 \times 10^{-3} \text{ kg}) = 0.500 \text{ J}$ . The number of

$$\pi^- \text{ mesons required is } \frac{0.500 \text{ J}}{2.23 \times 10^{-11} \text{ J}} = 2.24 \times 10^{10}.$$

(d) The RBE for the electrons that are produced is 1.0, so the equivalent dose is

$$1.0(50.0 \text{ Gy}) = 50.0 \text{ Sv} = 5.0 \times 10^3 \text{ rem.}$$

**EVALUATE:** The  $\pi$  are heavier than electrons and therefore behave differently as they hit the tissue.

**44.40. IDENTIFY:** The initial total energy of the colliding proton and antiproton equals the total energy of the two photons.

**SET UP:** For a particle with mass,  $E = K + mc^2$ . For a proton,  $m_p c^2 = 938 \text{ MeV}$ .

**EXECUTE:**  $K + m_p c^2 = \frac{hc}{\lambda}$ ,  $K = \frac{hc}{\lambda} - m_p c^2$ . Using  $\lambda = 0.720 \text{ fm} = 0.720 \times 10^{-15} \text{ m}$ , we get  $K = 784 \text{ MeV}$ .

**EVALUATE:** If the kinetic energies of the colliding particles increase, then the wavelength of each photon decreases.

**44.41. IDENTIFY:** With a stationary target, only part of the initial kinetic energy of the moving proton is available. Momentum conservation tells us that there must be nonzero momentum after the collision, which means that there must also be leftover kinetic energy. Therefore not all of the initial energy is available.

**SET UP:** The available energy is given by  $E_a^2 = 2mc^2(E_m + mc^2)$  for two particles of equal mass when one is initially stationary. The *minimum* available energy must be equal to the rest mass energies of the products, which in this case is two protons, a  $K^+$  and a  $K^-$ . The available energy must be at least the sum of the final rest masses.

**EXECUTE:** The minimum amount of available energy must be

$$E_a = 2m_p + m_{K^+} + m_{K^-} = 2(938.3 \text{ MeV}) + 493.7 \text{ MeV} + 493.7 \text{ MeV} = 2864 \text{ MeV} = 2.864 \text{ GeV.}$$

Solving the available energy formula for  $E_m$  gives  $E_a^2 = 2mc^2(E_m + mc^2)$  and

$$E_m = \frac{E_a^2}{2mc^2} - mc^2 = \frac{(2864 \text{ MeV})^2}{2(938.3 \text{ MeV})} - 938.3 \text{ MeV} = 3432.6 \text{ MeV.}$$

Recalling that  $E_m$  is the *total* energy of the proton, including its rest mass energy (RME), we have

$$K = E_m - \text{RME} = 3432.6 \text{ MeV} - 938.3 \text{ MeV} = 2494 \text{ MeV} = 2.494 \text{ GeV.}$$

Therefore the threshold kinetic energy is  $K = 2494 \text{ MeV} = 2.494 \text{ GeV}$ .

**EVALUATE:** Considerably less energy would be needed if the experiment were done using colliding beams of protons.

**44.42. IDENTIFY:** Apply Eq. (44.9).

**SET UP:** In Eq. (44.9),  $E_a = (m_{\Sigma^0} + m_{K^0})c^2$ , and with  $M = m_p$ ,  $m = m_{\pi^-}$  and  $E_m = (m_{\pi^-})c^2 + K$ ,

$$K = \frac{E_a^2 - (m_{\pi^-}c^2)^2 - (m_p c^2)^2}{2m_p c^2} - (m_{\pi^-})c^2.$$

**EXECUTE:**  $K = \frac{(1193 \text{ MeV} + 497.7 \text{ MeV})^2 - (139.6 \text{ MeV})^2 - (938.3 \text{ MeV})^2}{2(938.3 \text{ MeV})} - 139.6 \text{ MeV} = 904 \text{ MeV.}$

**EVALUATE:** The increase in rest energy is

$$(m_{\Sigma^0} + m_{K^0} - m_{\pi^-} - m_p)c^2 = 1193 \text{ MeV} + 497.7 \text{ MeV} - 139.6 \text{ MeV} - 938.3 \text{ MeV} = 613 \text{ MeV.}$$
 The

threshold kinetic energy is larger than this because not all the kinetic energy of the beam is available to form new particle states.

**44.43. IDENTIFY:** Baryon number, charge, strangeness, and lepton numbers are all conserved in the reactions. **SET UP:** Use Table 44.3 to identify the missing particle, once its properties have been determined.

**EXECUTE: (a)** The baryon number is 0, the charge is  $+e$ , the strangeness is 1, all lepton numbers are zero, and the particle is  $K^+$ .

**(b)** The baryon number is 0, the charge is  $-e$ , the strangeness is 0, all lepton numbers are zero, and the particle is  $\pi^-$ .

**(c)** The baryon number is  $-1$ , the charge is 0, the strangeness is zero, all lepton numbers are 0, and the particle is an antineutron.

**(d)** The baryon number is 0 the charge is  $+e$ , the strangeness is 0, the muonic lepton number is  $-1$ , all other lepton numbers are 0, and the particle is  $\mu^+$ .

**EVALUATE:** Rest energy considerations would determine if each reaction is endoergic or exoergic.

**44.44. IDENTIFY:** Charge must be conserved. The energy released equals the decrease in rest energy that occurs in the decay.

**SET UP:** The rest energies are given in Table 44.3.

**EXECUTE: (a)** The decay products must be neutral, so the only possible combinations are  $\pi^0\pi^0\pi^0$  or  $\pi^0\pi^+\pi^-$ .

**(b)**  $m_{\eta_0} - 3m_{\pi^0} = 142.3 \text{ MeV}/c^2$ , so the kinetic energy of the  $\pi^0$  mesons is 142.3 MeV. For the other reaction,  $K = (m_{\eta_0} - m_{\pi^0} - m_{\pi^+} - m_{\pi^-})c^2 = 133.1 \text{ MeV}$ .

**EVALUATE:** The total momentum of the decay products must be zero. This imposes a correlation between the directions of the velocities of the decay products.

**44.45. IDENTIFY and SET UP:** Apply the Heisenberg uncertainty principle in the form  $\Delta E\Delta t \approx \hbar/2$ . Let  $\Delta E$  be the energy width and let  $\Delta t$  be the lifetime.

$$\text{EXECUTE: } \frac{\hbar}{2\Delta E} = \frac{(1.054 \times 10^{-34} \text{ J}\cdot\text{s})}{2(4.4 \times 10^6 \text{ eV})(1.6 \times 10^{-19} \text{ J/eV})} = 7.5 \times 10^{-23} \text{ s}.$$

**EVALUATE:** The shorter the lifetime, the greater the energy width.

**44.46. IDENTIFY:** Apply the Heisenberg uncertainty principle in the form  $\Delta E\Delta t \approx \hbar/2$ . Let  $\Delta t$  be the mean lifetime.

**SET UP:** The rest energy of the  $\psi$  is 3097 MeV.

$$\text{EXECUTE: } \Delta t = 7.6 \times 10^{-21} \text{ s} \Rightarrow \Delta E = \frac{\hbar}{2\Delta t} = \frac{1.054 \times 10^{-34} \text{ J}\cdot\text{s}}{2(7.6 \times 10^{-21} \text{ s})} = 6.93 \times 10^{-15} \text{ J} = 43 \text{ keV}.$$

$$\frac{\Delta E}{m_{\psi}c^2} = \frac{0.043 \text{ MeV}}{3097 \text{ MeV}} = 1.4 \times 10^{-5}.$$

**EVALUATE:** The energy width due to the lifetime of the particle is a small fraction of its rest energy.

**44.47. IDENTIFY:** Apply  $\left| \frac{dN}{dt} \right| = \lambda N$  to find the number of decays in one year.

**SET UP:** Water has a molecular mass of  $18.0 \times 10^{-3} \text{ kg/mol}$ .

**EXECUTE: (a)** The number of protons in a kilogram is

$$(1.00 \text{ kg}) \left( \frac{6.022 \times 10^{23} \text{ molecules/mol}}{18.0 \times 10^{-3} \text{ kg/mol}} \right) (2 \text{ protons/molecule}) = 6.7 \times 10^{25}.$$

Note that only the protons in the hydrogen atoms are considered as possible sources of proton decay. The energy per decay is  $m_p c^2 = 938.3 \text{ MeV} = 1.503 \times 10^{-10} \text{ J}$ , and so the energy deposited in a year, per kilogram, is

$$(6.7 \times 10^{25}) \left( \frac{\ln 2}{1.0 \times 10^{18} \text{ y}} \right) (1 \text{ y}) (1.50 \times 10^{-10} \text{ J}) = 7.0 \times 10^{-3} \text{ Gy} = 0.70 \text{ rad}.$$

**(b)** For an RBE of unity, the equivalent dose is  $(1)(0.70 \text{ rad}) = 0.70 \text{ rem}$ .

**EVALUATE:** The equivalent dose is much larger than that due to the natural background. It is not feasible for the proton lifetime to be as short as  $1.0 \times 10^{18}$  y.

**44.48. IDENTIFY and SET UP:**  $\phi \rightarrow K^+ + K^-$ . The total energy released is the energy equivalent of the mass decrease.

**EXECUTE: (a)** The mass decrease is  $m(\phi) - m(K^+) - m(K^-)$ . The energy equivalent of the mass decrease is  $mc^2(\phi) - mc^2(K^+) - mc^2(K^-)$ . The rest mass energy  $mc^2$  for the  $\phi$  meson is given Problem 44.45, and the values for  $K^+$  and  $K^-$  are given in Table 44.3. The energy released then is  $1019.4 \text{ MeV} - 2(493.7 \text{ MeV}) = 32.0 \text{ MeV}$ . The  $K^+$  gets half this, 16.0 MeV.

**EVALUATE: (b)** Does the decay  $\phi \rightarrow K^+ + K^- + \pi^0$  occur? The energy equivalent of the  $K^+ + K^- + \pi^0$  mass is  $493.7 \text{ MeV} + 493.7 \text{ MeV} + 135.0 \text{ MeV} = 1122 \text{ MeV}$ . This is greater than the energy equivalent of the  $\phi$  mass. The mass of the decay products would be greater than the mass of the parent particle; the decay is energetically forbidden.

**(c)** Does the decay  $\phi \rightarrow K^+ + \pi^-$  occur? The reaction  $\phi \rightarrow K^+ + K^-$  is observed.  $K^+$  has strangeness +1 and  $K^-$  has strangeness -1, so the total strangeness of the decay products is zero. If strangeness must be conserved we deduce that the  $\phi$  particle has strangeness zero.  $\pi^-$  has strangeness 0, so the product  $K^+ + \pi^-$  has strangeness -1. The decay  $\phi \rightarrow K^+ + \pi^-$  violates conservation of strangeness. Does the decay  $\phi \rightarrow K^+ + \mu^-$  occur?  $\mu^-$  has strangeness 0, so this decay would also violate conservation of strangeness.

**44.49. IDENTIFY:** The matter density is proportional to  $1/R^3$ .

**SET UP and EXECUTE: (a)** When the matter density was large enough compared to the dark energy density, the slowing due to gravitational attraction would have dominated over the cosmic repulsion due to dark energy.

**(b)** Matter density is proportional to  $1/R^3$ , so  $R \propto \frac{1}{\rho^{1/3}}$ . Therefore  $\frac{R}{R_0} = \left(\frac{1/\rho_{\text{past}}}{1/\rho_{\text{now}}}\right)^{1/3} = \left(\frac{\rho_{\text{now}}}{\rho_{\text{past}}}\right)^{1/3}$ . If  $\rho_m$

and  $\rho_{\text{DE}}$  are the present-day densities of matter of all kinds and of dark energy, we have  $\rho_{\text{DE}} = 0.726\rho_{\text{crit}}$  and  $\rho_m = 0.274\rho_{\text{crit}}$  at the present time. Putting this into the above equation for  $R/R_0$  gives

$$\frac{R}{R_0} = \left(\frac{0.274}{0.726} \frac{\rho_{\text{DE}}}{2\rho_{\text{DE}}}\right)^{1/3} = 0.574.$$

**EVALUATE: (c)** 300 My: speeding up ( $R/R_0 = 0.98$ ); 13.1 Gy: slowing down ( $R/R_0 = 0.12$ ).

**44.50. IDENTIFY:** The energy comes from the mass difference.

**SET UP:**  $\Xi^- \rightarrow \Lambda^0 + \pi^-$ .  $p_\Lambda = p_\pi = p$ .  $E_\Xi = E_\Lambda + E_\pi$ .  $m_\Xi c^2 = 1321 \text{ MeV}$ .  $m_\Lambda c^2 = 1116 \text{ MeV}$ .

$$m_\pi c^2 = 139.6 \text{ MeV}. \quad m_\Xi c^2 = \sqrt{m_\Lambda^2 c^4 + p^2 c^2} + \sqrt{m_\pi^2 c^4 + p^2 c^2}.$$

**EXECUTE: (a)** The total energy released is

$$m_\Xi c^2 - m_\pi c^2 - m_\Lambda c^2 = 1321 \text{ MeV} - 139.6 \text{ MeV} - 1116 \text{ MeV} = 65.4 \text{ MeV}.$$

**(b)**  $m_\Xi c^2 = \sqrt{m_\Lambda^2 c^4 + p^2 c^2} + \sqrt{m_\pi^2 c^4 + p^2 c^2}$ .  $m_\Xi c^2 - \sqrt{m_\Lambda^2 c^4 + p^2 c^2} = \sqrt{m_\pi^2 c^4 + p^2 c^2}$ . Square both sides:

$$m_\Xi^2 c^4 + m_\Lambda^2 c^4 + p^2 c^2 - 2m_\Xi c^2 E_\Lambda = m_\pi^2 c^4 + p^2 c^2. \quad E_\Lambda = \frac{m_\Xi^2 c^4 + m_\Lambda^2 c^4 - m_\pi^2 c^4}{2m_\Xi c^2}.$$

$$K_\Lambda = \frac{m_\Xi^2 c^4 + m_\Lambda^2 c^4 - m_\pi^2 c^4}{2m_\Xi c^2} - m_\Lambda c^2. \quad E_\pi = E_\Xi - E_\Lambda = m_\Xi c^2 - \frac{m_\Xi^2 c^4 + m_\Lambda^2 c^4 - m_\pi^2 c^4}{2m_\Xi c^2}.$$

$$E_\pi = \frac{m_\Xi^2 c^4 - m_\Lambda^2 c^4 + m_\pi^2 c^4}{2m_\Xi c^2}. \quad K_\pi = \frac{m_\Xi^2 c^4 - m_\Lambda^2 c^4 + m_\pi^2 c^4}{2m_\Xi c^2} - m_\pi c^2. \quad \text{Putting in numbers gives}$$

$$K_{\Lambda} = \frac{(1321 \text{ MeV})^2 + (1116 \text{ MeV})^2 - (139.6 \text{ MeV})^2}{2(1321 \text{ MeV})} - 1116 \text{ MeV} = 8.5 \text{ MeV} \quad (13\% \text{ of total}).$$

$$K_{\pi} = \frac{(1321 \text{ MeV})^2 - (1116 \text{ MeV})^2 + (139.6 \text{ MeV})^2}{2(1321 \text{ MeV})} - 139.6 \text{ MeV} = 56.9 \text{ MeV} \quad (87\% \text{ of total}).$$

**EVALUATE:** The two particles do not have equal kinetic energies because they have different masses.

**44.51. IDENTIFY:** The kinetic energy comes from the mass difference.

**SET UP and EXECUTE:**  $K_{\Sigma} = 180 \text{ MeV}$ .  $m_{\Sigma}c^2 = 1197 \text{ MeV}$ .  $m_n c^2 = 939.6 \text{ MeV}$ .  $m_{\pi}c^2 = 139.6 \text{ MeV}$ .

$E_{\Sigma} = K_{\Sigma} + m_{\Sigma}c^2 = 180 \text{ MeV} + 1197 \text{ MeV} = 1377 \text{ MeV}$ . Conservation of the  $x$ -component of momentum gives  $p_{\Sigma} = p_{nx}$ . Then  $p_{nx}^2 c^2 = p_{\Sigma}^2 c^2 = E_{\Sigma}^2 - (m_{\Sigma}c)^2 = (1377 \text{ MeV})^2 - (1197 \text{ MeV})^2 = 4.633 \times 10^5 \text{ (MeV)}^2$ .

Conservation of energy gives  $E_{\Sigma} = E_{\pi} + E_n$ .  $E_{\Sigma} = \sqrt{m_{\pi}^2 c^4 + p_{\pi}^2 c^2} + \sqrt{m_n^2 c^4 + p_n^2 c^2}$ .

$E_{\Sigma} - \sqrt{m_n^2 c^4 + p_n^2 c^2} = \sqrt{m_{\pi}^2 c^4 + p_{\pi}^2 c^2}$ . Square both sides:

$$E_{\Sigma}^2 + m_n^2 c^4 + p_{nx}^2 c^2 + p_{ny}^2 c^2 - 2E_{\Sigma}E_n = m_{\pi}^2 c^4 + p_{\pi}^2 c^2. \quad p_{\pi} = p_{ny} \text{ so}$$

$$E_{\Sigma}^2 + m_n^2 c^4 + p_{nx}^2 c^2 - 2E_{\Sigma}E_n = m_{\pi}^2 c^4 \text{ and } E_n = \frac{E_{\Sigma}^2 + m_n^2 c^4 - m_{\pi}^2 c^4 + p_{nx}^2 c^2}{2E_{\Sigma}}.$$

$$E_n = \frac{(1377 \text{ MeV})^2 + (939.6 \text{ MeV})^2 - (139.6 \text{ MeV})^2 + 4.633 \times 10^5 \text{ (MeV)}^2}{2(1377 \text{ MeV})} = 1170 \text{ MeV}.$$

$$K_n = E_n - m_n c^2 = 1170 \text{ MeV} - 939.6 \text{ MeV} = 230 \text{ MeV}.$$

$$E_{\pi} = E_{\Sigma} - E_n = 1377 \text{ MeV} - 1170 \text{ MeV} = 207 \text{ MeV}.$$

$$K_{\pi} = E_{\pi} - m_{\pi}c^2 = 207 \text{ MeV} - 139.6 \text{ MeV} = 67 \text{ MeV}.$$

$p_n^2 c^2 = E_n^2 - m_n^2 c^4 = (1170 \text{ MeV})^2 - (939.6 \text{ MeV})^2 = 4.861 \times 10^5 \text{ (MeV)}^2$ . The angle  $\theta$  the velocity of the

neutron makes with the  $+x$ -axis is given by  $\cos \theta = \frac{p_{nx}}{p_n} = \sqrt{\frac{4.633 \times 10^5}{4.861 \times 10^5}}$  and  $\theta = 12.5^\circ$  below the  $+x$ -axis.

**EVALUATE:** The decay particles do not have equal energy because they have different masses.

**44.52. IDENTIFY:** The kinetic energy comes from the mass difference, and momentum is conserved.

**SET UP:**  $|p_{\pi^+ y}| = |p_{\pi^- y}|$ .  $p_{\pi^+} \sin \theta = p_{\pi^-} \sin \theta$  and  $p_{\pi^+} = p_{\pi^-} = p_{\pi}$ .  $m_K c^2 = 497.7 \text{ MeV}$ .

$$m_{\pi}c^2 = 139.6 \text{ MeV}.$$

**EXECUTE:** Conservation of momentum for the decay gives  $p_K = 2p_{\pi x}$  and  $p_K^2 = 4p_{\pi x}^2$ .

$$p_K^2 c^2 = E_K^2 - m_K^2 c^4. \quad E_K = 497.7 \text{ MeV} + 225 \text{ MeV} = 722.7 \text{ MeV} \text{ so}$$

$$p_K^2 c^2 = (722.7 \text{ MeV})^2 - (497.7 \text{ MeV})^2 = 2.746 \times 10^5 \text{ (MeV)}^2 \text{ and}$$

$$p_{\pi x}^2 c^2 = [2.746 \times 10^5 \text{ (MeV)}^2] / 4 = 6.865 \times 10^4 \text{ (MeV)}^2. \text{ Conservation of energy says } E_K = 2E_{\pi}.$$

$$E_{\pi} = \frac{E_K}{2} = 361.4 \text{ MeV}. \quad K_{\pi} = E_{\pi} - m_{\pi}c^2 = 361.4 \text{ MeV} - 139.6 \text{ MeV} = 222 \text{ MeV}.$$

$p_{\pi}^2 c^2 = E_{\pi}^2 - (m_{\pi}c^2)^2 = (361.4 \text{ MeV})^2 - (139.6 \text{ MeV})^2 = 1.11 \times 10^5 \text{ (MeV)}^2$ . The angle  $\theta$  that the velocity

of the  $\pi^+$  particle makes with the  $+x$ -axis is given by  $\cos \theta = \sqrt{\frac{p_{\pi x}^2 c^2}{p_{\pi}^2 c^2}} = \sqrt{\frac{6.865 \times 10^4}{1.11 \times 10^5}}$ , which gives

$$\theta = 38.2^\circ.$$

**EVALUATE:** The pions have the same energy and go off at the same angle because they have equal masses.

**44.53. IDENTIFY and SET UP:** For nonrelativistic motion, the maximum kinetic energy in a cyclotron is

$$K_{\max} = \frac{q^2 R^2}{2m} B^2. \text{ The angular frequency is } \omega = |q|B/m.$$

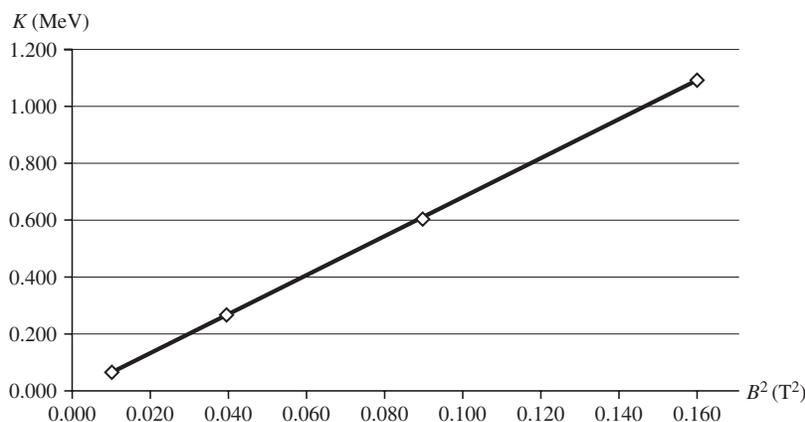
**EXECUTE: (a)** The rest energy of a proton is 938 MeV, and the kinetic energies in the data table in the problem are around 1 MeV or less, so there is no need to use relativistic expressions.

**(b)** Figure 44.53 shows the graph of  $K_{\max}$  versus  $B^2$  for the data in the problem. The graph is clearly a straight line and has slope equal to  $6.748 \text{ MeV/T}^2 = 1.081 \times 10^{-12} \text{ J/T}^2$ . The formula for  $K_{\max}$  is

$$K_{\max} = \frac{q^2 R^2}{2m} B^2, \text{ so a graph of } K_{\max} \text{ versus } B^2 \text{ should be a straight line with slope equal to } q^2 R^2/2m.$$

Solving  $q^2 R^2/2m = \text{slope}$  for  $R$  gives

$$R = \sqrt{\frac{2m(\text{slope})}{q^2}} = \sqrt{\frac{2(1.673 \times 10^{-27} \text{ kg})(1.081 \times 10^{-12} \text{ J/T}^2)}{(1.602 \times 10^{-19} \text{ C})^2}} = 0.375 \text{ m} = 37.5 \text{ cm}.$$



**Figure 44.53**

**(c)** Using the result from our graph, we get

$$K_{\max} = (\text{slope})B^2 = (6.748 \text{ MeV/T}^2)(0.25 \text{ T})^2 = 0.42 \text{ MeV}.$$

**(d)** The angular speed is  $\omega = |q|B/m = (1.602 \times 10^{-19} \text{ C})(0.40 \text{ T})/(1.67 \times 10^{-27} \text{ kg}) = 3.8 \times 10^7 \text{ rad/s}$ .

**EVALUATE:** In part (c) we can check by using  $K_{\max} = q^2 R^2 B^2/2m = (qRB)^2/2m$ . Using  $B = 0.25 \text{ T}$  and the standard values for the other quantities gives  $K_{\max} = 6.75 \times 10^{-14} \text{ J} = 0.42 \text{ MeV}$ , which agrees with our result.

**44.54. IDENTIFY:** Use Table 44.3 for data on the given particles. Apply conservation of energy in part (b).

**SET UP:** For any decay, conservation of energy tells us that  $E_i = E_f$ . If the decaying particle is at rest (or in its rest frame), this gives  $m_i c^2 = m_{\text{products}} c^2 + K$ .

**EXECUTE: (a)** The masses from Table 44.3 are:

$$\Sigma^- : 1197 \text{ MeV}/c^2$$

$$\Xi^0 : 1315 \text{ MeV}/c^2$$

$$\Delta^{++} : 1232 \text{ MeV}/c^2$$

$$\Omega^- : 1672 \text{ MeV}/c^2$$

We see that  $\Omega^-$  has the largest mass and  $\Sigma^-$  has the smallest mass.

**(b)** Solving  $m_i c^2 = m_{\text{products}} c^2 + K$  for  $K$  gives  $K = (m_i - m_{\text{products}})c^2$ . Therefore the greater the difference between the mass of the decaying particle and the mass of decay products, the greater the kinetic energy.

We show the decays and the mass differences below.

$$\Sigma^- \rightarrow n + \pi^- : K = (1197 - 939.6 - 139.6) \text{ MeV}/c^2 = 117.8 \text{ MeV}/c^2$$

$$\Xi^0 \rightarrow \Lambda^0 + \pi^0 : K = (1315 - 1116 - 135) \text{ MeV}/c^2 = 64 \text{ MeV}/c^2$$

$$\Delta^{++} \rightarrow p + \pi^+ : K = (1232 - 938.3 - 139.6) \text{ MeV}/c^2 = 154.1 \text{ MeV}/c^2$$

$$\Omega^- \rightarrow \Lambda^0 + K^- : K = (1672 - 1116 - 493.7) \text{ MeV}/c^2 = 62.3 \text{ MeV}/c^2$$

The kinetic energy is largest for the  $\Delta^{++}$  decay and smallest for the  $\Omega^-$  decay.

**EVALUATE:** A large-mass particle does not necessarily result in the release of more kinetic energy. For example, the  $\Omega^-$  particle has more mass than the  $\Delta^{++}$ , yet the decay products of the  $\Omega^-$  have less kinetic energy than those of the  $\Delta^{++}$  decay.

**44.55. IDENTIFY and SET UP:** Construct the diagram as specified in the problem. In part (b), use quark charges  $u = +\frac{2}{3}$ ,  $d = -\frac{1}{3}$ , and  $s = -\frac{1}{3}$  as a guide.

**EXECUTE: (a)** The diagram is given in Figure 44.55. The  $\Omega^-$  particle has  $Q = -1$  (as its label suggests) and  $S = -3$ . It appears as a “hole” in an otherwise regular lattice in the  $S - Q$  plane.

**(b)** The quark composition of each particle is shown in the figure.

**EVALUATE:** The mass difference between each  $S$  row is around 145 MeV (or so). This puts the  $\Omega^-$  mass at about the right spot. As it turns out, all the other particles on this lattice had been discovered already and it was this “hole” and mass regularity that led to an accurate prediction of the properties of the  $\Omega^-$ !

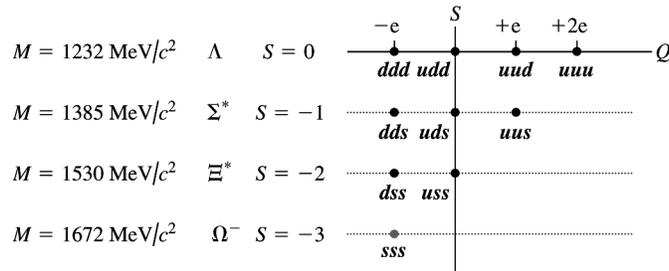


Figure 44.55

**44.56. IDENTIFY:** Follow the steps specified in the problem. The Lorentz velocity transformation is given by

$$v_x = \frac{v'_x + u}{1 + uv'_x/c^2}$$

**SET UP:** Let the  $+x$ -direction be the direction of the initial velocity of the bombarding particle.

**EXECUTE: (a)** For mass  $m$ , in  $v_x = \frac{v'_x + u}{1 + uv'_x/c^2}$ ,  $u = -v_{\text{cm}}$ ,  $v' = v_0$ , and so  $v_m = \frac{v_0 - v_{\text{cm}}}{1 - v_0 v_{\text{cm}}/c^2}$ . For mass

$$M, u = -v_{\text{cm}}, v' = 0, \text{ so } v_M = -v_{\text{cm}}.$$

**(b)** The condition for no net momentum in the center of mass frame is  $m\gamma_m v_m + M\gamma_M v_M = 0$ , where  $\gamma_m$  and  $\gamma_M$  correspond to the velocities found in part (a). The algebra reduces to

$$\beta_m \gamma_m = (\beta_0 - \beta') \gamma_0 \gamma_M, \text{ where } \beta_0 = \frac{v_0}{c}, \beta' = \frac{v_{\text{cm}}}{c}, \text{ and the condition for no net momentum becomes}$$

$$m(\beta_0 - \beta') \gamma_0 \gamma_M = M \beta' \gamma_M, \text{ or } \beta' = \frac{\beta_0}{1 + \frac{M}{m\gamma_0}} = \beta_0 \frac{m}{m + M\sqrt{1 - \beta_0^2}}. \quad v_{\text{cm}} = \frac{mv_0}{m + M\sqrt{1 - (v_0/c)^2}}$$

**(c)** Substitution of the above expression into the expressions for the velocities found in part (a) gives the relatively simple forms  $v_m = v_0 \gamma_0 \frac{M}{m + M\gamma_0}$ ,  $v_M = -v_0 \gamma_0 \frac{m}{m\gamma_0 + M}$ . After some more algebra,

$$\gamma_m = \frac{m + M\gamma_0}{\sqrt{m^2 + M^2 + 2mM\gamma_0}}, \gamma_M = \frac{M + m\gamma_0}{\sqrt{m^2 + M^2 + 2mM\gamma_0}}, \text{ from which}$$

$$m\gamma_m + M\gamma_M = \sqrt{m^2 + M^2 + 2mM\gamma_0}. \text{ This last expression, multiplied by } c^2, \text{ is the available energy } E_a$$

in the center of mass frame, so that

$$E_a^2 = (m^2 + M^2 + 2mM\gamma_0)c^4 = (mc^2)^2 + (Mc^2)^2 + (2Mc^2)(m\gamma_0c^2) = (mc^2)^2 + (Mc^2)^2 + 2Mc^2E_m, \text{ which is Eq. (44.9).}$$

**EVALUATE:** The energy  $E_a$  in the center-of-momentum frame is the energy that is available to form new particle states.

**44.57. IDENTIFY and SET UP:** Energy and momentum are conserved.

**EXECUTE:** The positron is moving slowly, so its only appreciable energy is its rest energy  $m_e c^2$ . The total energy released by the annihilation is  $2m_e c^2$ , but the two photons share it equally to conserve momentum. Therefore they also have equal energy, so each photon has energy  $m_e c^2$ , which is choice (d).

**EVALUATE:** If the positron had significant kinetic energy, the two photons would not have the same momentum and hence would not have the same energy.

**44.58. IDENTIFY and SET UP:** One photon travels 3 cm longer than the other one. If  $2L$  is the distance between the detectors, one photon travels a distance  $L + 3$  cm and other a distance  $L - 3$  cm. The time for a photon to travel a distance  $x$  is  $t = x/c$ .

**EXECUTE:**  $t_1 = (L + 3 \text{ cm})/c$  and  $t_2 = (L - 3 \text{ cm})/c$ . The time interval  $\Delta t$  between the arrival of the two photons is  $\Delta t = t_1 - t_2 = (L + 3 \text{ cm})/c - (L - 3 \text{ cm})/c = (6 \text{ cm})/c = (0.06 \text{ m})/c = 0.2 \times 10^{-9} \text{ s} = 0.2 \text{ ns}$ . This is within the 10-ns window, so the two photons will be counted as simultaneous. Thus choice (d) is correct.

**EVALUATE:** 0.2 ns is well within the 10-ns window for simultaneity. The annihilation would have to occur over 1.5 m from the center for the photons not to be counted as simultaneous.

**44.59. IDENTIFY and SET UP:** The absorption of photons obeys the equation  $N = N_0 e^{-\mu x}$ , where  $\mu = 0.1 \text{ cm}^{-1}$ .

**EXECUTE:**  $N/N_0 = e^{-\mu x} = e^{-(0.1 \text{ cm}^{-1})(20 \text{ cm})} = 0.14 = 14\%$ . Choice (c) is correct.

**EVALUATE:** If 14% of the photons exit the body, 86% were absorbed within 20 cm of tissue.