# Solutions Manual for <br> Essentials of Chemical Reaction Engineering 

Second Edition

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## WEB HOME PAGE



## Welcome to the Elements of Chemical Reaction Engineering 5th Edition Homepage!




# INTERACTIVE COMPUTER GAMES (ICGs) 



## Interactive Computer Games (ICGs)

俍 itie. Note that there will be a pause while the game is loaded from our servers. Aiternately, one can use the install to PC link to install each game on the PC. This instaliation will typically install an icon on the desktop. Please take the default location for the installation files. Detailed instructions for installing and using the ICGs are available.
As these interactive games are played, the player will be asked a number of questions related to the corresponding material in the textbook. The computer will keep track of al the correct answers and at the end of the game will display a codec performance number that reflects how well the player mastered the material in the text. Instructors will have a manuai to decode the performance number.
Note: The Interantive Computer Games may NOT work on approximately $10 \%$ of Windows manhines. We can't lind a speafic reason, so it it doesht woric, please try them on a different Windows computer.
Kinatics Challengel ( install to PC. Installation instructions)
Quiz Show
Introduction to Kinetics
Description of the Module
Objectives for Chapter One
Staging (Install to PC , Installation instructions)
Reactor Sequencing Optimization
Description of the Module
Objectives for Chapter Two
Kinetics Challenge if ( install to PC, Installation Instructions)
Quiz Show
Stolchlometry and Rate Laws
Descniption of the Module
Objectives for Chapter Four
Murder Mystery( Instali to PC. Instaliation instructions)
CSTR Volume Algorithm
Description of the Module
Objectives for Chapter Five
Tic Tac Toe ( Install to PC. Installation Instructions)
sothermal Reactor Design: Ergun, Arrhenius, and Van't Hoff Equations
Description of the Module
Objectives for Chapter Six
Ecology A Wetiands Problem (Install to PC, Installation Instructions)
Collection and Analysis of Rate Date: Ecological Engineering
Description of the Module
Objectives for Chapter Sever
Great Race ( install to PC , Installation instructions)
Muittiple Reactions
Description of the Module
Objectives for Chapter Eligh
Enzyme Man (Install to PC, Installation Instructions)
Enzyme Kinetics
Description of the Module
Objectives for Chapter Nine
Heterogeneous Catalysis (install to PC, Installation instructions)
Catalytic Rate Equations, Status: Alpha Release
Wsining: This module is not fully tested, You may encounter abnormal behavior,
Description of the Medule
Objectives for Chaptor Ten
Heat Effects 1 ( instali 10 PC. Installation instructions)
Basketball Challenge
Mole and Energy Balances in a CSTR
Description of the Module
Objectives for Chapter Thirteen
Heat Effects 2 (Install to PC, Installation instructions)
Effect of Parameter Variation on a PFR
Mole and Energy Balances in a PFR, Status: Alpha Release
Warring: This module is not fully tested. You may encounter abnormal behavion
Description of the Module
Objectives for Chapter Thirteen


Interactive Computer Games (ICGs)
Kinetic Challenge 1



# ALGORITHM TO DECODE ICGs 

**** CONFIDENTIAL ****

# UNIVERSITY OF MICHIGAN <br> INTERACTIVE COMPUTER MODULES FOR CHEMICAL ENGINEERING CHEMICAL REACTION ENGINEERING MODULES 

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M. Nihat Gürmen, Project Manager (2002-2004)

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## INTERPRETATION OF PERFORMANCE NUMBERS

Students should record their Performance Number for each program, along with the name of the program, and turn it in to the instructor. The Performance Number for each program is decoded as described in the following pages.

The official site for the distribution of the modules is http://www.engin.umich.edu/~cre/icm

Please report problems to icm.support@umich.edu.

# ICMs with Windows ${ }^{\circledR}$ interface 

Module Format
KINETIC CHALLENGE I
CzBzzAzz
\%
Interpretation

Score $=1.5$ * AB.C
$\mathrm{z}=$ random numbers

Note: $75 \%$ constitutes mastery.

## Example

Perf. No. $=\underline{\mathbf{7} 5} \underline{\mathbf{2}} \mathbf{4}_{\underline{\mathbf{6}}} \mathbf{9} 2$
Score $=1.5^{*}(62.7)=94$

## KINETIC CHALLENGE II

CzBzzAzz
\%
Score $=2.0$ * AB.C
Perf. No. $=\underline{\mathbf{0}} \mathbf{3} \underline{7} 76 \underline{\mathbf{4}} 67$
$\mathrm{z}=$ random numbers
Note: $75 \%$ constitutes mastery.

## MURDER MYSTERY

zzAzz

A even: Killer and victim correctly identified
A odd: Killer and victim not identified
$\mathrm{z}=$ random numbers
Note: An even number for the middle digit constitutes
mastery.

## TIC TAC TOE

Score $=4.0$ * AB.C $\mathrm{z}=$ random numbers

Perf. No. $=7 \underline{7} 8 \underline{0} \underline{5} 8 \underline{1}$
Score $=4 *(15.0)=60$ configuration 7
completed

## Configurations



Note: Student receives 20 points for every square answered correctly. A score of 60 is needed for mastery of this module.

## GREAT RACE

zzzCzABz
Score $=6.0$ * AB.C
Perf. No. $=777 \underline{3} 8 \underline{078}$
$\mathrm{z}=$ random numbers
Score $=6^{*}(07.3)=44$
Note: A score of 40 is needed for mastery of this
module.

## AzBCzaaD <br> $\mathrm{z}=$ random numbers <br> $\mathrm{a}=$ random characters

A gives info on $r^{\wedge} 2$ value of the student's linearized plot
$\mathrm{A}=\mathrm{Y}$ if $\mathrm{r}^{\wedge} 2>=0.9$
$\mathrm{A}=\mathrm{A}$ if $0.9>\mathrm{r}^{\wedge} 2>=0.8$
$\mathrm{A}=\mathrm{X}$ if $0.8>\mathrm{r}^{\wedge} 2>=0.7$
$\mathrm{A}=\mathrm{F}$ if $0.7>\mathrm{r}^{\wedge} 2$
$\mathrm{A}=\mathrm{Q}$ if Wetland Analysis/Simulator portion has not been completed
B gives info on alpha
$\mathrm{B}=1$ to $4 \Rightarrow>$ student's alpha $<$ (simulator's alpha $\pm 0.5$ )
$\mathrm{B}=5$ to $9 \Rightarrow>$ student's alpha $>$ (simulator's alpha $\pm 0.5$ )
$\mathrm{B}=\mathrm{X}$ if Wetland Analysis/Simulator portion has not been completed
C indicates number of data points deactivated during analysis
$\mathrm{C}=$ number of deactivated data points if at least 1 point has been deactivated
$\mathrm{C}=\mathrm{a}$ randomly generated letter from A to Y if 0 points deactivated
$\mathrm{C}=\mathrm{Z}$ if Wetland Analysis/Simulator portion has not been completed
D gives info on solution method used by student
$\mathrm{D}=1$ if polynomial regression was used
$D=2$ if differential formulas were used
$\mathrm{D}=3$ if graphical differentiation was used
$\mathrm{D}=4$ to 9 if Wetland Analysis/Simulator portion has not been completed
Perf No. $=\underline{A} 7 \underline{213 D F} \underline{2}$

1) $\mathrm{A}=>0.9>\mathrm{r}^{\wedge} 2>=0.8$
2) $2 \Rightarrow$ student's alpha $<$ (simulator's alpha $\pm 0.5$ )
3) $1=>$ one data point was deactivated
4) $2=>$ differential formulas were used

## STAGING

| zCBzAFzED | $\mathbf{z}=$ random numbers |
| :---: | :--- |
| Final conversion $=2 *$ AB.C | Perf. No. $=\mathbf{2 \underline { \mathbf { 1 2 5 } 5 } \mathbf { 4 } \mathbf { 2 } \mathbf { 9 } \underline { \mathbf { 3 } }}$ |
| Final flow rate $=2 *$ DE. | conversion $=2 * 42.1=84.2$ |
| flow rate $=2 * 31.2=62.4$ |  |

Please make a pass/fail criterion based on these values.

## ICMs with Dos ${ }^{\circledR}$ interface

## Module Format

Interpretation

## Example

HETCAT

$$
\text { zzABzCD } \quad \mathrm{A}=2,3,5,7: \text { interaction done } \quad \text { Perf. No. }=80 \underline{27} \underline{355}
$$

$B=2,3,5,7$ : intro done
A: Worked on
interaction
values,
$\mathrm{C}=2,3,5,7$ : review done
B: Looked at intro
D denotes how much they
C: Looked at review did in the interaction: D: found parameter mechanism

$$
\begin{array}{ll}
\mathrm{D}<2 & \text { Not done } \\
2<\mathrm{D}: 5 & 4 \\
\text { Dependences } \\
\text { 4<D:5 } & \text { Parameter values } \\
\text { 6<D } \quad \text { Mechanism } \\
\mathrm{z}=\text { random numbers }
\end{array}
$$

Note: Performance number given only if student goes through the interaction portion of the module

HEATFX1

```
zzAzz A even: score > 85 %
\(\mathrm{z}=\) random numbers
Perf. No. \(=53 \underline{\mathbf{6}} 07\)
Score > 85 \%
```

Note: Student told they have achieved mastery if their score is greater than $85 \%$

HEATFX2
zzzAzz
A even: completed interaction $\mathrm{z}=$ random numbers

Perf. No. $=407 \underline{5} 82$ Interaction not
completed
Note: Performance number given only if student goes through the interaction portion of the module.

# LIVING EXAMPLE PROBLEMS (LEPs) 



## Chapter 12: Steady-State Nonisothermal Reactor Design: Flow Reactors with Heat Exchange

Living Example Problems
The following examples can be accessed with Polymath ${ }^{\text {ru }}$, MATLAB ${ }^{\text {M }}$, or Woiffam ODF Playerth

| Living Example Problem | Polymath ${ }^{\text {TM }}$ Code | Maxiab Code | Woltram CDF Code | Aspentech ${ }^{\text {tm }}$ |
| :---: | :---: | :---: | :---: | :---: |
| Example 12-1 isomerization of Normal Butane with Heat Exchenger | a) Co-currant: LEP-12. <br> 1apol <br> b) Countercurrent: LEP- <br> 12-1b.001 <br> c) Constant $T_{A}:$ LEP-12 <br> 1C.pol <br> d) Adiabatic: LEP-12- <br> 1d.pol | a) Co-current: LEP. 12-1azie <br> b) Countercurrent: <br> LEP-12-1b.zie <br> c) Constant $\mathrm{T}_{3}$ ' LEEP. <br> 12-1czip <br> d) Adiabatic: LEP-T2- <br> 1d.zle | a) Co-current: LEP-12. la.cal <br> b) Countercurrent: LEP-12-16.caf <br> a) Constant Ti LEP. <br> 12-1c.cad <br> d) Adiabatic: LEP-12- <br> Id. Cdf | -. |
| Example 12-2 Production of Acetic Anhydride | a) Adiabatic: LEP-12. Rapol <br> b) Constant $T_{2}$ LEP- <br> 12-2b.00\| <br> c) Co-current LEP-12. <br> 2c.pol <br> d) Countercurrent: LEP- <br> 12-2d.pol | a) Adiabatic: EP-12zazip <br> b) Constant $\mathrm{T}_{\mathrm{a}}$ : LEP- <br> 12-2b-zip <br> c) Co-current: LEP- <br> 12-2czip <br> d) Countercurrent: <br> LEP-12-2d.210 | a) Aciabatic: LEP-12. Racdf <br> b) Constant $T_{3} \div$ LEP- <br> 12-2b, cdf <br> c) Co-current: LEP-12. <br> 2c.odf <br> d) Countercurrent: <br> LEP-12-20.001 | a) Adiabatic: Iutorial. ASPEN Backup File <br> b) Constant Heat Exchange: Tutorie, ASPEN Backup File |
| Example 12-3 Production of Propylene Glycol in an Adiabatic CSTR | - | -- | LEP-2-3. off | - |
| Example 12-4 CSTR with a Cooling Coil | LEP-12-4.001 | LEP-12-4.zip | LEP-12-4.0才t | -r |
| Example 12-6 Parallel Reaction in a PFR with Heat Effects | LEP-12-5.pol | LEP-12-5.210 | LEP-12-5.codi | - |
| Example 12-6 Multiple Reactions in a CSTR | LEP-12-6.pol Alternative Solution: LEP-12-6a.pol | LEEP-12-6.2ip | LEP-12-6.0.df | - |
| Example 12-7 Complex Reactions | a) Co-Current LEP-12: <br> 7a.pol <br> D) Countercurrent: LEP- <br> 12.7 b .ool <br> c) Constant $T_{a}$. LEP-12- <br> 7raod <br> d) Adiabatic: LEP-12- <br> 70.001 | a) Co-current: LEP-12-7az1p <br> b) Countercurrent; <br> LEP-12-76.2]\| <br> c) Constant $\mathrm{T}_{n}$ : LEP - <br> 12-7c.zip <br> d) Adiabatic: LEP-12- <br> 70.2ie | a) Co-ourrent: LEP-12Ta.cdt <br> b) Countercurrent: <br> LEP-12-7b.cdf <br> C) Constant Tallep: <br> 12-7c.codf <br> ब) Adiabatie: LEP-12- <br> 7a.cadr | - |
| Example R12-1 industrial Oxidation of $\mathrm{SO}_{2}$ | LEP-RET2-1.pol | LEP-RE12-121P | - | - |
| Example 12-T12-3 PBR with Variable Coolant Temperature | LEP-T12-3.pol | LEP-T12-9.2i9 | LEP-T12-3.cdi | - |
| Example Lecture 19 $\mathrm{A}=\mathrm{B}$ Adiabatic | Acliabatic $A=B$ pol | ... | Adiabatic A B B.cdf | - |

## SAMPLE COURSE SYLLABUS

## ChE 344: CHEMICAL REACTION ENGINEERING

Fundamentals of chemical reaction engineering. Rate laws, kinetics, and mechanisms of homogeneous and heterogeneous reactions. Analysis of rate data, multiple reactions, heat effects, bioreactors. Design of industrial reactors.
Prerequisite: ChE 330, ChE 342
Fall 2015
Lectures: M,W 8:40 (Sharp) to 10:30 (not so sharp) - Room: 1013 Dow
Instructor:
Professor H. Scott Fogler
3168 DOW, 763-1361, sfogler@umich.edu
Office Hours: M, W 10:30a to 11:30a
Course assistants include: Instructional aids, tutor, proctors, and graders
Text Required
Elements of Chemical Reaction Engineering, $5^{\text {th }}$ edition, H. Scott Fogler
Web site: www.umich.edu/~elements/5e
Recommended Reading List

- Problem Solving in Chemical and Biochemical Engineering with POLYMATH, Excel, and MATLAB, 2nd Edition 2008, Cutlip \& Shacham
- The Elements of Style, Strunk and White
- Strategies for Creative Problem Solving, 3rd Edition 2014, Fogler, LeBlanc \& Rizzo (for OEP's)

Schedule
*Note - all ICGs (Interactive Computer Games) are Individual*

1) Wednesday, September 9

Topic: $\quad$ Lecture 1 - Chapter 1, Introduction, POLYMATH, Mole balances
Read: Preface, Prerequisites, Appendix B
In-Class Problem: No In-Class Problem
2) Monday, September 14

Topic: Lecture 2 - Chapter 2, Design equations, Levenspiel plots, Reactor staging
Read: $\quad$ Chapter 1, P1-9A, Appendix A, from the Web
Chapter 2, Sections 2.1, 2.2, and 2.3
Hand In: Problem Set 1: P1-1 ${ }_{\mathrm{A}}, \mathrm{P} 1-6_{\mathrm{B}}$
In-Class Problem: 1
Study Problems: P1-8A
3) Wednesday, September 16

Topic: $\quad$ Lecture 3 - Chapter 3, Rate laws
Read: $\quad$ Chapter 2, Chapter 3
Hand In: Problem Set 2: Define terms in the Arrhenius Equation, P2-2 A , Intro to Learncheme
In-Class Problem: 2 (Hint: Viewing the University of Alabama YouTube video "The Black Widow" noted in Problem P3-8 $\mathrm{B}_{\mathrm{B}}$ may help you with today's in class problem)

Study Problems: $\quad$ P2-7A
4) Monday, September 21

Topic: $\quad$ Lecture 4 - Chapter 4, Stoichiometry Batch Systems
Read: Chapter 4 Section 4.1
Hand In: Problem Set 3: Define $\theta_{\mathrm{i}}, \theta_{\mathrm{A}}, \theta_{\mathrm{B}}$, and $\delta, \mathrm{P} 2-10_{\mathrm{B}}, \mathrm{P} 3-5_{\mathrm{A}}, \mathrm{P} 3-8_{\mathrm{B}}, \mathrm{P} 3-11_{\mathrm{B}}, \mathrm{P} 3-13_{\mathrm{A}}$
In-Class Problem: 3 - Bring $i>c l i c k e r s ~(t e n t a t i v e) ~-~ T e s t ~ R u n ~ o f ~ S y s t e m ~ i n ~ 2166 ~ D o w ~$
Study Problems: P3-14 $A_{A}$
5) Wednesday, September 23

Topic: Lecture 5 - Chapter 4, Stoichiometry Flow Systems
Read: Chapter 4, Section 4.1
Hand In: Problem Set 4: Define $\varepsilon, \mathrm{F}_{\mathrm{T} 0}, \mathrm{C}_{\mathrm{T} 0}, \mathrm{P} 4-2_{\mathrm{A}}$.
In-Class Problem: 4
Study Problems: $\quad \mathrm{P} 4-1_{\mathrm{A}}$ parts (c) and (d)
6) Monday, September 28

Topic: $\quad$ Lecture 6 - Chapter 5, Isothermal reactor design
Read: Chapter 5, Chapter 5 Summary Notes on the Web site
Hand In: Problem Set 5: P4-1 (a) and (b) only, P4-3,$~ P 4-4$ B,$~ P 4-5_{B}$.
In-Class Problem: 5
Study Problems: P4-10C
7) Wednesday, September 30

| Topic: | Lecture $7-$ Chapter 5, California Registration Exam Problem |
| :--- | :--- |
| Hand In: | Problem Set 6: What are you asked to find P5-18 ${ }^{\text {B }}$ ? What is the Ergun |
|  | Equation? P5-2. |

8) Monday, October 5

Topic:
Read:
Hand In: Problem Set 7: P5-3 $A$, P5-4, P5-5A, P5-8 ${ }_{B}$, P5-13 $3_{B}$ omit parts (j) and (k), P5-16B (a).
In-Class Problem: 7 - Bring Laptops
Study Problems: $\quad \mathrm{P} 5-9_{\mathrm{A}}, \mathrm{P} 5-10_{\mathrm{B}}$ (a).
9) Wednesday, October 7

Topic: $\quad$ Lecture 9 - Chapter 6, Membrane Reactors
Read: Chapter 6
Hand In: Problem Set 8: P5-13 ${ }_{\mathrm{B}}$ part (j) and (k), P5-22 ${ }_{\mathrm{A}}$.
In-Class Problem: 8 - Bring Laptops
Study Problems: P5-21 B
10) Monday, October 12

Topic:
Lecture 10 - Chapter 6, Semibatch Reactors
Read:
Hand In:
In-Class Problem: $\quad 9-$ Bring Laptops to carry out Polymath ODE Solver
Study Problems: $\quad \mathrm{P} 6-7_{B}$
11) Wednesday, October 14

Topic:
Read:
Hand In:
In-Class Problem: 10 - Bring Laptops to carry out Polymath Regression
Study Problems: $\quad$ P7-6B.
12) Monday, October 19

Topic:
No Classes - Fall Study Break
13) Wednesday, October 21

Topic: Lecture 12 - Chapter 8, Multiple Reactions
Read: $\quad$ Chapter 8, Sections 8.1, 8.2, 8.3 and 8.4;
Hand In: Problem Set 11: P7-7,$~ P 7-8_{A}$.
In-Class Problem: 11
Study Problems $\quad$ P7-10 $A$
14) Monday, October 26

Topic: $\quad$ Lecture 13 - EXAM I - Covers Chapters 1 through 7 Closed book, web, notes, in-class problems and home problems.
15) Wednesday, October 28

Topic: $\quad$ Lecture 14 - Chapter 8: Multiple Reactions
Read: $\quad$ Chapter 8, Sections 8.5, 8.6, 8.7 and 8.8
In-Class Problem: 12 - Bring Laptops
Hand In: $\quad$ Problem Set 12: P8-1 $\mathrm{A}_{\mathrm{A}}$ (a) part (1) only, P8-1 $\mathrm{A}_{\mathrm{A}}$ (b), P8-1 $\mathrm{A}_{\mathrm{A}}$ (c) part (1) only, P8-2 ${ }_{\mathrm{B}}, \mathrm{P} 8-6_{\mathrm{B}}, \mathrm{P} 8-7_{\mathrm{C}}$ (a), (b) and (c)
Study Problems $\quad$ P8-10 ${ }_{B}$
16) Monday, November 2

Topic: $\quad$ Lecture 15 - Derivation of Energy Balance
Read: Chapter 11, Sections 11.1, 11.2 and 11.3
Hand In: Problem Set 13: P8-12 . Comprehensive Problem
In-Class Problem: 13 - Bring Laptops
Study Problems: P8-16A
17) Wednesday, November 4

Topic: Lecture 16 - Chapter 11: Adiabatic Equilibrium Conversion and Reactor Staging
Read: Finish Reading Chapter 11, Equilibrium conversion appendix
In-Class Problem: 14
Study Problems P11-6B
18) Monday, November 9

Topic:
Read: Chapter 12 Sections 12.1 through 12.2
Hand In: Problem Set 14: P11-1 ${ }_{A}$ (b), P11-3 $\mathrm{B}_{\mathrm{B}}, \mathrm{P} 11-4_{\mathrm{A}}$.
In-Class Problem: 15
Study Problem: P12-6A
19) Wednesday, November 11

| Topic: | Lecture 18 - Trends in Conversion and Temperature Profiles |
| :--- | :--- |
| Read: | Applications of the Energy Balance to PFRs |
| Chapter 12, Section 12.3 and 12.4 |  |
| Hand In: | Problem Set 15: P12-3 B $_{\text {LEP }}$ |
| In-Class Problem: | $16-$ Bring Laptops |

20) Monday, November 16

Topic: $\quad$ Lecture 19 - Multiple Reactions with Heat Effects This topic is a major goal of this course, to carry out calculations for non isothermal multiple reactions.
Applications of the Energy Balance to PFRs
Hand In: Problem Set 16: P12-4 (a) and (b), P12-14 ${ }_{\mathrm{B}}, \mathrm{P} 12-17_{\mathrm{B}}, \mathrm{P} 12-21_{\mathrm{B}}$.
In-Class Problem: 17 - Bring Laptops
Study Problem: $\quad$ P12-19 ${ }_{\mathrm{B}}$, $\mathrm{i}>$ clicker questions handed out in class
21) Wednesday, November 18

Topic: $\quad$ Lecture 20 - CSTR and Review for Exam II
22) Monday, November 23

Topic: $\quad$ Lecture 21 - EXAM II - Chapters 8, 11 and 12. Book and notecard are the only materials allowed
Hand In: Problem Set 17: P12-26c
23) Wednesday, November 25

Topic: $\quad$ Lecture 22 - Multiple Steady States (MSS) Multiple Reactions with Heat Effects
Read: $\quad$ Sections 12.6 and 12.7
In-Class Problem: 18 - Bring a Ruler/Straight Edge
Study Problems: $\quad$ P13-4B
24) Monday, November 30

Topic: $\quad$ Lecture 23 - Safety (CSI)
Read: Chapter 13
Hand In: Problem Set 18: P13-1 $\quad$ (b) and (f), P13-8 $\mathrm{B}_{\mathrm{B}}$
In-Class Problem: 19 - Bring Laptops
Study Problems: P13-4B
25) Wednesday, December 2

Topic: $\quad$ Lecture 24 -Catalysis Reactor Safety
Read: $\quad$ Chapter 13, Sections 13.1 through 13.3, and 13.5
Hand In: Problem Set 19: P10-2 A part (d), P10-4 ${ }_{\mathrm{B}}$
In-Class Problem: 20
Study Problems: P12-16B
26) Monday, December 7

Topic:
Read:
Hand In:
In-Class Problem:
Study Problems: $\quad$ P10-7, , P10-9
27) Wednesday, December 9

Topic:
Read
Hand In:
In-Class Problem:
Study Problems: $\quad$ P9-12 ${ }_{\mathrm{B}}, \mathrm{P} 9-16_{\mathrm{B}}, \mathrm{P} 9-21_{\mathrm{A}}$

## 28) FINAL EXAM

## P1-1 (a) Example 1-3

(i) $C_{A}$ decreases and $C_{B}$ increases with an increase in $k$, and a decrease in $v_{0}$ for the same volume.
(ii) $C_{A}$ decreases and $C_{B}$ increases with an increase in $k$ and $K_{e}$, and a decrease in $v_{0}$ for the same volume.
(iii) Individualized solution
(iv) Refer to the polymath report below

## POLYMATH Report

Ordinary Differential Equations
Calculated values of DEQ variables
Variable Initial value Minimal value Maximal value Final value

| 1 | Ca | 10. | 2.849321 | 10. |
| :--- | :--- | :--- | :--- | :--- |
| 2 | Cb | 0 | 0 | 7.150679 |
| 3 | k | 0.23 | 0.23 | 0.23 |
| 4 Ke | 3. | 3. | 3. | 0.150679 |
| 5 | ra | -2.3 | -2.3 | -0.1071251 |
| 6 | rb | 2.3 | 0.1071251 | 2.3 |
| 7 | V | 0 | 0 | -0.1071251 |
| 8 | v 0 | 10. | 10. | 100. |

Differential equations
$1 \mathrm{~d}(\mathrm{Ca}) / \mathrm{d}(\mathrm{V})=\mathrm{ra} / \mathrm{v} 0$
$2 \mathrm{~d}(\mathrm{Cb}) / \mathrm{d}(\mathrm{V})=\mathrm{rb} / \mathrm{v} 0$

## Explicit equations

$1 \mathrm{k}=0.23$
$2 \mathrm{Ke}=3$
$3 \mathrm{ra}=-\mathrm{k} *(\mathrm{Ca}-\mathrm{Cb} / \mathrm{Ke})$
$4 \mathrm{rb}=-\mathrm{ra}$
$5 \mathrm{v} 0=10$

## P1-2

Given

| $A=2 * 10^{10} \mathrm{ft}^{2}$ | $T_{\text {STP }}=491.69 \mathrm{R}$ | $H=2000 \mathrm{ft}$ |  |
| :--- | :--- | :--- | :--- |
| $V=4 * 10^{13} \mathrm{ft}^{3}$ | $\mathrm{~T}=534.7^{\circ} \mathrm{R}$ | $\mathrm{P}_{\mathrm{O}}=1 \mathrm{~atm}$ |  |
| $R=0.7302 \frac{\mathrm{~atm} \mathrm{ft}^{3}}{\mathrm{lbmol} R}$ | $\mathrm{Y}_{\mathrm{A}}=0.02$ | $C_{S}=2.04 * 10^{-10} \frac{\mathrm{lbmol}}{\mathrm{ft}^{3}}$ | $\mathrm{C}=4 * 10^{5} \mathrm{cars}$ |

$F_{S}=$ CO in Santa Ana winds $\quad F_{A}=$ CO emission from autos $\quad v_{A}=3000 \frac{f t^{3}}{h r}$ per car at STP

## P1-2 (a)

Total number of lb moles gas in the system:
$N=\frac{P_{0} V}{R T}$
$N=\frac{1 \mathrm{~atm} \times\left(4 \times 10^{13} \mathrm{ft}^{3}\right)}{\left(0.73 \frac{\mathrm{~atm} . \mathrm{ft}^{3}}{\mathrm{lbmol} . R}\right) \times 534.69 \mathrm{R}}=1.025 \times 10^{11} \mathrm{lb} \mathrm{mol}$

## P1-2 (b)

Molar flowrate of CO into L.A. Basin by cars.
$F_{A}=y_{A} F_{T}=\left.y_{A} \cdot v_{A} C_{T}\right|_{\text {STP }} ^{0 \text { no. of cars }}$
$F_{T}=\frac{3000 \mathrm{ft}^{3}}{h_{r c a r}} \times \frac{1 / \mathrm{bmol}}{359 \mathrm{ft}^{3}} \times 400000$ cars $\quad$ (See appendix B)
$\mathrm{F}_{\mathrm{A}}=6.685 \times 10^{4} \mathrm{lb} \mathrm{mol} / \mathrm{hr}$

## P1-2 (c)

Wind speed through corridor is $\mathrm{U}=15 \mathrm{mph}$
$\mathrm{W}=20$ miles
The volumetric flowrate in the corridor is
$v_{0}=$ U.W.H $=(15 \times 5280)(20 \times 5280)(2000) \mathrm{ft}^{3} / \mathrm{hr}=1.673 \times 10^{13} \mathrm{ft}^{3} / \mathrm{hr}$

## P1-2 (d)

Molar flowrate of CO into basin from Sant Ana wind.

$$
\begin{aligned}
F_{S} & :=v_{0} \cdot C_{S} \\
& =1.673 \times 10^{13} \mathrm{ft}^{3} / \mathrm{hr} \times 2.04 \times 10^{-10} \mathrm{lbmol} / \mathrm{ft}^{3} \\
& =3.412 \times 10^{3} \mathrm{lbmol} / \mathrm{hr}
\end{aligned}
$$

## P1-2 (e)

Rate of emission of CO by cars + Rate of CO in Wind - Rate of removal of CO $=\frac{d N_{C O}}{d t}$

$$
F_{A}+F_{S}-v_{o} C_{c o}=V \frac{d C_{c o}}{d t} \quad\left(V=\text { constant }, N_{c o}=C_{c o} V\right)
$$

## P1-2 (f)

$\mathrm{t}=0, C_{c o}=C_{c o O}$
$\int_{0}^{t} d t=V \int_{C_{c o o}}^{C_{c o}} \frac{d C_{c o}}{F_{A}+F_{S}-v_{o} C_{c o}}$
$t=\frac{V}{v_{o}} \ln \left(\frac{F_{A}+F_{S}-v_{o} C_{C O O}}{F_{A}+F_{S}-v_{o} C_{c o}}\right)$

## P1-2 (g)

Time for concentration to reach 8 ppm .
$C_{C O O}=2.04 \times 10^{-8} \frac{\mathrm{lbmol}}{\mathrm{ft}^{3}}, C_{C O}=\frac{2.04}{4} \times 10^{-8} \frac{\mathrm{lbmol}}{\mathrm{ft}^{3}}$
From (f),
$t=\frac{v}{v_{0}} \ln \left(\frac{F_{A}+F_{S}-v_{O} \cdot C_{C O O}}{F_{A}+F_{S}-v_{O} \cdot C_{C O}}\right)$
$=\frac{4 \mathrm{ft}^{3}}{1.673 \times 10^{13} \frac{\mathrm{ft}^{3}}{\mathrm{hr}}} \ln \left(\frac{6.7 \times 10^{4} \frac{\mathrm{lbmol}}{\mathrm{hr}}+3.4 \times 10^{3} \frac{\mathrm{lbmol}}{\mathrm{hr}}-1.673 \times 10^{13} \frac{\mathrm{ft}}{}{ }^{3}}{6 r} \times 2.04 \times 10^{-8} \frac{\mathrm{lbmol}}{\mathrm{ft}^{3}}\right)$
$\mathrm{t}=6.92 \mathrm{hr}$

## P1-2 (h)

(1)

$$
\begin{array}{rlrl}
\mathrm{t}_{\mathrm{o}} & =0 & \mathrm{t}_{\mathrm{f}}=72 \mathrm{hrs} \\
C_{c o} & =2.00 \mathrm{E}-10 \mathrm{lbmol} / \mathrm{ft}^{3} & \mathrm{a}=3.50 \mathrm{E}+04 \mathrm{lbmol} / \mathrm{hr} \\
v_{o} & =1.67 \mathrm{E}+12 \mathrm{ft}^{3} / \mathrm{hr} & \mathrm{~b}=3.00 \mathrm{E}+04 \mathrm{lbmol} / \mathrm{hr} \\
\mathrm{~F}_{\mathrm{s}} & =341.23 \mathrm{lbmol} / \mathrm{hr} & \mathrm{~V}=4.0 \mathrm{E}+13 \mathrm{ft}^{3} \\
a+b \sin \left(\pi \frac{t}{6}\right)+F_{s}-v_{o} C_{c o}=V \frac{d C_{c o}}{d t}
\end{array}
$$

Now solving this equation using POLYMATH we get plot between $\mathrm{C}_{\mathrm{co}}$ vs. t

See Polymath program P1-4-h-1.pol.
POLYMATH Results
Calculated values of the DEQ variables

| Variable | initial value | minimal value | maximal value | final value |
| :--- | :--- | :--- | :--- | :--- |
| T | 0 | 0 | 72 | 72 |
| C | $2.0 \mathrm{E}-10$ | $2.0 \mathrm{E}-10$ | $2.134 \mathrm{E}-08$ | $1.877 \mathrm{E}-08$ |
| v0 | $1.67 \mathrm{E}+12$ | $1.67 \mathrm{E}+12$ | $1.67 \mathrm{E}+12$ | $1.67 \mathrm{E}+12$ |
| A | $3.5 \mathrm{E}+04$ | $3.5 \mathrm{E}+04$ | $3.5 \mathrm{E}+04$ | $3.5 \mathrm{E}+04$ |
| B | $3.0 \mathrm{E}+04$ | $3.0 \mathrm{E}+04$ | $3.0 \mathrm{E}+04$ | $3.0 \mathrm{E}+04$ |
| F | 341.23 | 341.23 | 341.23 | 341.23 |
| V | $4.0 \mathrm{E}+13$ | $4.0 \mathrm{E}+13$ | $4.0 \mathrm{E}+13$ | $4.0 \mathrm{E}+13$ |

ODE Report (RKF45)
Differential equations as entered by the user
$[1] d(C) / d(t)=\left(a+b^{*} \sin \left(3.14^{*} t / 6\right)+F-v 0^{*} C\right) / V$
Explicit equations as entered by the user
[1] $\mathrm{vO}=1.67^{*} 10^{\wedge} 12$
[2] a $=35000$
[3] $b=30000$
[4] F $=341.23$
[5] $\mathrm{V}=4^{*} 10^{\wedge} 13$

P1-2 (h) Continued

(2) $\mathrm{t}_{\mathrm{f}}=48 \mathrm{hrs} \quad F_{s}=0 \quad a+b \sin \left(\pi \frac{t}{6}\right)-v_{o} C_{c o}=V \frac{d C_{c o}}{d t}$

Now solving this equation using POLYMATH we get plot between $\mathrm{C}_{\mathrm{co}}$ vs t
See Polymath program P1-4-h-2.pol.
POLYMATH Results
Calculated values of the DEQ variables

| Variable | initial value | minimal value | maximal value | final value |
| :--- | :--- | :--- | :--- | :--- |
| T | 0 | 0 | 72 | 72 |
| C | $2.0 \mathrm{E}-10$ | $2.0 \mathrm{E}-10$ | $2.134 \mathrm{E}-08$ | $1.877 \mathrm{E}-08$ |
| v0 | $1.67 \mathrm{E}+12$ | $1.67 \mathrm{E}+12$ | $1.67 \mathrm{E}+12$ | $1.67 \mathrm{E}+12$ |
| A | $3.5 \mathrm{E}+04$ | $3.5 \mathrm{E}+04$ | $3.5 \mathrm{E}+04$ | $3.5 \mathrm{E}+04$ |
| B | $3.0 \mathrm{E}+04$ | $3.0 \mathrm{E}+04$ | $3.0 \mathrm{E}+04$ | $3.0 \mathrm{E}+04$ |
| F | 341.23 | 341.23 | 341.23 | 341.23 |
| V | $4.0 \mathrm{E}+13$ | $4.0 \mathrm{E}+13$ | $4.0 \mathrm{E}+13$ | $4.0 \mathrm{E}+13$ |

ODE Report (RKF45)
Differential equations as entered by the user
$[1] d(C) / d(t)=\left(a+b * \sin \left(3.14^{*} t / 6\right)-v 0^{*} C\right) / V$
Explicit equations as entered by the user
[1] $v 0=1.67 * 10^{\wedge} 12$
[2] $a=35000$
[3] b = 30000
[4] $V=4^{*} 10^{\wedge} 13$


P1-2 (h) Continued
(3)

Changing $a \Rightarrow$ Increasing ' $a$ ' reduces the amplitude of ripples in graph. It reduces the effect of the sine function by adding to the baseline.

Changing $b \rightarrow$ The amplitude of ripples is directly proportional to ' $b$ '. As $b$ decreases amplitude decreases and graph becomes smooth.

Changing $v_{0} \rightarrow$ As the value of $v_{0}$ is increased the graph changes to a "shifted sin-curve". And as $v_{0}$ is decreased graph changes to a smooth increasing curve.

## P1-3 (a)

Initial number of rabbits, $x(0)=500$
Initial number of foxes, $y(0)=200$
Number of days $=500$
$\frac{d x}{d t}=k_{1} x-k_{2} x y$
$\frac{d y}{d t}=k_{3} x y-k_{4} y$
Given,
$k_{1}=0.02 d a y^{-1}$
$k_{2}=0.00004 /($ day $\times$ foxes $)$
$k_{3}=0.0004 /($ day $\times$ rabbits $)$
$k_{4}=0.04 d a y^{-1}$
See Polymath program P1-3-a.pol.

POLYMATH Results
Calculated values of the DEQ variables

| Variable | initial value | minimal value | maximal value | final value |
| :--- | :--- | :--- | :--- | :--- |
| T | 0 | 0 | 500 | 500 |
| X | 500 | 2.9626929 | 519.40024 | 4.2199691 |
| Y | 200 | 1.1285722 | 4099.517 | 117.62928 |
| k1 | 0.02 | 0.02 | 0.02 | 0.02 |
| k2 | $4.0 \mathrm{E}-05$ | $4.0 \mathrm{E}-05$ | $4.0 \mathrm{E}-05$ | $4.0 \mathrm{E}-05$ |
| k3 | $4.0 \mathrm{E}-04$ | $4.0 \mathrm{E}-04$ | $4.0 \mathrm{E}-04$ | $4.0 \mathrm{E}-04$ |
| k 4 | 0.04 | 0.04 | 0.04 | 0.04 |

## ODE Report (RKF45)

Differential equations as entered by the user
[1] $d(x) / d(t)=\left(k 1^{*} x\right)-\left(k 2^{*} x^{*} y\right)$
[2] $d(y) / d(t)=\left(k 3^{*} x^{*} y\right)-\left(k 4^{*} y\right)$

Explicit equations as entered by the user
[1] k1 $=0.02$
[2] k2 $=0.00004$
[3] k3 $=0.0004$
[4] k4 $=0.04$

P1-3 (a) Continued


When, $\mathrm{t}_{\text {final }}=800$ and $k_{3}=0.00004 /($ day $\times$ rabbits $)$


Plotting rabbits vs. foxes


## P1-3 (b)

POLYMATH 6.10 Educational Release


## P1-3 (c)

We would have to change k 2 and k 4 for the plot to become a circle from an oval.

## P1-3 (d)



## P1-3 (d) Continued



- Foxes

P1-4
Individualized solution

## P1-5

The correct answer is b.)
a.) Has the wrong sign for $-\int^{V} r_{A} d V$ and $-2 \int^{V} r_{A} d V$. Should be $+\int^{V} r_{A} d V$ and

$$
+2 \int^{V} r_{A} d V
$$

b.) All are correct
c.) Wrong sign for $F_{c}$, should be $-F_{c}$.
d.) Wrong sign for $-\int^{V} r_{C} d V$, should be $+\int^{V} r_{C} d V$

## P1-6 (a)

$-r_{A}=k$ with $k=0.05 \mathrm{~mol} / \mathrm{h} \mathrm{dm}^{3}$
CSTR: The general equation is

$$
V=\frac{F_{A 0}-F_{A}}{-r_{A}}
$$

Here $\mathrm{C}_{\mathrm{A}}=0.01 \mathrm{C}_{\mathrm{A} 0}, \mathrm{~V}_{0}=10 \mathrm{dm}^{3} / \mathrm{min}, \mathrm{F}_{\mathrm{A}}=5.0 \mathrm{~mol} / \mathrm{hr}$
Also we know that $F_{A}=C_{A} v_{0}$ and $F_{A 0}=C_{A 0} v_{0}, C_{A 0}=F_{A 0} / v_{0}=0.5 \mathrm{~mol} / \mathrm{dm}^{3}$
Substituting the values in the above equation we get,
$V=\frac{C_{A 0} v_{0}-C_{A} v_{0}}{k}=\frac{(0.5) 10-0.01(0.5) 10}{0.05}$

$$
\rightarrow \mathrm{V}=99 \mathrm{dm}^{3}
$$

PFR: The general equation is

$$
\frac{d F_{A}}{d V}=r_{A}=k, \text { Now } F_{A}=C_{A} V_{0} \text { and } F_{A 0}=C_{A 0} V_{0}=>\frac{d C_{A} V_{0}}{d V}=-k
$$

Integrating the above equation we get

P1-6 (a) Continued

$$
\frac{v_{0}}{k} \int_{C_{A 0}}^{C_{A}} d C_{A}=\int_{0}^{V} d V \Rightarrow V=\frac{v_{0}}{k}\left(C_{A 0}-C_{A}\right)
$$

Hence V = $99 \mathrm{dm}^{\mathbf{3}}$
Volume of PFR is same as the volume for a CSTR since the rate is constant and independent of concentration.

## P1-6 (b)

$-r_{A}=k C_{A}$ with $k=0.0001 \mathrm{~s}^{-1}$
CSTR:
We have already derived that

$$
\begin{aligned}
& V=\frac{C_{A 0} v_{0}-C_{A} v_{0}}{-r_{A}}=\frac{v_{0} C_{A 0}(1-0.01)}{k C_{A}} \\
& \mathrm{k}=0.0001 \mathrm{~s}^{-1}=0.0001 \times 3600 \mathrm{hr}^{-1}=0.36 \mathrm{hr}^{-1} \\
& \rightarrow V=\frac{\left(10 \mathrm{dm}^{3} / \mathrm{hr}\right)\left(0.5 \mathrm{~mol} / \mathrm{dm}^{3}\right)(0.99)}{\left(0.36 \mathrm{hr}^{-1}\right)\left(0.01 * 0.5 \mathrm{~mol} / \mathrm{dm}^{3}\right)} \Rightarrow \mathrm{V}=\mathbf{2 7 5 0 \mathrm { dm } ^ { 3 }}
\end{aligned}
$$

PFR:
From above we already know that for a PFR

$$
\frac{d C_{A} v_{0}}{d V}=r_{A}=-k C_{A}
$$

Integrating

$$
\begin{aligned}
& \frac{v_{0}}{k} \int_{C_{A 0}}^{C_{A}} \frac{d C_{A}}{C_{A}}=-\int_{0}^{V} d V \\
& \frac{v_{0}}{k} \ln \frac{C_{A 0}}{C_{A}}=V
\end{aligned}
$$

Again $\mathrm{k}=0.0001 \mathrm{~s}^{-1}=0.0001 \times 3600 \mathrm{hr}^{-1}=0.36 \mathrm{hr}^{-1}$
Substituting the values in above equation we get $\mathbf{V}=\mathbf{1 2 7 . 9} \mathbf{d m}^{\mathbf{3}}$

P1-6 (c)
$-r_{A}=k C_{A}^{2}$ with $k=300 \mathrm{dm}^{3} / \mathrm{mol} . \mathrm{hr}$
CSTR:

$$
V=\frac{C_{A 0} v_{0}-C_{A} v_{0}}{-r_{A}}=\frac{v_{0} C_{A 0}(1-0.01)}{k C_{A}^{2}}
$$

Substituting all the values we get

$$
\left.V=\frac{(10 \mathrm{dm}}{}{ }^{3} / \mathrm{hr}\right)\left(0.5 \mathrm{~mol} / \mathrm{dm}^{3}\right)(0.99) \mid(\mathrm{mol} . h r)\left(0.01^{*} 0.5 \mathrm{~mol} / \mathrm{dm}^{3}\right)^{2} \quad=>\mathbf{V}=660 \mathrm{dm}^{3}
$$

PFR:

$$
\frac{d C_{A} v_{0}}{d V}=r_{A}=-k C_{A}^{2}
$$

P1-6 (c) Continued
Integrating

$$
\begin{aligned}
& \frac{v_{0}}{k} \int_{C_{A 0}}^{C_{A}} \frac{d C_{A}}{C_{A}^{2}}=-\int_{0}^{V} d V \Rightarrow \frac{v_{0}}{k}\left(\frac{1}{C_{A}}-\frac{1}{C_{A 0}}\right)=V \\
& \Rightarrow V=\frac{10 d m^{3} / \mathrm{hr}}{300 \mathrm{dm}^{3} / \mathrm{mol} . h r}\left(\frac{1}{0.01 C_{A 0}}-\frac{1}{C_{A 0}}\right)=6.6 \mathrm{dm}^{3}
\end{aligned}
$$

P1-6 (d)
$\mathrm{C}_{\mathrm{A}}=0.001 \mathrm{C}_{\mathrm{AO}}$
$t=\int_{N_{A}}^{N_{A O}} \frac{d N}{-r_{A} V}$
Constant Volume $\mathrm{V}=\mathrm{V}_{0}$
$t=\int_{C_{A}}^{C_{A O}} \frac{d C_{A}}{-r_{A}}$
Zero order:
$t=\frac{1}{k}\left[C_{A 0}-0.001 C_{A 0}\right]=\frac{.999 C_{A O}}{0.05}=9.99 h$
First order:
$t=\frac{1}{k} \ln \left(\frac{C_{A 0}}{C_{A}}\right)=\frac{1}{0.0001} \ln \left(\frac{1}{.001}\right)=69078 s=19.19 h$
Second order:
$t=\frac{1}{k}\left[\frac{1}{C_{A}}-\frac{1}{C_{A 0}}\right]=\frac{1}{300}\left[\frac{1}{0.5 \cdot 0.001}-\frac{1}{0.5}\right]=6.66 h$

P1-7 Enrico Fermi Problem
P1-7(a) Population of Chicago $=4,000,000$
Size of Households $=4$
Number of Households $=1,000,000$
Fraction of Households that own a piano $=1 / 5$
Number of Pianos $=200,000$
Number of Tunes/year per Piano = 1
Number of Tunes Needed Per Year $=200,000$
Tunes per day $=2$
Tunes per year per tuner $=\frac{250 \text { days }}{y r} \times \frac{2}{d a y}=500 / \mathrm{yr} / \mathrm{tuner}$
$\frac{200,000 \text { tunes }}{y r} \times \frac{1}{500 \text { tunes } / y r / \text { tuner }}=400$ Tuners

