Chapter 2

Functions and Their Graphs

Section 2.1

1. $(-1,3)$

2. $3(-2)^2 - 5(-2) + \dfrac{1}{(-2)} = 3(4) - 5(-2) - \dfrac{1}{2}$

$= 12 + 10 - \dfrac{1}{2}$

$= \dfrac{43}{2}$ or $21\frac{1}{2}$ or 21.5

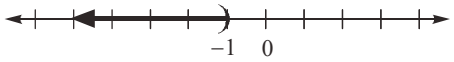
3. We must not allow the denominator to be 0.
$x + 4 \neq 0 \Rightarrow x \neq -4$; Domain: $\{x \mid x \neq -4\}$.

4. $3 - 2x > 5$

$-2x > 2$

$x < -1$

Solution set: $\{x \mid x < -1\}$ or $(-\infty, -1)$



5. $\sqrt{5} + 2$

6. radicals

7. independent; dependent

8. **a**

9. **c**

10. False; $g \neq 0$

11. False; every function is a relation, but not every relation is a function. For example, the relation $x^2 + y^2 = 1$ is not a function.

12. verbally, numerically, graphically, algebraically

13. False; if the domain is not specified, we assume it is the largest set of real numbers for which the value of *f* is a real number.

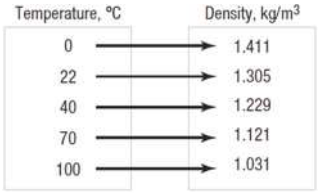
14. False; if x is in the domain of a function *f*, we say that *f* is defined at *x*, or *f(x)* exists.

15. difference quotient

16. explicitly

17. a. Domain: {0,22,40,70,100}
Range: {1.031, 1.121, 1.229, 1.305, 1.411}

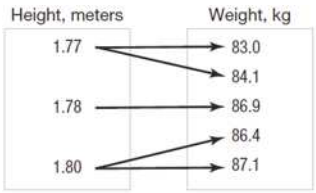
b.



c. {(0, 1.411), (22, 1.305), (40, 1.229), (70, 1.121), (100, 1.031)}

18. a. Domain: {1.80, 1.78, 1.77}
Range: {87.1, 86.9, 92.0, 84.1, 86.4}

b.



c. {(1.80, 87.1), (1.78, 86.9), (1.77, 83.0), (1.77, 84.1), (1.80, 86.4)}

19. Domain: {Elvis, Colleen, Kaleigh, Marissa}
Range: {Jan. 8, Mar. 15, Sept. 17}
Function

20. Domain: {Bob, John, Chuck}
Range: {Beth, Diane, Linda, Marcia}
Not a function

21. Domain: {20, 30, 40}
Range: {200, 300, 350, 425}
Not a function

22. Domain: {Less than 9th grade, 9th-12th grade, High School Graduate, Some College, College Graduate}
Range: {$18,120, $23,251, $36,055, $45,810, $67,165}
Function

23. Domain: {-3, 2, 4}
Range: {6, 9, 10}
Not a function

24. Domain: {–2, –1, 3, 4}
Range: {3, 5, 7, 12}
Function

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25. Domain: {1, 2, 3, 4}
Range: {3}
Function

26. Domain: {0, 1, 2, 3}
Range: {–2, 3, 7}
Function

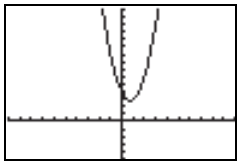
27. Domain: {-4, 0, 3}
Range: {1, 3, 5, 6}
Not a function

28. Domain: {-4, -3, -2, -1}
Range: {0, 1, 2, 3, 4}
Not a function

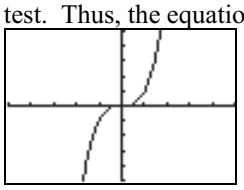
29. Domain: {–1, 0, 2, 4}
Range: {-1, 3, 8}
Function

30. Domain: {–2, –1, 0, 1}
Range: {3, 4, 16}
Function

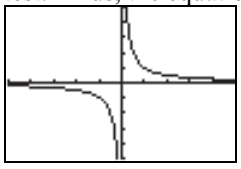
31. Graph $y = 2x^2 - 3x + 4$. The graph passes the vertical line test. Thus, the equation represents a function.



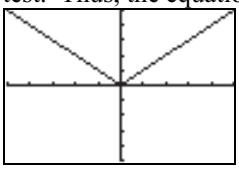
32. Graph $y = x^3$. The graph passes the vertical line test. Thus, the equation represents a function.



33. Graph $y = \frac{1}{x}$. The graph passes the vertical line test. Thus, the equation represents a function.



34. Graph $y = |x|$. The graph passes the vertical line test. Thus, the equation represents a function.



35. $x^2 = 8 - y^2$

Solve for y: $y = \pm\sqrt{8 - x^2}$

For $x = 0$, $y = \pm 2\sqrt{2}$. Thus, $\left(0, -2\sqrt{2}\right)$ and $\left(0, 2\sqrt{2}\right)$ are on the graph. This is not a function, since a distinct x-value corresponds to two different y-values.

36. $y = \pm\sqrt{1 - 2x}$

For $x = 0$, $y = \pm 1$. Thus, (0, 1) and (0, –1) are on the graph. This is not a function, since a distinct x-value corresponds to two different y-values.

37. $x = y^2$

Solve for y: $y = \pm\sqrt{x}$

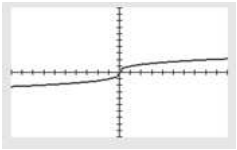
For $x = 1$, $y = \pm 1$. Thus, (1, 1) and (1, –1) are on the graph. This is not a function, since a distinct x-value corresponds to two different y-values.

38. $x + y^2 = 1$

Solve for y: $y = \pm\sqrt{1 - x}$

For $x = 0$, $y = \pm 1$. Thus, (0, 1) and (0, –1) are on the graph. This is not a function, since a distinct x-value corresponds to two different y-values.

39. Graph $y = \sqrt[3]{x}$. The graph passes the vertical line test. Thus, the equation represents a function.



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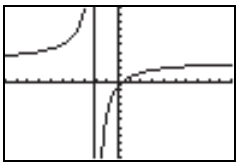
40. Graph $y = \dfrac{3x-1}{x+2}$. The graph passes the vertical line test. Thus, the equation represents a function.



41. $|y| = 2x+3$

Solve for y: $y = 2x+3$ or $y = -(2x+3)$

For $x = 1$, $y = 5$ or $y = -5$. Thus, $(1,5)$ and $(1,-5)$ are on the graph. This is not a function, since a distinct x-value corresponds to two different y-values.

42. $x^2 - 4y^2 = 1$

Solve for y: $x^2 - 4y^2 = 1$

$$4y^2 = x^2 - 1$$

$$y^2 = \frac{x^2-1}{4}$$

$$y = \frac{\pm\sqrt{x^2-1}}{2}$$

For $x = \sqrt{2}$, $y = \pm\dfrac{1}{2}$. Thus, $\left(\sqrt{2}, \dfrac{1}{2}\right)$ and $\left(\sqrt{2}, -\dfrac{1}{2}\right)$ are on the graph. This is not a function, since a distinct x-value corresponds to two different y-values.

43. $f(x) = 3x^2 + 2x - 4$

a. $f(0) = 3(0)^2 + 2(0) - 4 = -4$

b. $f(1) = 3(1)^2 + 2(1) - 4 = 3 + 2 - 4 = 1$

c. $f(-1) = 3(-1)^2 + 2(-1) - 4 = 3 - 2 - 4 = -3$

d. $f(-x) = 3(-x)^2 + 2(-x) - 4 = 3x^2 - 2x - 4$

e. $-f(x) = -\left(3x^2 + 2x - 4\right) = -3x^2 - 2x + 4$

f. $f(x+1) = 3(x+1)^2 + 2(x+1) - 4$

$$= 3\left(x^2 + 2x + 1\right) + 2x + 2 - 4$$

$$= 3x^2 + 6x + 3 + 2x + 2 - 4$$

$$= 3x^2 + 8x + 1$$

g. $f(2x) = 3(2x)^2 + 2(2x) - 4 = 12x^2 + 4x - 4$

h. $f(x+h) = 3(x+h)^2 + 2(x+h) - 4$

$$= 3\left(x^2 + 2xh + h^2\right) + 2x + 2h - 4$$

$$= 3x^2 + 6xh + 3h^2 + 2x + 2h - 4$$

44. $f(x) = -2x^2 + x - 1$

a. $f(0) = -2(0)^2 + 0 - 1 = -1$

b. $f(1) = -2(1)^2 + 1 - 1 = -2$

c. $f(-1) = -2(-1)^2 + (-1) - 1 = -4$

d. $f(-x) = -2(-x)^2 + (-x) - 1 = -2x^2 - x - 1$

e. $-f(x) = -\left(-2x^2 + x - 1\right) = 2x^2 - x + 1$

f. $f(x+1) = -2(x+1)^2 + (x+1) - 1$

$$= -2\left(x^2 + 2x + 1\right) + x + 1 - 1$$

$$= -2x^2 - 4x - 2 + x$$

$$= -2x^2 - 3x - 2$$

g. $f(2x) = -2(2x)^2 + (2x) - 1 = -8x^2 + 2x - 1$

h. $f(x+h) = -2(x+h)^2 + (x+h) - 1$

$$= -2\left(x^2 + 2xh + h^2\right) + x + h - 1$$

$$= -2x^2 - 4xh - 2h^2 + x + h - 1$$

45. $f(x) = \dfrac{x}{x^2+1}$

a. $f(0) = \dfrac{0}{0^2+1} = \dfrac{0}{1} = 0$

b. $f(1) = \dfrac{1}{1^2+1} = \dfrac{1}{2}$

c. $f(-1) = \dfrac{-1}{(-1)^2+1} = \dfrac{-1}{1+1} = -\dfrac{1}{2}$

d. $f(-x) = \dfrac{-x}{(-x)^2+1} = \dfrac{-x}{x^2+1}$

e. $-f(x) = -\left(\dfrac{x}{x^2+1}\right) = \dfrac{-x}{x^2+1}$

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f. $f(x+1)=\dfrac{x+1}{(x+1)^2+1}$

$=\dfrac{x+1}{x^2+2x+1+1}$

$=\dfrac{x+1}{x^2+2x+2}$

g. $f(2x)=\dfrac{2x}{(2x)^2+1}=\dfrac{2x}{4x^2+1}$

h. $f(x+h)=\dfrac{x+h}{(x+h)^2+1}=\dfrac{x+h}{x^2+2xh+h^2+1}$

46. $f(x)=\dfrac{x^2-1}{x+4}$

a. $f(0)=\dfrac{0^2-1}{0+4}=\dfrac{-1}{4}=-\dfrac{1}{4}$

b. $f(1)=\dfrac{1^2-1}{1+4}=\dfrac{0}{5}=0$

c. $f(-1)=\dfrac{(-1)^2-1}{-1+4}=\dfrac{0}{3}=0$

d. $f(-x)=\dfrac{(-x)^2-1}{-x+4}=\dfrac{x^2-1}{-x+4}$

e. $-f(x)=-\left(\dfrac{x^2-1}{x+4}\right)=\dfrac{-x^2+1}{x+4}$

f. $f(x+1)=\dfrac{(x+1)^2-1}{(x+1)+4}$

$=\dfrac{x^2+2x+1-1}{x+5}=\dfrac{x^2+2x}{x+5}$

g. $f(2x)=\dfrac{(2x)^2-1}{2x+4}=\dfrac{4x^2-1}{2x+4}$

h. $f(x+h)=\dfrac{(x+h)^2-1}{(x+h)+4}=\dfrac{x^2+2xh+h^2-1}{x+h+4}$

47. $f(x)=|x|+4$

a. $f(0)=|0|+4=0+4=4$

b. $f(1)=|1|+4=1+4=5$

c. $f(-1)=|-1|+4=1+4=5$

d. $f(-x)=|-x|+4=|x|+4$

e. $-f(x)=-(|x|+4)=-|x|-4$

f. $f(x+1)=|x+1|+4$

g. $f(2x)=|2x|+4=2|x|+4$

h. $f(x+h)=|x+h|+4$

48. $f(x)=\sqrt{x^2+x}$

a. $f(0)=\sqrt{0^2+0}=\sqrt{0}=0$

b. $f(1)=\sqrt{1^2+1}=\sqrt{2}$

c. $f(-1)=\sqrt{(-1)^2+(-1)}=\sqrt{1-1}=\sqrt{0}=0$

d. $f(-x)=\sqrt{(-x)^2+(-x)}=\sqrt{x^2-x}$

e. $-f(x)=-\left(\sqrt{x^2+x}\right)=-\sqrt{x^2+x}$

f. $f(x+1)=\sqrt{(x+1)^2+(x+1)}$

$=\sqrt{x^2+2x+1+x+1}$

$=\sqrt{x^2+3x+2}$

g. $f(2x)=\sqrt{(2x)^2+2x}=\sqrt{4x^2+2x}$

h. $f(x+h)=\sqrt{(x+h)^2+(x+h)}$

$=\sqrt{x^2+2xh+h^2+x+h}$

49. $f(x)=\dfrac{2x+1}{3x-5}$

a. $f(0)=\dfrac{2(0)+1}{3(0)-5}=\dfrac{0+1}{0-5}=-\dfrac{1}{5}$

b. $f(1)=\dfrac{2(1)+1}{3(1)-5}=\dfrac{2+1}{3-5}=\dfrac{3}{-2}=-\dfrac{3}{2}$

c. $f(-1)=\dfrac{2(-1)+1}{3(-1)-5}=\dfrac{-2+1}{-3-5}=\dfrac{-1}{-8}=\dfrac{1}{8}$

d. $f(-x)=\dfrac{2(-x)+1}{3(-x)-5}=\dfrac{-2x+1}{-3x-5}=\dfrac{2x-1}{3x+5}$

e. $-f(x)=-\left(\dfrac{2x+1}{3x-5}\right)=\dfrac{-2x-1}{3x-5}$

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f. $f(x+1)=\dfrac{2(x+1)+1}{3(x+1)-5}=\dfrac{2x+2+1}{3x+3-5}=\dfrac{2x+3}{3x-2}$

g. $f(2x)=\dfrac{2(2x)+1}{3(2x)-5}=\dfrac{4x+1}{6x-5}$

h. $f(x+h)=\dfrac{2(x+h)+1}{3(x+h)-5}=\dfrac{2x+2h+1}{3x+3h-5}$

50. $f(x)=1-\dfrac{1}{(x+2)^2}$

a. $f(0)=1-\dfrac{1}{(0+2)^2}=1-\dfrac{1}{4}=\dfrac{3}{4}$

b. $f(1)=1-\dfrac{1}{(1+2)^2}=1-\dfrac{1}{9}=\dfrac{8}{9}$

c. $f(-1)=1-\dfrac{1}{(-1+2)^2}=1-\dfrac{1}{1}=0$

d. $f(-x)=1-\dfrac{1}{(-x+2)^2}$

e. $-f(x)=-\left(1-\dfrac{1}{(x+2)^2}\right)=\dfrac{1}{(x+2)^2}-1$

f. $f(x+1)=1-\dfrac{1}{(x+1+2)^2}=1-\dfrac{1}{(x+3)^2}$

g. $f(2x)=1-\dfrac{1}{(2x+2)^2}=1-\dfrac{1}{4(x+1)^2}$

h. $f(x+h)=1-\dfrac{1}{(x+h+2)^2}$

51. $f(x)=-5x+4$

Domain: $\{x \mid x \text{ is any real number}\}$

52. $f(x)=x^2+2$

Domain: $\{x \mid x \text{ is any real number}\}$

53. $f(x)=\dfrac{x+1}{2x^2+8}$

Domain: $\{x \mid x \text{ is any real number}\}$

54. $f(x)=\dfrac{x^2}{x^2+1}$

Domain: $\{x \mid x \text{ is any real number}\}$

55. $g(x)=\dfrac{x}{x^2-16}$

$x^2-16\neq 0$

$x^2\neq 16 \Rightarrow x\neq \pm 4$

Domain: $\{x \mid x\neq -4, x\neq 4\}$

56. $h(x)=\dfrac{2x}{x^2-4}$

$x^2-4\neq 0$

$x^2\neq 4 \Rightarrow x\neq \pm 2$

Domain: $\{x \mid x\neq -2, x\neq 2\}$

57. $F(x)=\dfrac{x-2}{x^3+x}$

$x^3+x\neq 0$

$x(x^2+1)\neq 0$

$x\neq 0, \quad x^2\neq -1$

Domain: $\{x \mid x\neq 0\}$

58. $G(x)=\dfrac{x+4}{x^3-4x}$

$x^3-4x\neq 0$

$x(x^2-4)\neq 0$

$x\neq 0, \quad x^2\neq 4$

$x\neq 0, \quad x\neq \pm 2$

Domain: $\{x \mid x\neq -2, x\neq 0, x\neq 2\}$

59. $h(x)=\sqrt{3x-12}$

$3x-12\geq 0$

$3x\geq 12$

$x\geq 4$

Domain: $\{x \mid x\geq 4\}$

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60. $G(x)=\sqrt{1-x}$

$1-x\ge 0$

$-x\ge -1$

$x\le 1$

Domain: $\{x\,|\,x\le 1\}$

61. $p(x)=\dfrac{x}{|2x+3|-1}$

$|2x+3|-1=0$

$|2x+3|=1$

$2x+3=-1$ or $2x+3=1$

$2x=-4 \qquad 2x=-2$

$x=-2 \qquad x=-1$

Domain: $\{x\,|\,x\ne -2, x\ne -1\}$

62. $p(x)=\dfrac{x-1}{|3x-1|-4}$

$|3x-1|-4=0$

$|3x-1|=4$

$3x-1=-4$ or $3x-1=4$

$3x=-3 \qquad 3x=5$

$x=-1 \qquad x=\dfrac{5}{3}$

Domain: $\left\{x\,\middle|\,x\ne -1, x\ne \dfrac{5}{3}\right\}$

63. $f(x)=\dfrac{x}{\sqrt{x-4}}$

$x-4>0$

$x>4$

Domain: $\{x\,|\,x>4\}$

64. $q(x)=\frac{-x}{\sqrt{-x-2}}$

$-x-2>0$

$-x>2$

$x<-2$

Domain: $\{x\,|\,x<-2\}$

65. $P(t)=\dfrac{\sqrt{t-4}}{3t-21}$

$t-4\ge 0$

$t\ge 4$

Also $3t-21\ne 0$

$3t-21\ne 0$

$3t\ne 21$

$t\ne 7$

Domain: $\{t\,|\,t\ge 4, t\ne 7\}$

66. $h(z)=\dfrac{\sqrt{z+3}}{z-2}$

$z+3\ge 0$

$z\ge -3$

Also $z-2\ne 0$

$z\ne 2$

Domain: $\{z\,|\,z\ge -3, z\ne 2\}$

67. $f(x)=\sqrt[3]{5x-4}$

Domain: $\{x\,|\,x \text{ is any real number}\}$.

68. $g(t)=-t^2+\sqrt[3]{t^2+7t}$

Domain: $\{t\,|\,t \text{ is any real number}\}$.

69. $M(t)=\sqrt[5]{\dfrac{t+1}{t^2-5t-14}}$

$t^2-5t-14=0$

$(t+2)(t-7)=0$

$t+2=0$ or $t-7=0$

$t=-2 \qquad t=7$

Domain: $\{t\,|\,t\ne -2, x\ne 7\}$

70. $N(p)=\sqrt[5]{\dfrac{p}{2p^2-98}}$

$2p^2-98=0$

$2(p^2-49)=0$

$2(p+7)(p-7)=0$

$p+7=0$ or $p-7=0$

$p=-7 \qquad p=7$

Domain: $\{p\,|\,p\ne -7, x\ne 7\}$

71. $f(x)=3x+4 \qquad g(x)=2x-3$

a. $(f+g)(x)=3x+4+2x-3=5x+1$

Domain: $\{x\,|\,x \text{ is any real number}\}$.

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b. $(f-g)(x) = (3x+4)-(2x-3)$
$= 3x+4-2x+3$
$= x+7$
Domain: $\{x \mid x \text{ is any real number}\}$.

c. $(f \cdot g)(x) = (3x+4)(2x-3)$
$= 6x^2 - 9x + 8x - 12$
$= 6x^2 - x - 12$
Domain: $\{x \mid x \text{ is any real number}\}$.

d. $\left(\frac{f}{g}\right)(x) = \frac{3x+4}{2x-3}$

$2x-3 \neq 0 \Rightarrow 2x \neq 3 \Rightarrow x \neq \frac{3}{2}$

Domain: $\left\{x \middle| x \neq \frac{3}{2}\right\}$.

e. $(f+g)(3) = 5(3)+1 = 15+1 = 16$

f. $(f-g)(4) = 4+7 = 11$

g. $(f \cdot g)(2) = 6(2)^2 - 2 - 12 = 24 - 2 - 12 = 10$

h. $\left(\frac{f}{g}\right)(1) = \frac{3(1)+4}{2(1)-3} = \frac{3+4}{2-3} = \frac{7}{-1} = -7$

72. $f(x) = 2x+1 \qquad g(x) = 3x-2$

a. $(f+g)(x) = 2x+1+3x-2 = 5x-1$
Domain: $\{x \mid x \text{ is any real number}\}$.

b. $(f-g)(x) = (2x+1)-(3x-2)$
$= 2x+1-3x+2$
$= -x+3$
Domain: $\{x \mid x \text{ is any real number}\}$.

c. $(f \cdot g)(x) = (2x+1)(3x-2)$
$= 6x^2 - 4x + 3x - 2$
$= 6x^2 - x - 2$
Domain: $\{x \mid x \text{ is any real number}\}$.

d. $\left(\frac{f}{g}\right)(x) = \frac{2x+1}{3x-2}$
$3x-2 \neq 0$

$3x \neq 2 \Rightarrow x \neq \frac{2}{3}$

Domain: $\left\{x \middle| x \neq \frac{2}{3}\right\}$.

e. $(f+g)(3) = 5(3)-1 = 15-1 = 14$

f. $(f-g)(4) = -4+3 = -1$

g. $(f \cdot g)(2) = 6(2)^2 - 2 - 2$
$= 6(4) - 2 - 2$
$= 24 - 2 - 2 = 20$

h. $\left(\frac{f}{g}\right)(1) = \frac{2(1)+1}{3(1)-2} = \frac{2+1}{3-2} = \frac{3}{1} = 3$

73. $f(x) = x-1 \qquad g(x) = 2x^2$

a. $(f+g)(x) = x-1+2x^2 = 2x^2+x-1$
Domain: $\{x \mid x \text{ is any real number}\}$.

b. $(f-g)(x) = (x-1)-(2x^2)$
$= x-1-2x^2$
$= -2x^2+x-1$
Domain: $\{x \mid x \text{ is any real number}\}$.

c. $(f \cdot g)(x) = (x-1)(2x^2) = 2x^3 - 2x^2$
Domain: $\{x \mid x \text{ is any real number}\}$.

d. $\left(\frac{f}{g}\right)(x) = \frac{x-1}{2x^2}$
Domain: $\{x \mid x \neq 0\}$.

e. $(f+g)(3) = 2(3)^2 + 3 - 1$
$= 2(9) + 3 - 1$
$= 18 + 3 - 1 = 20$

f. $(f-g)(4) = -2(4)^2 + 4 - 1$
$= -2(16) + 4 - 1$
$= -32 + 4 - 1 = -29$

g. $(f \cdot g)(2) = 2(2)^3 - 2(2)^2$
$= 2(8) - 2(4)$
$= 16 - 8 = 8$

h. $\left(\frac{f}{g}\right)(1) = \frac{1-1}{2(1)^2} = \frac{0}{2(1)} = \frac{0}{2} = 0$

74. $f(x) = 2x^2+3 \qquad g(x) = 4x^3+1$

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a. $(f+g)(x) = 2x^2 + 3 + 4x^3 + 1$
$= 4x^3 + 2x^2 + 4$
Domain: $\{x \mid x \text{ is any real number}\}$.

b. $(f-g)(x) = (2x^2 + 3) - (4x^3 + 1)$
$= 2x^2 + 3 - 4x^3 - 1$
$= -4x^3 + 2x^2 + 2$
Domain: $\{x \mid x \text{ is any real number}\}$.

c. $(f \cdot g)(x) = (2x^2 + 3)(4x^3 + 1)$
$= 8x^5 + 12x^3 + 2x^2 + 3$
Domain: $\{x \mid x \text{ is any real number}\}$.

d. $\left(\frac{f}{g}\right)(x) = \frac{2x^2 + 3}{4x^3 + 1}$
$4x^3 + 1 \neq 0$
$4x^3 \neq -1$
$x^3 \neq -\frac{1}{4} \Rightarrow x \neq \sqrt[3]{-\frac{1}{4}} = -\frac{\sqrt[3]{2}}{2}$
Domain: $\left\{x \mid x \neq -\frac{\sqrt[3]{2}}{2}\right\}$.

e. $(f+g)(3) = 4(3)^3 + 2(3)^2 + 4$
$= 4(27) + 2(9) + 4$
$= 108 + 18 + 4 = 130$

f. $(f-g)(4) = -4(4)^3 + 2(4)^2 + 2$
$= -4(64) + 2(16) + 2$
$= -256 + 32 + 2 = -222$

g. $(f \cdot g)(2) = 8(2)^5 + 12(2)^3 + 2(2)^2 + 3$
$= 8(32) + 12(8) + 2(4) + 3$
$= 256 + 96 + 8 + 3 = 363$

h. $\left(\frac{f}{g}\right)(1) = \frac{2(1)^2 + 3}{4(1)^3 + 1} = \frac{2(1) + 3}{4(1) + 1} = \frac{2 + 3}{4 + 1} = \frac{5}{5} = 1$

75. $f(x) = \sqrt{x} \qquad g(x) = 3x - 5$

a. $(f+g)(x) = \sqrt{x} + 3x - 5$
Domain: $\{x \mid x \geq 0\}$.

b. $(f-g)(x) = \sqrt{x} - (3x - 5) = \sqrt{x} - 3x + 5$
Domain: $\{x \mid x \geq 0\}$.

c. $(f \cdot g)(x) = \sqrt{x}(3x - 5) = 3x\sqrt{x} - 5\sqrt{x}$
Domain: $\{x \mid x \geq 0\}$.

d. $\left(\frac{f}{g}\right)(x) = \frac{\sqrt{x}}{3x - 5}$
$x \geq 0$ and $3x - 5 \neq 0$
$3x \neq 5 \Rightarrow x \neq \frac{5}{3}$
Domain: $\left\{x \mid x \geq 0 \text{ and } x \neq \frac{5}{3}\right\}$.

e. $(f+g)(3) = \sqrt{3} + 3(3) - 5$
$= \sqrt{3} + 9 - 5 = \sqrt{3} + 4$

f. $(f-g)(4) = \sqrt{4} - 3(4) + 5$
$= 2 - 12 + 5 = -5$

g. $(f \cdot g)(2) = 3(2)\sqrt{2} - 5\sqrt{2}$
$= 6\sqrt{2} - 5\sqrt{2} = \sqrt{2}$

h. $\left(\frac{f}{g}\right)(1) = \frac{\sqrt{1}}{3(1) - 5} = \frac{1}{3 - 5} = \frac{1}{-2} = -\frac{1}{2}$

76. $f(x) = |x| \qquad g(x) = x$

a. $(f+g)(x) = |x| + x$
Domain: $\{x \mid x \text{ is any real number}\}$.

b. $(f-g)(x) = |x| - x$
Domain: $\{x \mid x \text{ is any real number}\}$.

c. $(f \cdot g)(x) = |x| \cdot x = x|x|$
Domain: $\{x \mid x \text{ is any real number}\}$.

d. $\left(\frac{f}{g}\right)(x) = \frac{|x|}{x}$
Domain: $\{x \mid x \neq 0\}$.

e. $(f+g)(3) = |3| + 3 = 3 + 3 = 6$

f. $(f-g)(4) = |4| - 4 = 4 - 4 = 0$

g. $(f \cdot g)(2) = 2|2| = 2 \cdot 2 = 4$

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h. $\left(\frac{f}{g}\right)(1)=\frac{|1|}{1}=\frac{1}{1}=1$

77. $f(x)=1+\frac{1}{x} \qquad g(x)=\frac{1}{x}$

a. $(f+g)(x)=1+\frac{1}{x}+\frac{1}{x}=1+\frac{2}{x}$

Domain: $\{x \mid x \neq 0\}$.

b. $(f-g)(x)=1+\frac{1}{x}-\frac{1}{x}=1$

Domain: $\{x \mid x \neq 0\}$.

c. $(f \cdot g)(x)=\left(1+\frac{1}{x}\right)\frac{1}{x}=\frac{1}{x}+\frac{1}{x^2}$

Domain: $\{x \mid x \neq 0\}$.

d. $\left(\frac{f}{g}\right)(x)=\frac{1+\frac{1}{x}}{\frac{1}{x}}=\frac{\frac{x+1}{x}}{\frac{1}{x}}=\frac{x+1}{x}\cdot\frac{x}{1}=x+1$

Domain: $\{x \mid x \neq 0\}$.

e. $(f+g)(3)=1+\frac{2}{3}=\frac{5}{3}$

f. $(f-g)(4)=1$

g. $(f \cdot g)(2)=\frac{1}{2}+\frac{1}{(2)^2}=\frac{1}{2}+\frac{1}{4}=\frac{3}{4}$

h. $\left(\frac{f}{g}\right)(1)=1+1=2$

78. $f(x)=\sqrt{x-1} \qquad g(x)=\sqrt{4-x}$

a. $(f+g)(x)=\sqrt{x-1}+\sqrt{4-x}$

$x-1 \geq 0$ and $4-x \geq 0$

$x \geq 1$ and $-x \geq -4$

$x \leq 4$

Domain: $\{x \mid 1 \leq x \leq 4\}$.

b. $(f-g)(x)=\sqrt{x-1}-\sqrt{4-x}$

$x-1 \geq 0$ and $4-x \geq 0$

$x \geq 1$ and $-x \geq -4$

$x \leq 4$

Domain: $\{x \mid 1 \leq x \leq 4\}$.

c. $(f \cdot g)(x)=\left(\sqrt{x-1}\right)\left(\sqrt{4-x}\right)$

$=\sqrt{-x^2+5x-4}$

$x-1 \geq 0$ and $4-x \geq 0$

$x \geq 1$ and $-x \geq -4$

$x \leq 4$

Domain: $\{x \mid 1 \leq x \leq 4\}$.

d. $\left(\frac{f}{g}\right)(x)=\frac{\sqrt{x-1}}{\sqrt{4-x}}=\sqrt{\frac{x-1}{4-x}}$

$x-1 \geq 0$ and $4-x > 0$

$x \geq 1$ and $-x > -4$

$x < 4$

Domain: $\{x \mid 1 \leq x < 4\}$.

e. $(f+g)(3)=\sqrt{3-1}+\sqrt{4-3}$

$=\sqrt{2}+\sqrt{1}=\sqrt{2}+1$

f. $(f-g)(4)=\sqrt{4-1}-\sqrt{4-4}$

$=\sqrt{3}-\sqrt{0}=\sqrt{3}-0=\sqrt{3}$

g. $(f \cdot g)(2)=\sqrt{-(2)^2+5(2)-4}$

$=\sqrt{-4+10-4}=\sqrt{2}$

h. $\left(\frac{f}{g}\right)(1)=\sqrt{\frac{1-1}{4-1}}=\sqrt{\frac{0}{3}}=\sqrt{0}=0$

79. $f(x)=\frac{2x+3}{3x-2} \qquad g(x)=\frac{4x}{3x-2}$

a. $(f+g)(x)=\frac{2x+3}{3x-2}+\frac{4x}{3x-2}$

$=\frac{2x+3+4x}{3x-2}=\frac{6x+3}{3x-2}$

$3x-2 \neq 0$

$3x \neq 2 \Rightarrow x \neq \frac{2}{3}$

Domain: $\left\{x \mid x \neq \frac{2}{3}\right\}$.

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b. $(f-g)(x)=\dfrac{2x+3}{3x-2}-\dfrac{4x}{3x-2}$

$=\dfrac{2x+3-4x}{3x-2}=\dfrac{-2x+3}{3x-2}$

$3x-2\neq 0$

$3x\neq 2\Rightarrow x\neq\dfrac{2}{3}$

Domain: $\left\{x\,\middle|\, x\neq\dfrac{2}{3}\right\}$.

c. $(f\cdot g)(x)=\left(\dfrac{2x+3}{3x-2}\right)\left(\dfrac{4x}{3x-2}\right)=\dfrac{8x^2+12x}{(3x-2)^2}$

$3x-2\neq 0$

$3x\neq 2\Rightarrow x\neq\dfrac{2}{3}$

Domain: $\left\{x\,\middle|\, x\neq\dfrac{2}{3}\right\}$.

d. $\left(\dfrac{f}{g}\right)(x)=\dfrac{\dfrac{2x+3}{3x-2}}{\dfrac{4x}{3x-2}}=\dfrac{2x+3}{3x-2}\cdot\dfrac{3x-2}{4x}=\dfrac{2x+3}{4x}$

$3x-2\neq 0$ and $x\neq 0$

$3x\neq 2$

$x\neq\dfrac{2}{3}$

Domain: $\left\{x\,\middle|\, x\neq\dfrac{2}{3}\text{ and }x\neq 0\right\}$.

e. $(f+g)(3)=\dfrac{6(3)+3}{3(3)-2}=\dfrac{18+3}{9-2}=\dfrac{21}{7}=3$

f. $(f-g)(4)=\dfrac{-2(4)+3}{3(4)-2}=\dfrac{-8+3}{12-2}=\dfrac{-5}{10}=-\dfrac{1}{2}$

g. $(f\cdot g)(2)=\dfrac{8(2)^2+12(2)}{(3(2)-2)^2}$

$=\dfrac{8(4)+24}{(6-2)^2}=\dfrac{32+24}{(4)^2}=\dfrac{56}{16}=\dfrac{7}{2}$

h. $\left(\dfrac{f}{g}\right)(1)=\dfrac{2(1)+3}{4(1)}=\dfrac{2+3}{4}=\dfrac{5}{4}$

80. $f(x)=\sqrt{x+1}\qquad g(x)=\dfrac{2}{x}$

a. $(f+g)(x)=\sqrt{x+1}+\dfrac{2}{x}$

$x+1\geq 0$ and $x\neq 0$

$x\geq -1$

Domain: $\{x\,|\, x\geq -1,\text{ and }x\neq 0\}$.

b. $(f-g)(x)=\sqrt{x+1}-\dfrac{2}{x}$

$x+1\geq 0$ and $x\neq 0$

$x\geq -1$

Domain: $\{x\,|\, x\geq -1,\text{ and }x\neq 0\}$.

c. $(f\cdot g)(x)=\sqrt{x+1}\cdot\dfrac{2}{x}=\dfrac{2\sqrt{x+1}}{x}$

$x+1\geq 0$ and $x\neq 0$

$x\geq -1$

Domain: $\{x\,|\, x\geq -1,\text{ and }x\neq 0\}$.

d. $\left(\dfrac{f}{g}\right)(x)=\dfrac{\sqrt{x+1}}{\dfrac{2}{x}}=\dfrac{x\sqrt{x+1}}{2}$

$x+1\geq 0$ and $x\neq 0$

$x\geq -1$

Domain: $\{x\,|\, x\geq -1,\text{ and }x\neq 0\}$.

e. $(f+g)(3)=\sqrt{3+1}+\dfrac{2}{3}=\sqrt{4}+\dfrac{2}{3}=2+\dfrac{2}{3}=\dfrac{8}{3}$

f. $(f-g)(4)=\sqrt{4+1}-\dfrac{2}{4}=\sqrt{5}-\dfrac{1}{2}$

g. $(f\cdot g)(2)=\dfrac{2\sqrt{2+1}}{2}=\dfrac{2\sqrt{3}}{2}=\sqrt{3}$

h. $\left(\dfrac{f}{g}\right)(1)=\dfrac{1\sqrt{1+1}}{2}=\dfrac{\sqrt{2}}{2}$

81. $f(x)=3x+1\qquad (f+g)(x)=6-\dfrac{1}{2}x$

$6-\dfrac{1}{2}x=3x+1+g(x)$

$5-\dfrac{7}{2}x=g(x)$

$g(x)=5-\dfrac{7}{2}x$

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82. $f(x)=\dfrac{1}{x}$ $\qquad \left(\dfrac{f}{g}\right)(x)=\dfrac{x+1}{x^2-x}$

$$\frac{x+1}{x^2-x}=\frac{\frac{1}{x}}{g(x)}$$

$$g(x)=\frac{\frac{1}{x}}{\frac{x+1}{x^2-x}}=\frac{1}{x}\cdot\frac{x^2-x}{x+1}$$
$$=\frac{1}{x}\cdot\frac{x(x-1)}{x+1}=\frac{x-1}{x+1}$$

83. $f(x)=4x+3$

$$\frac{f(x+h)-f(x)}{h}=\frac{4(x+h)+3-(4x+3)}{h}$$
$$=\frac{4x+4h+3-4x-3}{h}$$
$$=\frac{4h}{h}=4$$

84. $f(x)=-3x+1$

$$\frac{f(x+h)-f(x)}{h}=\frac{-3(x+h)+1-(-3x+1)}{h}$$
$$=\frac{-3x-3h+1+3x-1}{h}$$
$$=\frac{-3h}{h}=-3$$

85. $f(x)=x^2-4$

$$\frac{f(x+h)-f(x)}{h}$$
$$=\frac{(x+h)^2-4-(x^2-4)}{h}$$
$$=\frac{x^2+2xh+h^2-4-x^2+4}{h}$$
$$=\frac{2xh+h^2}{h}$$
$$=2x+h$$

86. $f(x)=3x^2+2$

$$\frac{f(x+h)-f(x)}{h}$$
$$=\frac{3(x+h)^2+2-(3x^2+2)}{h}$$
$$=\frac{3x^2+6xh+3h^2+2-3x^2-2}{h}$$
$$=\frac{6xh+3h^2}{h}$$
$$=6x+3h$$

87. $f(x)=x^2-x+4$

$$\frac{f(x+h)-f(x)}{h}$$
$$=\frac{(x+h)^2-(x+h)+4-(x^2-x+4)}{h}$$
$$=\frac{x^2+2xh+h^2-x-h+4-x^2+x-4}{h}$$
$$=\frac{2xh+h^2-h}{h}$$
$$=2x+h-1$$

88. $f\left(x\right)=3x^2-2x+6$

$$\frac{f\left(x+h\right)-f\left(x\right)}{h}$$
$$=\frac{\left[3\left(x+h\right)^2-2\left(x+h\right)+6\right]-\left[3x^2-2x+6\right]}{h}$$
$$=\frac{3\left(x^2+2xh+h^2\right)-2x-2h+6-3x^2+2x-6}{h}$$
$$=\frac{3x^2+6xh+3h^2-2h-3x^2}{h}=\frac{6xh+3h^2-2h}{h}$$
$$=6x+3h-2$$

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89. $f(x)=\dfrac{5}{4x-3}$

$$\begin{aligned}\frac{f(x+h)-f(x)}{h}&=\frac{\dfrac{5}{4(x+h)-3}-\dfrac{5}{4x-3}}{h}\\&=\frac{\dfrac{5(4x-3)-5\big(4(x+h)-3\big)}{\big(4(x+h)-3\big)\big(4x-3\big)}}{h}\\&=\left(\frac{20x+15-20x-15-20h}{\big(4(x+h)-3\big)\big(4x-3\big)}\right)\left(\frac{1}{h}\right)\\&=\left(\frac{-20h}{\big(4(x+h)-3\big)\big(4x-3\big)}\right)\left(\frac{1}{h}\right)\\&=\frac{-20}{\big(4(x+h)-3\big)\big(4x-3\big)}\end{aligned}$$

90. $f(x)=\dfrac{1}{x+3}$

$$\begin{aligned}\frac{f(x+h)-f(x)}{h}&=\frac{\dfrac{1}{x+h+3}-\dfrac{1}{x+3}}{h}\\&=\frac{\dfrac{x+3-\big(x+3+h\big)}{\big(x+h+3\big)\big(x+3\big)}}{h}\\&=\left(\frac{x+3-x-3-h}{\big(x+h+3\big)\big(x+3\big)}\right)\left(\frac{1}{h}\right)\\&=\left(\frac{-h}{\big(x+h+3\big)\big(x+3\big)}\right)\left(\frac{1}{h}\right)\\&=\frac{-1}{\big(x+h+3\big)\big(x+3\big)}\end{aligned}$$

91. $f(x)=\dfrac{2x}{x+3}$

$$\begin{aligned}\frac{f(x+h)-f(x)}{h}&=\frac{\dfrac{2(x+h)}{x+h+3}-\dfrac{2x}{x+3}}{h}\\&=\frac{\dfrac{2(x+h)(x+3)-2x\big(x+3+h\big)}{\big(x+h+3\big)\big(x+3\big)}}{h}\\&=\frac{\dfrac{2x^2+6x+2hx+6h-2x^2-6x-2xh}{\big(x+h+3\big)\big(x+3\big)}}{h}\\&=\left(\frac{6h}{\big(x+h+3\big)\big(x+3\big)}\right)\left(\frac{1}{h}\right)\\&=\frac{6}{\big(x+h+3\big)\big(x+3\big)}\end{aligned}$$

92. $f(x)=\dfrac{5x}{x-4}$

$$\begin{aligned}\frac{f(x+h)-f(x)}{h}&=\frac{\dfrac{5(x+h)}{x+h-4}-\dfrac{5x}{x-4}}{h}\\&=\frac{\dfrac{5(x+h)(x-4)-5x\big(x-4+h\big)}{\big(x+h-4\big)\big(x-4\big)}}{h}\\&=\frac{\dfrac{5x^2-20x+5hx-20h-5x^2+20x-5xh}{\big(x+h-4\big)\big(x-4\big)}}{h}\\&=\left(\frac{-20h}{\big(x+h-4\big)\big(x-4\big)}\right)\left(\frac{1}{h}\right)\\&=-\frac{20}{\big(x+h-4\big)\big(x-4\big)}\end{aligned}$$

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93. $f(x)=\sqrt{x-2}$

$$\frac{f(x+h)-f(x)}{h}$$

$$=\frac{\sqrt{x+h-2}-\sqrt{x-2}}{h}$$

$$=\frac{\sqrt{x+h-2}-\sqrt{x-2}}{h}\cdot\frac{\sqrt{x+h-2}+\sqrt{x-2}}{\sqrt{x+h-2}+\sqrt{x-2}}$$

$$=\frac{x+h-2-x+2}{h\left(\sqrt{x+h-2}+\sqrt{x-2}\right)}$$

$$=\frac{h}{h\left(\sqrt{x+h-2}+\sqrt{x-2}\right)}$$

$$=\frac{1}{\sqrt{x+h-2}+\sqrt{x-2}}$$

94. $f(x)=\sqrt{x+1}$

$$\frac{f(x+h)-f(x)}{h}$$

$$=\frac{\sqrt{x+h+1}-\sqrt{x+1}}{h}$$

$$=\frac{\sqrt{x+h+1}-\sqrt{x+1}}{h}\cdot\frac{\sqrt{x+h+1}+\sqrt{x+1}}{\sqrt{x+h+1}+\sqrt{x+1}}$$

$$=\frac{x+h+1-(x+1)}{h\left(\sqrt{x+h+1}+\sqrt{x+1}\right)}=\frac{h}{h\left(\sqrt{x+h+1}+\sqrt{x+1}\right)}$$

$$=\frac{1}{\sqrt{x+h+1}+\sqrt{x+1}}$$

95. $f(x)=\frac{1}{x^2}$

$$\frac{f(x+h)-f(x)}{h}=\frac{\frac{1}{(x+h)^2}-\frac{1}{x^2}}{h}$$

$$=\frac{\frac{x^2-(x+h)^2}{x^2(x+h)^2}}{h}$$

$$=\frac{\frac{x-\left(x^2+2xh+h^2\right)}{x^2(x+h)^2}}{h}$$

$$=\left(\frac{1}{h}\right)\frac{-2xh-h^2}{x^2(x+h)^2}$$

$$=\left(\frac{1}{h}\right)\frac{h(-2x-h)}{x^2(x+h)^2}$$

$$=\frac{-2x-h}{x^2(x+h)^2}=\frac{-(2x+h)}{x^2(x+h)^2}$$

96. $f(x)=\frac{1}{x^2+1}$

$$\frac{f(x+h)-f(x)}{h}=\frac{\frac{1}{(x+h)^2+1}-\frac{1}{x^2+1}}{h}$$

$$=\frac{\frac{x^2+1-\left((x+h)^2+1\right)}{(x^2+1)\left((x+h)^2+1\right)}}{h}$$

$$=\frac{\frac{x^2+1-\left(x^2+2xh+h^2\right)-1}{(x^2+1)\left((x+h)^2+1\right)}}{h}$$

$$=\left(\frac{1}{h}\right)\frac{-2xh-h^2}{(x^2+1)\left((x+h)^2+1\right)}$$

$$=\left(\frac{1}{h}\right)\frac{h(-2x-h)}{(x^2+1)\left((x+h)^2+1\right)}$$

$$=\frac{-2x-h}{(x^2+1)\left((x+h)^2+1\right)}$$

$$=\frac{-(2x+h)}{(x^2+1)\left((x+h)^2+1\right)}$$

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97. $f(x)=\sqrt{4-x^2}$

$$\frac{f(x+h)-f(x)}{h}$$

$$=\frac{\sqrt{4-(x+h)^2}-\sqrt{4-x^2}}{h}$$

$$=\frac{\sqrt{4-(x+h)^2}-\sqrt{4-x^2}}{h}\cdot\frac{\sqrt{4-(x+h)^2}+\sqrt{4-x^2}}{\sqrt{4-(x+h)^2}+\sqrt{4-x^2}}$$

$$=\frac{4-(x+h)^2-(4-x^2)}{h\left(\sqrt{4-(x+h)^2}-\sqrt{4-x^2}\right)}$$

$$=\frac{4-(x^2+2xh+h^2)-(4-x^2)}{h\left(\sqrt{x+h+1}+\sqrt{x+1}\right)}$$

$$=\frac{-2xh-h^2}{h\left(\sqrt{x+h+1}+\sqrt{x+1}\right)}$$

$$=\frac{-2x-h}{\sqrt{4-(x+h)^2}-\sqrt{4-x^2}}$$

$$=\frac{-(2x+h)}{\sqrt{4-(x+h)^2}-\sqrt{4-x^2}}$$

98. $f(x)=\dfrac{1}{\sqrt{x+2}}$

$$\frac{f(x+h)-f(x)}{h}=$$

$$\frac{\dfrac{1}{\sqrt{x+h+2}}-\dfrac{1}{\sqrt{x+2}}}{h}=$$

$$\frac{\sqrt{x+2}-\sqrt{x+h+2}}{h\sqrt{x+2}\sqrt{x+h+2}}=$$

$$\frac{\sqrt{x+2}-\sqrt{x+h+2}}{h\sqrt{x+2}\sqrt{x+h+2}}\cdot\frac{\sqrt{x+2}+\sqrt{x+h+2}}{\sqrt{x+2}+\sqrt{x+h+2}}=$$

$$\frac{x+2-(x+h+2)}{h(x+2)\sqrt{x+h+2}+(x+h+2)\sqrt{x+2}}=$$

$$\frac{x+2-x-h-2}{h(x+2)\sqrt{x+h+2}+(x+h+2)\sqrt{x+2}}=$$

$$\frac{-h}{h(x+2)\sqrt{x+h+2}+(x+h+2)\sqrt{x+2}}=$$

$$-\frac{1}{(x+2)\sqrt{x+h+2}+(x+h+2)\sqrt{x+2}}$$

99.
$$11=x^2-2x+3$$
$$0=x^2-2x-8$$
$$0=(x-4)(x+2)$$
$$x-4=0 \quad \text{or} \quad x+2=0$$
$$x=4 \quad \text{or} \quad x=-2$$

The solution set is: $\{-2,4\}$

100.
$$-\frac{7}{16}=\frac{5}{6}x-\frac{3}{4}$$
$$-\frac{7}{16}+\frac{3}{4}=\frac{5}{6}x$$
$$\frac{5}{6}x=-\frac{7}{16}+\frac{12}{16}$$
$$\frac{5}{6}x=\frac{5}{16}$$
$$x=\frac{5}{16}\cdot\frac{6}{5}=\frac{3}{8}$$

The solution set is: $\left\{\dfrac{3}{8}\right\}$

101. $f(x)=2x^3+Ax^2+4x-5$ and $f(2)=5$

$$f(2)=2(2)^3+A(2)^2+4(2)-5$$
$$5=16+4A+8-5$$
$$5=4A+19$$
$$-14=4A$$
$$A=\frac{-14}{4}=-\frac{7}{2}$$

102. $f(x)=3x^2-Bx+4$ and $f(-1)=12$:

$$f(-1)=3(-1)^2-B(-1)+4$$
$$12=3+B+4$$
$$B=5$$

103. $f(x)=\dfrac{3x+8}{2x-A}$ and $f(0)=2$

$$f(0)=\frac{3(0)+8}{2(0)-A}$$
$$2=\frac{8}{-A}$$
$$-2A=8$$
$$A=-4$$

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104. $f(x)=\dfrac{2x-B}{3x+4}$ and $f(2)=\dfrac{1}{2}$

$$f(2)=\frac{2(2)-B}{3(2)+4}$$
$$\frac{1}{2}=\frac{4-B}{10}$$
$$5=4-B$$
$$B=-1$$

105. Let x represent the length of the rectangle.

Then, $\dfrac{x}{2}$ represents the width of the rectangle since the length is twice the width. The function for the area is: $A(x)=x\cdot\dfrac{x}{2}=\dfrac{x^2}{2}=\dfrac{1}{2}x^2$

106. Let x represent the length of one of the two equal sides. The function for the area is:

$$A(x)=\frac{1}{2}\cdot x\cdot x=\frac{1}{2}x^2$$

107. Let x represent the number of hours worked.
The function for the gross salary is:
$G(x)=16x$

108. Let x represent the number of items sold.
The function for the gross salary is:
$G(x)=10x+100$

109. **a.** $H(1)=20-4.9(1)^2$
$=20-4.9=15.1$ meters

$H(1.1)=20-4.9(1.1)^2$
$=20-4.9(1.21)$
$=20-5.929=14.071$ meters

$H(1.2)=20-4.9(1.2)^2$
$=20-4.9(1.44)$
$=20-7.056=12.944$ meters

b. $H(x)=15$:
$15=20-4.9x^2$
$-5=-4.9x^2$
$x^2\approx 1.0204$
$x\approx 1.01$ seconds

$H(x)=10$:
$10=20-4.9x^2$
$-10=-4.9x^2$
$x^2\approx 2.0408$
$x\approx 1.43$ seconds

$H(x)=5$:
$5=20-4.9x^2$
$-15=-4.9x^2$
$x^2\approx 3.0612$
$x\approx 1.75$ seconds

c. $H(x)=0$
$0=20-4.9x^2$
$-20=-4.9x^2$
$x^2\approx 4.0816$
$x\approx 2.02$ seconds

110. **a.** $H(1)=20-13(1)^2=20-13=7$ meters

$H(1.1)=20-13(1.1)^2=20-13(1.21)$
$=20-15.73=4.27$ meters

$H(1.2)=20-13(1.2)^2=20-13(1.44)$
$=20-18.72=1.28$ meters

b. $H(x)=15$
$15=20-13x^2$
$-5=-13x^2$
$x^2\approx 0.3846$
$x\approx 0.62$ seconds

$H(x)=10$
$10=20-13x^2$
$-10=-13x^2$
$x^2\approx 0.7692$
$x\approx 0.88$ seconds

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$$H(x) = 5$$
$$5 = 20 - 13x^2$$
$$-15 = -13x^2$$
$$x^2 \approx 1.1538$$
$$x \approx 1.07 \text{ seconds}$$

c. $H(x) = 0$
$$0 = 20 - 13x^2$$
$$-20 = -13x^2$$
$$x^2 \approx 1.5385$$
$$x \approx 1.24 \text{ seconds}$$

111. $C(x) = 100 + \frac{x}{10} + \frac{36,000}{x}$

a. $C(500) = 100 + \frac{500}{10} + \frac{36,000}{500}$
$= 100 + 50 + 72$
$= \$222$

b. $C(450) = 100 + \frac{450}{10} + \frac{36,000}{450}$
$= 100 + 45 + 80$
$= \$225$

c. $C(600) = 100 + \frac{600}{10} + \frac{36,000}{600}$
$= 100 + 60 + 60$
$= \$220$

d. $C(400) = 100 + \frac{400}{10} + \frac{36,000}{400}$
$= 100 + 40 + 90$
$= \$230$

112. $A(x) = 4x\sqrt{1-x^2}$

a. $A\left(\frac{1}{3}\right) = 4 \cdot \frac{1}{3}\sqrt{1-\left(\frac{1}{3}\right)^2} = \frac{4}{3}\sqrt{\frac{8}{9}} = \frac{4}{3} \cdot \frac{2\sqrt{2}}{3}$
$= \frac{8\sqrt{2}}{9} \approx 1.26 \text{ ft}^2$

b. $A\left(\frac{1}{2}\right) = 4 \cdot \frac{1}{2}\sqrt{1-\left(\frac{1}{2}\right)^2} = 2\sqrt{\frac{3}{4}} = 2 \cdot \frac{\sqrt{3}}{2}$
$= \sqrt{3} \approx 1.73 \text{ ft}^2$

c. $A\left(\frac{2}{3}\right) = 4 \cdot \frac{2}{3}\sqrt{1-\left(\frac{2}{3}\right)^2} = \frac{8}{3}\sqrt{\frac{5}{9}} = \frac{8}{3} \cdot \frac{\sqrt{5}}{3}$
$= \frac{8\sqrt{5}}{9} \approx 1.99 \text{ ft}^2$

113. $R(x) = \left(\frac{L}{P}\right)(x) = \frac{L(x)}{P(x)}$

114. $T(x) = (V + P)(x) = V(x) + P(x)$

115. $H(x) = (P \cdot I)(x) = P(x) \cdot I(x)$

116. $N(x) = (I - T)(x) = I(x) - T(x)$

117. **a.** $P(x) = R(x) - C(x)$
$= \left(-1.2x^2 + 220x\right) - \left(0.05x^3 - 2x^2 + 65x + 500\right)$
$= -1.2x^2 + 220x - 0.05x^3 + 2x^2 - 65x - 500$
$= -0.05x^3 + 0.8x^2 + 155x - 500$

b. $P(15) = -0.05(15)^3 + 0.8(15)^2 + 155(15) - 500$
$= -168.75 + 180 + 2325 - 500$
$= \$1836.25$

c. When 15 hundred smartphones are sold, the profit is \$1836.25.

118. **a.** P is the dependent variable; a is the independent variable

b. $P(20) = 0.027(20)^2 - 6.530(20) + 363.804$
$= 10.8 - 130.6 + 363.804$
$= 244.004$
In 2015 there are 244.004 million people who are 20 years of age or older.

c. $P(0) = 0.027(0)^2 - 6.530(0) + 363.804$
$= 363.804$
In 2015 there are 363.804 million people.

119. **a.** $R(v) = 2.2v; B(v) = 0.05v^2 + 0.4\text{v} - 15$
$D(v) = R(v) + B(v)$
$= 2.2v + 0.05v^2 + 0.4\text{v} - 15$
$= 0.05v^2 + 2.6v - 15$

b. $D(60) = 0.05(60)^2 + 2.6(60) - 15$
$= 180 + 156 - 15$
$= 321$

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c. The car will need 321 feet to stop once the impediment is observed.

120. a. $h(x) = 2x$

$h(a+b) = 2(a+b) = 2a + 2b$

$= h(a) + h(b)$

$h(x) = 2x$ has the property.

b. $g(x) = x^2$

$g(a+b) = (a+b)^2 = a^2 + 2ab + b^2$

Since

$a^2 + 2ab + b^2 \neq a^2 + b^2 = g(a) + g(b)$,

$g(x) = x^2$ does not have the property.

c. $F(x) = 5x - 2$

$F(a+b) = 5(a+b) - 2 = 5a + 5b - 2$

Since

$5a + 5b - 2 \neq 5a - 2 + 5b - 2 = F(a) + F(b)$,

$F(x) = 5x - 2$ does not have the property.

d. $G(x) = \dfrac{1}{x}$

$G(a+b) = \dfrac{1}{a+b} \neq \dfrac{1}{a} + \dfrac{1}{b} = G(a) + G(b)$

$G(x) = \dfrac{1}{x}$ does not have the property.

---

121. $\dfrac{f(x+h) - f(x)}{h} = \dfrac{\sqrt[3]{x+h} - \sqrt[3]{x}}{h} =$

$= \dfrac{(x+h)^{1/3} - x^{1/3}}{h}$

$= \dfrac{(x+h)^{1/3} - x^{1/3}}{h} \cdot \dfrac{(x+h)^{2/3} + x^{1/3}(x+h)^{1/3} + x^{2/3}}{(x+h)^{2/3} + x^{1/3}(x+h)^{1/3} + x^{2/3}}$

$= \dfrac{h}{(x+h)^{2/3} + x^{1/3}(x+h)^{1/3} + x^{2/3}}$

$= \dfrac{x+h-x}{h\left[(x+h)^{2/3} + x^{1/3}(x+h)^{1/3} + x^{2/3}\right]} = \dfrac{h}{h\left[(x+h)^{2/3} + x^{1/3}(x+h)^{1/3} + x^{2/3}\right]}$

$= \dfrac{1}{(x+h)^{2/3} + x^{1/3}(x+h)^{1/3} + x^{2/3}}$

122. $f\left(\dfrac{x+4}{5x-4}\right) = 3x^2 - 2$

Solve $\dfrac{x+4}{5x-4} = 1.$

$\dfrac{x+4}{5x-4} = 1$

$x + 4 = 5x - 4$

$x = 2$

Therefore, $f(1) = 3(2)^2 - 2 = 10$

123. We need $\dfrac{x^2+1}{7 - |3x-1|} \geq 0$. Since $x^2 + 1 > 0$ for all real numbers x, we need $7 - |3x-1| > 0$.

$7 - |3x-1| > 0$

$|3x-1| < 7$

$-7 < 3x - 1 < 7$

$-2 < x < \dfrac{8}{3}$

The domain of f is $\left\{x \mid -2 < x < \dfrac{8}{3}\right\}$, or $\left(-2, \dfrac{8}{3}\right)$ in interval notation.

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124. No. The domain of f is $\{x \mid x \text{ is any real number}\}$, but the domain of g is $\{x \mid x \neq -1\}$.

125. $\dfrac{3x - x^3}{(your\ age)}$

126. Answers will vary.

127. $(x+12)^2 + y^2 = 16$

x-intercept (y=0):

$(x+12)^2 + 0^2 = 16$

$(x+12)^2 = 16$

$(x+12) = \pm 4$

$x = -12 \pm 4$

$x = -16, x = -8$

$(-16, 0), (-8, 0)$

y-intercept (x=0):

$(0+12)^2 + y^2 = 16$

$(12)^2 + y^2 = 16$

$y^2 = 16 - 144 = -128$

There are no real solutions so there are no y-intercepts.

Symmetry: $(x+12)^2 + (-y)^2 = 16$

$(x+12)^2 + y^2 = 16$

This shows x-axis symmetry.

128. $y = 3x^2 - 8\sqrt{x}$

$y = 3(-1)^2 - 8\sqrt{-1}$

There is no solution so (-1,-5) is NOT a solution.

$y = 3x^2 - 8\sqrt{x}$

$y = 3(4)^2 - 8\sqrt{4}$

$= 48 - 16 = 32$

So (4,32) is a solution.

$y = 3x^2 - 8\sqrt{x}$

$y = 3(9)^2 - 8\sqrt{9}$

$= 243 - 24 = 219 \neq 171$

So (9,171) is NOT a solution.

129. Let x represent the amount of the 7% fat hamburger added.

% fat	tot. amt.	amt. of fat
20%	12	$(0.20)(12)$
7%	x	$(0.07)(x)$
15%	$12+x$	$(0.15)(12+x)$

$(0.20)(12) + (0.07)(x) = (0.15)(12+x)$

$2.4 + 0.07x = 1.8 + 0.15x$

$0.6 = .08x$

$x = 7.5$

7.5 lbs. of the 7% fat hamburger must be added, producing 19.5 lbs. of the 15% fat hamburger.

130. $x^3 - 9x = 2x^2 - 18$

$x^3 - 2x^2 - 9x + 18 = 0$

$(x^3 - 2x^2) - (9x - 18) = 0$

$x^2(x-2) - 9(x-2) = 0$

$(x^2 - 9)(x-2) = 0$

$(x-3)(x+3)(x-2) = 0$

$(x-3) = 0$ or $(x+3) = 0$ or $(x-2) = 0$

$x = 3, x = -3, x = 2$

The solution set is: $\{3, -3, 2\}$

131. $a + bx = ac + d$

$a - ac = d - bx$

$a(1-c) = d - bx$

$a = \dfrac{d - bx}{1-c}$

132. $r = kd^2$

$0.4 = k(0.6)^2$

$\dfrac{10}{9} = k$

Thus,

$r = \dfrac{10}{9}(1.5)^2$

$= 2.5\ \text{kg} \cdot m^2$

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133. $3x-10y=12$

$-10y=-3x+12$

$y=\frac{3}{10}x-\frac{6}{5}$

The slope of the line is $\frac{3}{10}$. The slope of a perpendicular line would be $-\frac{10}{3}$.

134. $\frac{(4x^2-7)\cdot 3-(3x+5)\cdot 8x}{(4x^2-7)^2}=$

$\frac{12x^2-21-(24x^2+40x)}{(4x^2-7)^2}=$

$\frac{12x^2-21-24x^2-40x}{(4x^2-7)^2}=\frac{-12x^2-40x-21}{(4x^2-7)^2}$

$=-\frac{12x^2+40x+21}{(4x^2-7)^2}$

135. Add the powers of x to obtain a degree of 7.

Section 2.2

1. $x^2+4y^2=16$

x-intercepts:

$x^2+4(0)^2=16$

$x^2=16$

$x=\pm 4\Rightarrow(-4,0),(4,0)$

y-intercepts:

$(0)^2+4y^2=16$

$4y^2=16$

$y^2=4$

$y=\pm 2\Rightarrow(0,-2),(0,2)$

2. False; $x=2y-2$

$-2=2y-2$

$0=2y$

$0=y$

The point $(-2,0)$ is on the graph.

3. vertical

4. $f(5)=-3$

5. $f(x)=ax^2+4$

$a(-1)^2+4=2\Rightarrow a=-2$

6. False. The graph must pass the vertical line test in order to be the graph of a function.

7. False; e.g. $y=\frac{1}{x}$.

8. True

9. c

10. a

11. **a.** $f(0)=3$ since $(0,3)$ is on the graph.
$f(-6)=-3$ since $(-6,-3)$ is on the graph.

b. $f(6)=0$ since $(6,0)$ is on the graph.
$f(11)=1$ since $(11,1)$ is on the graph.

c. $f(3)$ is positive since $f(3)\approx 3.7$.

d. $f(-4)$ is negative since $f(-4)\approx -1$.

e. $f(x)=0$ when $x=-3$, $x=6$, and $x=10$.

f. $f(x)>0$ when $-3<x<6$, and $10<x\le 11$.

g. The domain of f is $\{x\,|\,-6\le x\le 11\}$ or $[-6,11]$.

h. The range of f is $\{y\,|\,-3\le y\le 4\}$ or $[-3,4]$.

i. The x-intercepts are -3, 6, and 10.

j. The y-intercept is 3.

k. The line $y=\frac{1}{2}$ intersects the graph 3 times.

l. The line $x=5$ intersects the graph 1 time.

m. $f(x)=3$ when $x=0$ and $x=4$.

n. $f(x)=-2$ when $x=-5$ and $x=8$.

12. **a.** $f(0)=0$ since $(0,0)$ is on the graph.
$f(6)=0$ since $(6,0)$ is on the graph.

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b. $f(2) = -2$ since $(2, -2)$ is on the graph.
$f(-2) = 1$ since $(-2, 1)$ is on the graph.

c. $f(3)$ is negative since $f(3) \approx -1$.

d. $f(-1)$ is positive since $f(-1) \approx 1.0$.

e. $f(x) = 0$ when $x = 0$, $x = 4$, and $x = 6$.

f. $f(x) < 0$ when $0 < x < 4$.

g. The domain of f is $\{x \mid -4 \le x \le 6\}$ or $[-4, 6]$.

h. The range of f is $\{y \mid -2 \le y \le 3\}$ or $[-2, 3]$.

i. The x-intercepts are 0, 4, and 6.

j. The y-intercept is 0.

k. The line $y = -1$ intersects the graph 2 times.

l. The line $x = 1$ intersects the graph 1 time.

m. $f(x) = 3$ when $x = 5$.

n. $f(x) = -2$ when $x = 2$.

13. Not a function since vertical lines will intersect the graph in more than one point.

a. Domain: $\{x \mid x \le -1 \text{ or } x \ge 1\}$;
Range: $\{y \mid y \text{ is any real number}\}$

b. Intercepts: $(-1,0), (1,0)$

c. Symmetry about the x-axis, y-axis and the origin

14. Function

a. Domain: $\{x \mid x \text{ is any real number}\}$;
Range: $\{y \mid y > 0\}$

b. Intercepts: $(0,1)$

c. None

15. Function

a. Domain: $\{x \mid -\pi \le x \le \pi\}$;
Range: $\{y \mid -1 \le y \le 1\}$

b. Intercepts: $\left(-\frac{\pi}{2}, 0\right)$, $\left(\frac{\pi}{2}, 0\right)$, $(0,1)$

c. Symmetry about y-axis.

16. Function

a. Domain: $\{x \mid -\pi \le x \le \pi\}$;
Range: $\{y \mid -1 \le y \le 1\}$

b. Intercepts: $(-\pi, 0)$, $(\pi, 0)$, $(0, 0)$

c. Symmetry about the origin.

17. Not a function since vertical lines will intersect the graph in more than one point.

a. Domain: $\{x \mid x \le 0\}$;
Range: $\{y \mid y \text{ is any real number}\}$

b. Intercepts: $(0,0)$

c. Symmetry about the x-axis

18. Not a function since vertical lines will intersect the graph in more than one point.

a. Domain: $\{x \mid -2 \le x \le 2\}$;
Range: $\{y \mid -2 \le y \le 2\}$

b. Intercepts: $(-2,0)(2,0)(0,-2)(0,2)$

c. Symmetry about the x-axis, y-axis and the origin

19. Function

a. Domain: $\{x \mid 0 < x < 3\}$;
Range: $\{y \mid y < 2\}$

b. Intercepts: (1, 0)

c. None

20. Function

a. Domain: $\{x \mid 0 \le x < 4\}$;
Range: $\{y \mid 0 \le y < 3\}$

b. Intercepts: (0, 0)

c. None

21. Function

a. Domain: $\{x \mid x \text{ is any real number}\}$;
Range: $\{y \mid y \le 2\}$

b. Intercepts: (–3, 0), (3, 0), (0,2)

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c. Symmetry about *y*-axis.

22. Function

a. Domain: $\{x \mid x \geq -3\}$;

Range: $\{y \mid y \geq 0\}$

b. Intercepts: (–3, 0), (2,0), (0,2)

c. None

23. Function

a. Domain: $\{x \mid x \text{ is any real number}\}$;

Range: $\{y \mid y \geq -3\}$

b. Intercepts: (1, 0), (3,0), (0,9)

c. None

24. Function

a. Domain: $\{x \mid x \text{ is any real number}\}$;

Range: $\{y \mid y \leq 5\}$

b. Intercepts: (–1, 0), (2,0), (0,4)

c. None

25. $f(x) = 3x^2 + x - 2$

a. $f(1) = 3(1)^2 + (1) - 2 = 2$

The point $(-1, 2)$ is on the graph of *f*.

b. $f(-2) = 3(-2)^2 + (-2) - 2 = 8$

The point $(-2, 8)$ is on the graph of *f*.

c. Solve for x:

$-2 = 3x^2 + x - 2$

$0 = 3x^2 + x$

$0 = x(3x+1) \Rightarrow x = 0, x = -\frac{1}{3}$

(0, –2) and $\left(-\frac{1}{3}, -2\right)$ are on the graph of f.

d. The domain of *f* is $\{x \mid x \text{ is any real number}\}$.

e. *x*-intercepts:

$f(x) = 0 \Rightarrow 3x^2 + x - 2 = 0$

$(3x-2)(x+1) = 0 \Rightarrow x = \frac{2}{3}, x = -1$

f. *y*-intercept: $f(0) = 3(0)^2 + 0 - 2 = -2$

26. $f(x) = -3x^2 + 5x$

a. $f(-1) = -3(-1)^2 + 5(-1) = -8 \neq 2$

The point $(-1, 2)$ is not on the graph of *f*.

b. $f(-2) = -3(-2)^2 + 5(-2) = -22$

The point $(-2, -22)$ is on the graph of *f*.

c. Solve for x:

$-2 = -3x^2 + 5x \Rightarrow 3x^2 - 5x - 2 = 0$

$(3x+1)(x-2) = 0 \Rightarrow x = -\frac{1}{3}, x = 2$

(2, –2) and $\left(-\frac{1}{3}, -2\right)$ on the graph of f.

d. The domain of *f* is $\{x \mid x \text{ is any real number}\}$.

e. *x*-intercepts:

$f(x) = 0 \Rightarrow -3x^2 + 5x = 0$

$x(-3x+5) = 0 \Rightarrow x = 0, x = \frac{5}{3}$

f. *y*-intercept:

$f(0) = -3(0)^2 + 5(0) = 0$

27. $f(x) = \dfrac{x+2}{x-6}$

a. $f(3) = \dfrac{3+2}{3-6} = -\dfrac{5}{3} \neq 14$

The point $(3, 14)$ is not on the graph of *f*.

b. $f(4) = \dfrac{4+2}{4-6} = \dfrac{6}{-2} = -3$

The point $(4, -3)$ is on the graph of *f*.

c. Solve for x:

$2 = \dfrac{x+2}{x-6}$

$2x - 12 = x + 2$

$x = 14$

(14, 2) is a point on the graph of f.

d. The domain of *f* is $\{x \mid x \neq 6\}$.

e. *x*-intercepts:

$f(x) = 0 \Rightarrow \dfrac{x+2}{x-6} = 0$

$x + 2 = 0 \Rightarrow x = -2$

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f. y-intercept: $f(0)=\dfrac{0+2}{0-6}=-\dfrac{1}{3}$

28. $f(x)=\dfrac{x^2+2}{x+4}$

a. $f(1)=\dfrac{1^2+2}{1+4}=\dfrac{3}{5}$

The point $\left(1,\dfrac{3}{5}\right)$ is on the graph of f.

b. $f(0)=\dfrac{0^2+2}{0+4}=\dfrac{2}{4}=\dfrac{1}{2}$

The point $\left(0,\dfrac{1}{2}\right)$ is on the graph of f.

c. Solve for x:

$$\frac{1}{2}=\frac{x^2+2}{x+4}\Rightarrow x+4=2x^2+4$$
$$0=2x^2-x$$
$$x(2x-1)=0\Rightarrow x=0 \text{ or } x=\frac{1}{2}$$

$\left(0,\dfrac{1}{2}\right)$ and $\left(\dfrac{1}{2},\dfrac{1}{2}\right)$ are on the graph of f.

d. The domain of f is $\{x \mid x\neq -4\}$.

e. x-intercepts:

$$f(x)=0\Rightarrow \frac{x^2+2}{x+4}=0\Rightarrow x^2+2=0$$

This is impossible, so there are no x-intercepts.

f. y-intercept:

$$f(0)=\frac{0^2+2}{0+4}=\frac{2}{4}=\frac{1}{2}$$

29. $f(x)=\dfrac{12x^4}{x^2+1}$

a. $f(-1)=\dfrac{12(-1)^4}{(-1)^2+1}=\dfrac{12}{2}=6$

The point $(-1,1)$ is on the graph of f.

b. $f(3)=\dfrac{12(3)^4}{(3)^2+1}=\dfrac{972}{10}=\dfrac{486}{5}$

The point $\left(3,\dfrac{486}{5}\right)$ is on the graph of f.

c. Solve for x:

$$1=\frac{12x^4}{x^2+1}$$
$$x^2+1=12x^4$$
$$12x^4-x^2-1=0$$
$$(3x^2-1)(4x^2+1)=0$$
$$3x^2-1=0\Rightarrow x=\pm\frac{1}{\sqrt{3}}=\pm\frac{\sqrt{3}}{3}$$

$\left(-\dfrac{\sqrt{3}}{3},1\right),\left(\dfrac{\sqrt{3}}{3},1\right)$ are on the graph of f.

d. The domain of f is $\{x \mid x \text{ is any real number}\}$.

e. x-intercept:

$$f(x)=0\Rightarrow \frac{12x^4}{x^2+1}=0$$
$$12x^4=0\Rightarrow x=0$$

f. y-intercept:

$$f(0)=\frac{12(0)^4}{0^2+1}=\frac{0}{0+1}=0$$

30. $f(x)=\dfrac{2x}{x-2}$

a. $f\left(\dfrac{1}{2}\right)=\dfrac{2\left(\dfrac{1}{2}\right)}{\dfrac{1}{2}-2}=\dfrac{1}{-\dfrac{3}{2}}=-\dfrac{2}{3}$

The point $\left(\dfrac{1}{2},-\dfrac{2}{3}\right)$ is on the graph of f.

b. $f(4)=\dfrac{2(4)}{4-2}=\dfrac{8}{2}=4$

The point $(4,4)$ is on the graph of f.

c. Solve for x:

$$1=\frac{2x}{x-2}\Rightarrow x-2=2x\Rightarrow -2=x$$

(–2,1) is a point on the graph of f.

d. The domain of f is $\{x \mid x\neq 2\}$.

e. x-intercept:

$$f(x)=0\Rightarrow \frac{2x}{x-2}=0\Rightarrow 2x=0$$
$$\Rightarrow x=0$$

f. y-intercept: $f(0)=\dfrac{0}{0-2}=0$

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31. a. $(f+g)(2) = f(2)+g(2) = 2+1 = 3$

b. $(f+g)(4) = f(4)+g(4) = 1+(-3) = -2$

c. $(f-g)(6) = f(6)-g(6) = 0-1 = -1$

d. $(g-f)(6) = g(6)-f(6) = 1-0 = 1$

e. $(f\cdot g)(2) = f(2)\cdot g(2) = 2(1) = 2$

f. $\left(\frac{f}{g}\right)(4) = \frac{f(4)}{g(4)} = \frac{1}{-3} = -\frac{1}{3}$

32. $h(x) = -\frac{136x^2}{v^2} + 2.7x + 3.5$

a. We want $h(15) = 10$.

$$-\frac{136(15)^2}{v^2} + 2.7(15) + 3.5 = 10$$

$$-\frac{30,600}{v^2} = -34$$

$$v^2 = 900$$

$$v = 30 \text{ ft/sec}$$

The ball needs to be thrown with an initial velocity of 30 feet per second.

b. $h(x) = -\frac{126x^2}{30^2} + 2.7x + 3.5$

which simplifies to

$$h(x) = -\frac{34}{225}x^2 + 2.7x + 3.5$$

c. Using the velocity from part (b),

$$h(9) = -\frac{34}{225}(9)^2 + 2.7(9) + 3.5 = 15.56 \text{ ft}$$

The ball will be 15.56 feet above the floor when it has traveled 9 feet in front of the foul line.

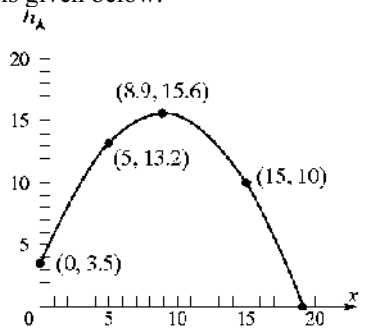
d. Select several values for x and use these to find the corresponding values for h. Use the results to form ordered pairs (x,h). Plot the points and connect with a smooth curve.

$$h(0) = -\frac{34}{225}(0)^2 + 2.7(0) + 3.5 = 3.5 \text{ ft}$$

$$h(5) = -\frac{34}{225}(5)^2 + 2.7(5) + 3.5 \approx 13.2 \text{ ft}$$

$$h(15) = -\frac{24}{225}(15)^2 + 2.7(15) + 3.5 \approx 10 \text{ ft}$$

Thus, some points on the graph are $(0,3.5)$, $(5,13.2)$, and $(15,10)$. The complete graph is given below.



33. $h(x) = -\frac{44x^2}{v^2} + x + 6$

a. $$h(8) = -\frac{44(8)^2}{28^2} + (8) + 6$$

$$= -\frac{2816}{784} + 14$$

$$\approx 10.4 \text{ feet}$$

b. $$h(12) = -\frac{44(12)^2}{28^2} + (12) + 6$$

$$= -\frac{6336}{784} + 18$$

$$\approx 9.9 \text{ feet}$$

c. From part (a) we know the point $(8,10.4)$ is on the graph and from part (b) we know the point $(12,9.9)$ is on the graph. We could evaluate the function at several more values of x (e.g. $x = 0$, $x = 15$, and $x = 20$) to obtain additional points.

$$h(0) = -\frac{44(0)^2}{28^2} + (0) + 6 = 6$$

$$h(15) = -\frac{44(15)^2}{28^2} + (15) + 6 \approx 8.4$$

$$h(20) = -\frac{44(20)^2}{28^2} + (20) + 6 \approx 3.6$$

Some additional points are $(0,6)$, $(15,8.4)$ and $(20,3.6)$. The complete graph is given

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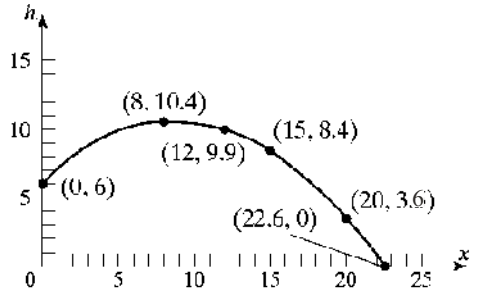
below.



d. $h(15) = -\dfrac{44(15)^2}{28^2} + (15) + 6 \approx 8.4$ feet

No; when the ball is 15 feet in front of the foul line, it will be below the hoop. Therefore it cannot go through the hoop.

In order for the ball to pass through the hoop, we need to have $h(15) = 10$.

$$10 = -\frac{44(15)^2}{v^2} + (15) + 6$$

$$-11 = -\frac{44(15)^2}{v^2}$$

$$v^2 = 4(225)$$

$$v^2 = 900$$

$$v = 30 \text{ ft/sec}$$

The ball must be shot with an initial velocity of 30 feet per second in order to go through the hoop.

34. $A(x) = 4x\sqrt{1-x^2}$

a. Domain of $A(x) = 4x\sqrt{1-x^2}$; we know that x must be greater than or equal to zero, since x represents a length. We also need $1 - x^2 \geq 0$, since this expression occurs under a square root. In fact, to avoid Area = 0, we require $x > 0$ and $1 - x^2 > 0$.

Solve: $1 - x^2 > 0$

$$(1+x)(1-x) > 0$$

Case1: $1 + x > 0$ and $1 - x > 0$

$x > -1$ and $x < 1$

(i.e. $-1 < x < 1$)

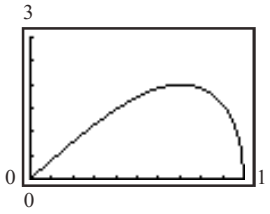
Case2: $1 + x < 0$ and $1 - x < 0$

$x < -1$ and $x > 1$

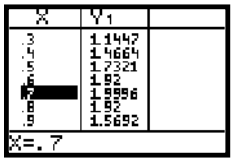
(which is impossible)

Therefore the domain of A is $\{x \mid 0 < x < 1\}$.

b. Graphing $A(x) = 4x\sqrt{1-x^2}$



c. When $x = 0.7$ feet, the cross-sectional area is maximized at approximately 1.9996 square feet. Therefore, the length of the base of the beam should be 1.4 feet in order to maximize the cross-sectional area.



35. $h(x) = \dfrac{-32x^2}{130^2} + x$

a. $h(100) = \dfrac{-32(100)^2}{130^2} + 100$

$$= \frac{-320,000}{16,900} + 100 \approx 81.07 \text{ feet}$$

b. $h(300) = \dfrac{-32(300)^2}{130^2} + 300$

$$= \frac{-2,880,000}{16,900} + 300 \approx 129.59 \text{ feet}$$

c. $h(500) = \dfrac{-32(500)^2}{130^2} + 500$

$$= \frac{-8,000,000}{16,900} + 500 \approx 26.63 \text{ feet}$$

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The ball is about 26.63 feet high after it has traveled 500 feet.

d. Solving $h(x) = \dfrac{-32x^2}{130^2} + x = 0$

$$\frac{-32x^2}{130^2} + x = 0$$

$$x\left(\frac{-32x}{130^2} + 1\right) = 0$$

$$x = 0 \quad \text{or} \quad \frac{-32x}{130^2} + 1 = 0$$

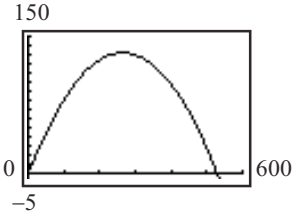
$$1 = \frac{32x}{130^2}$$

$$130^2 = 32x$$

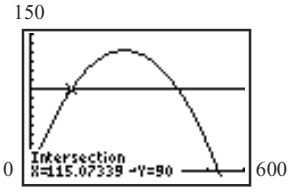
$$x = \frac{130^2}{32} = 528.13 \text{ feet}$$

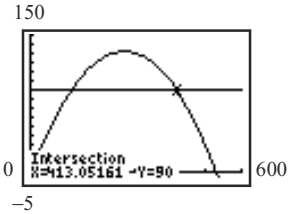
Therefore, the golf ball travels 528.13 feet.

e. $y_1 = \dfrac{-32x^2}{130^2} + x$



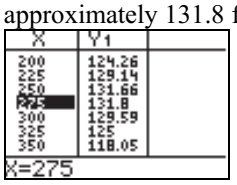
f. Use INTERSECT on the graphs of $y_1 = \dfrac{-32x^2}{130^2} + x$ and $y_2 = 90$.



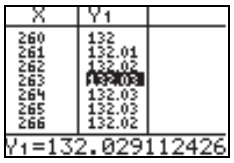


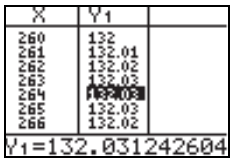
The ball reaches a height of 90 feet twice. The first time is when the ball has traveled approximately 115.07 feet, and the second time is when the ball has traveled about 413.05 feet.

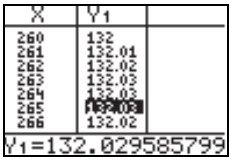
g. The ball travels approximately 275 feet before it reaches its maximum height of approximately 131.8 feet.



h. The ball travels approximately 264 feet before it reaches its maximum height of approximately 132.03 feet.







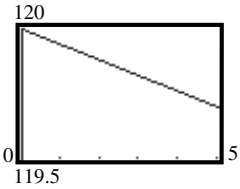
36. $W(h) = m\left(\dfrac{4000}{4000+h}\right)^2$

a. $h = 14110$ feet ≈ 2.67 miles;

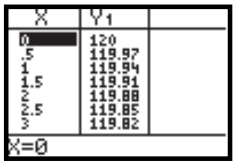
$$W(2.67) = 120\left(\frac{4000}{4000+2.67}\right)^2 \approx 119.84$$

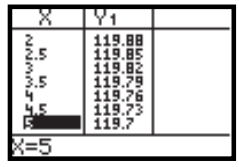
On Pike's Peak, Amy will weigh about 119.84 pounds.

b. Graphing:



c. Create a TABLE:





The weight W will vary from 120 pounds to about 119.7 pounds.

d. By refining the table, Amy will weigh 119.95 lbs at a height of about 0.83 miles

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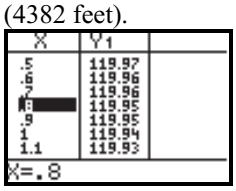
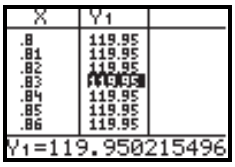
(4382 feet).



X	Y1
.5	119.97
.6	119.96
.7	119.96
.8	119.95
.9	119.95
1	119.94
1.1	119.93

X=.8



X	Y1
.8	119.95
.81	119.95
.82	119.95
.83	119.95
.84	119.95
.85	119.95
.86	119.95

Y1=119.950215496

e. Yes, 4382 feet is reasonable.

37. $C(x) = 100 + \dfrac{x}{10} + \dfrac{36000}{x}$

a. $C(480) = 100 + \dfrac{480}{10} + \dfrac{36000}{480}$

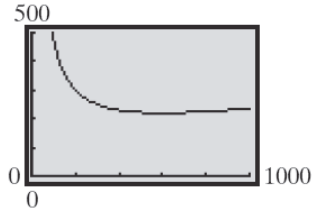
$= \$223$

$C(600) = 100 + \dfrac{600}{10} + \dfrac{36000}{600}$

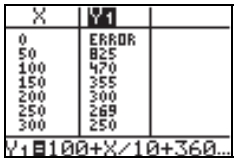
$= \$220$

b. $\{x \mid x > 0\}$

c. Graphing:



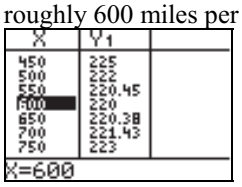
d. TblStart = 0; ΔTbl = 50



X	Y1
0	ERROR
50	825
100	470
150	355
200	300
250	269
300	250

Y1=100+X/10+360...

e. The cost per passenger is minimized to about \$220 when the ground speed is roughly 600 miles per hour.



X	Y1
450	225
500	222
550	220.45
600	220
650	220.38
700	221.43
750	223

X=600

38. **a.** $C(0) = 5000$

This represents the fixed overhead costs. That is, the company will incur costs of \$5000 per day even if no computers are manufactured.

b. $C(10) = 19{,}000$

It costs the company \$19,000 to produce 10 computers in a day.

c. $C(50) = 51{,}000$

It costs the company \$51,000 to produce 50 computers in a day.

d. The domain is $\{q \mid 0 \le q \le 80\}$. This indicates that production capacity is limited to 80 computers in a day.

e. The graph is curved down and rises slowly at first. As production increases, the graph rises more quickly and changes to being curved up.

f. The inflection point is where the graph changes from being curved down to being curved up.

39. **a.** $C(0) = \$50$

It costs \$50 if you use 0 gigabytes.

b. $C(5) = \$50$

It costs \$50 if you use 5 gigabytes.

c. $C(15) = \$150$

It costs \$90 if you use 15 gigabytes.

d. The domain is $\{g \mid 0 \le g \le 30\}$. This indicates that there are at most 30 gigabytes in a month.

e. The graph is flat at first and then rises in a straight line.

40. $g(-2) = 5 = f(-2) = 4$

Since $f(-2) = (-2)^2 - 4(-2) + c$

$= 12 + c$

we have

$\dfrac{12+c}{3} - 4 = 5$

$\dfrac{12+c}{3} = 9$

$12 + c = 27$

$c = 15$

$f(3) = 3^2 - 4 \cdot 3 + 15 = 12$

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41. $g(5) = 5^2 + n = 25 + n$

$f(g(5)) = f(25+n) = \sqrt{25+n} + 2 = 4$

so, $\sqrt{25+n} = 2$

$25 + n = 4$

$n = -21$

$g(n) = n^2 + n = (-21)^2 + (-21) = 420$ **.**

42. Answers will vary. From a graph, the domain can be found by visually locating the x-values for which the graph is defined. The range can be found in a similar fashion by visually locating the y-values for which the function is defined.

If an equation is given, the domain can be found by locating any restricted values and removing them from the set of real numbers. The range can be found by using known properties of the graph of the equation, or estimated by means of a table of values.

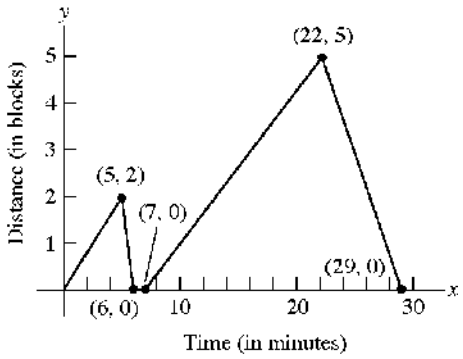
43. The graph of a function can have any number of x-intercepts. The graph of a function can have at most one y-intercept (otherwise the graph would fail the vertical line test).

44. Yes, the graph of a single point is the graph of a function since it would pass the vertical line test. The equation of such a function would be something like the following: $f(x) = 2$, where $x = 7$.

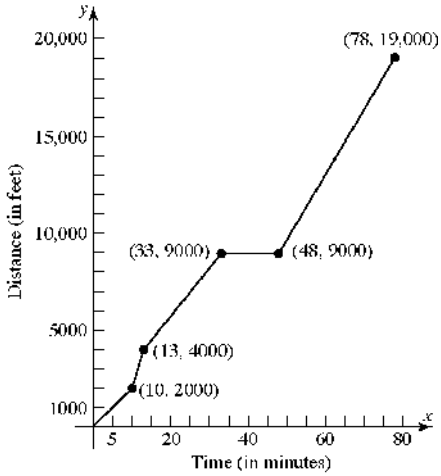
45. (a) III; (b) IV; (c) I; (d) V; (e) II

46. (a) II; (b) V; (c) IV; (d) III; (e) I

47.



48.



49. **a.** 2 hours elapsed; Kevin was between 0 and 3 miles from home.

b. 0.5 hours elapsed; Kevin was 3 miles from home.

c. 0.3 hours elapsed; Kevin was between 0 and 3 miles from home.

d. 0.2 hours elapsed; Kevin was at home.

e. 0.9 hours elapsed; Kevin was between 0 and 2.8 miles from home.

f. 0.3 hours elapsed; Kevin was 2.8 miles from home.

g. 1.1 hours elapsed; Kevin was between 0 and 2.8 miles from home.

h. The farthest distance Kevin is from home is 3 miles.

i. Kevin returned home 2 times.

50. **a.** Michael travels fastest between 7 and 7.4 minutes. That is, $(7, 7.4)$.

b. Michael's speed is zero between 4.2 and 6 minutes. That is, $(4.2, 6)$.

c. Between 0 and 2 minutes, Michael's speed increased from 0 to 30 miles/hour.

d. Between 4.2 and 6 minutes, Michael was stopped (i.e, his speed was 0 miles/hour).

e. Between 7 and 7.4 minutes, Michael was traveling at a steady rate of 50 miles/hour.

f. Michael's speed is constant between 2 and 4 minutes, between 4.2 and 6 minutes, between 7 and 7.4 minutes, and between 7.6 and 8 minutes. That is, on the intervals (2, 4), (4.2, 6), (7, 7.4), and (7.6, 8).

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51. Answers (graphs) will vary. Points of the form $(5, y)$ and of the form $(x, 0)$ cannot be on the graph of the function.

52. The only such function is $f(x) = 0$ because it is the only function for which $f(x) = -f(x)$. Any other such graph would fail the vertical line test.

53. Answers may vary.

54. $f(x-2) = -(x-2)^2 + (x-2) - 3$
$= -(x^2 - 4x + 4) + x - 2 - 3$
$= -x^2 + 5x - 9$

55. $d = \sqrt{(1-3)^2 + (0-(-6))^2}$
$= \sqrt{(-2)^2 + (-6)^2}$
$= \sqrt{4+36} = \sqrt{40} = 2\sqrt{10}$

56. $y - 4 = \frac{2}{3}(x - (-6))$
$y - 4 = \frac{2}{3}x + 4$
$y = \frac{2}{3}x + 8$

57. Since the function contains a cube root then the domain is:

$(-\infty, \infty)$

58. $\left[\frac{1}{2}(-12)\right]^2 = 36$

59. $\frac{\sqrt{x}-\sqrt{6}}{x-6} \cdot \frac{\sqrt{x}+\sqrt{6}}{\sqrt{x}+\sqrt{6}} =$
$\frac{x-6}{(x-6)(\sqrt{x}+\sqrt{6})} = \frac{1}{\sqrt{x}+\sqrt{6}}$

60. The car traveling north travels a distance or 25t and the car traveling west travels a distance of 35t where t is the time of travel. Using the Pythagorean we have:
$40^2 = (35t)^2 + (25t)^2$
$1600 = 1225t^2 + 625t^2$
$1600 = 1850t^2$
$t^2 = 0.8649$
$t = 0.93$ hours
Converting to minutes we have
$0.93(60) = 55.8$ minutes

61. $3x + 4 \le 7$ and $5 - 2x < 13$
$3x \le 3$ $\quad -2x < 8$
$x \le 1$ $\quad x > -4$

The solution set is $(-4, 1]$.

62. $(5x^2 - 7x + 2) - (8x - 10)$
$= 5x^2 - 7x + 2 - 8x + 10$
$= 5x^2 - 15x + 12$

63. $[-3, 10]$

Section 2.3

1. $2 < x < 5$

2. slope $= \frac{\Delta y}{\Delta x} = \frac{8-3}{3-(-2)} = \frac{5}{5} = 1$

3. x-axis: $y \to -y$
$(-y) = 5x^2 - 1$
$-y = 5x^2 - 1$
$y = -5x^2 + 1$ different

y-axis: $x \to -x$
$y = 5(-x)^2 - 1$
$y = 5x^2 - 1$ same

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origin: $x \to -x$ and $y \to -y$

$(-y) = 5(-x)^2 - 1$

$-y = 5x^2 - 1$

$y = -5x^2 + 1$ different

The equation has symmetry with respect to the y-axis only.

4. $y - y_1 = m(x - x_1)$

$y - (-2) = 5(x - 3)$

$y + 2 = 5(x - 3)$

5. $y = x^2 - 9$

x-intercepts:

$0 = x^2 - 9$

$x^2 = 9 \to x = \pm 3$

y-intercept:

$y = (0)^2 - 9 = -9$

The intercepts are $(-3, 0)$, $(3, 0)$, and $(0, -9)$.

6. increasing

7. even; odd

8. True

9. True

10. False; odd functions are symmetric with respect to the origin. Even functions are symmetric with respect to the y-axis.

11. c

12. d

13. Yes

14. No, it is increasing.

15. No

16. Yes

17. f is increasing on the intervals $[-8, -2], [0, 2], [5, 7]$.

18. f is decreasing on the intervals: $[-10, -8], [-2, 0], [2, 5]$.

19. Yes. The local maximum at $x = 2$ is 10.

20. No. There is a local minimum at $x = 5$; the local minimum is 0.

21. f has local maxima at $x = -2$ and $x = 2$. The local maxima are 6 and 10, respectively.

22. f has local minima at $x = -8$, $x = 0$ and $x = 5$. The local minima are –4, 0, and 0, respectively.

23. f has absolute minimum of -4 at $x = -8$.

24. f has absolute maximum of 10 at $x = 2$.

25. **a.** Intercepts: (–2, 0), (2, 0), and (0, 3).

b. Domain: $\{x \mid -4 \le x \le 4\}$ or $[-4, 4]$;

Range: $\{y \mid 0 \le y \le 3\}$ or $[0, 3]$.

c. Increasing: [–2, 0] and [2, 4];
Decreasing: [–4, –2] and [0, 2].

d. Since the graph is symmetric with respect to the y-axis, the function is <u>even</u>.

26. **a.** Intercepts: (–1, 0), (1, 0), and (0, 2).

b. Domain: $\{x \mid -3 \le x \le 3\}$ or $[-3, 3]$;

Range: $\{y \mid 0 \le y \le 3\}$ or $[0, 3]$.

c. Increasing: [–1, 0] and [1, 3];
Decreasing: [–3, –1] and [0, 1].

d. Since the graph is symmetric with respect to the y-axis, the function is <u>even</u>.

27. **a.** Intercepts: (0, 1).

b. Domain: $\{x \mid x \text{ is any real number}\}$;

Range: $\{y \mid y > 0\}$ or $(0, \infty)$.

c. Increasing: $(-\infty, \infty)$; Decreasing: never.

d. Since the graph is not symmetric with respect to the y-axis or the origin, the function is <u>neither</u> even nor odd.

28. **a.** Intercepts: (1, 0).

b. Domain: $\{x \mid x > 0\}$ or $(0, \infty)$;

Range: $\{y \mid y \text{ is any real number}\}$.

c. Increasing: $[0, \infty)$; Decreasing: never.

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d. Since the graph is not symmetric with respect to the y-axis or the origin, the function is neither even nor odd.

29. a. Intercepts: $(-\pi, 0), (\pi, 0),$ and $(0, 0)$.

b. Domain: $\{x \mid -\pi \le x \le \pi\}$ or $[-\pi, \pi]$;
Range: $\{y \mid -1 \le y \le 1\}$ or $[-1, 1]$.

c. Increasing: $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$;
Decreasing: $\left[-\pi, -\frac{\pi}{2}\right]$ and $\left[\frac{\pi}{2}, \pi\right]$.

d. Since the graph is symmetric with respect to the origin, the function is odd.

30. a. Intercepts: $\left(-\frac{\pi}{2}, 0\right), \left(\frac{\pi}{2}, 0\right),$ and $(0, 1)$.

b. Domain: $\{x \mid -\pi \le x \le \pi\}$ or $[-\pi, \pi]$;
Range: $\{y \mid -1 \le y \le 1\}$ or $[-1, 1]$.

c. Increasing: $[-\pi, 0]$; Decreasing: $[0, \pi]$.

d. Since the graph is symmetric with respect to the y-axis, the function is even.

31. a. Intercepts: $\left(\frac{1}{3}, 0\right), \left(\frac{5}{2}, 0\right),$ and $\left(0, \frac{1}{2}\right)$.

b. Domain: $\{x \mid -3 \le x \le 3\}$ or $[-3, 3]$;
Range: $\{y \mid -1 \le y \le 2\}$ or $[-1, 2]$.

c. Increasing: $[2, 3]$; Decreasing: $[-1, 1]$;
Constant: $[-3, -1]$ and $[1, 2]$

d. Since the graph is not symmetric with respect to the y-axis or the origin, the function is neither even nor odd.

32. a. Intercepts: $(-2.3, 0), (3, 0),$ and $(0, 1)$.

b. Domain: $\{x \mid -3 \le x \le 3\}$ or $[-3, 3]$;
Range: $\{y \mid -2 \le y \le 2\}$ or $[-2, 2]$.

c. Increasing: $[-3, -2]$ and $[0, 2]$;
Decreasing: $[2, 3]$; Constant: $[-2, 0]$.

d. Since the graph is not symmetric with respect to the y-axis or the origin, the function is neither even nor odd.

33. a. f has a local maximum value of 3 at $x = 0$.

b. f has a local minimum value of 0 at both $x = -2$ and $x = 2$.

34. a. f has a local maximum value of 2 at $x = 0$.

b. f has a local minimum value of 0 at both $x = -1$ and $x = 1$.

35. a. f has a local maximum value of 1 at $x = \frac{\pi}{2}$.

b. f has a local minimum value of -1 at $x = -\frac{\pi}{2}$.

36. a. f has a local maximum value of 1 at $x = 0$.

b. f has a local minimum value of -1 both at $x = -\pi$ and $x = \pi$.

37. $f(x) = 4x^3$
$f(-x) = 4(-x)^3 = -4x^3 = -f(x)$
Therefore, f is odd.

38. $f(x) = 2x^4 - x^2$
$f(-x) = 2(-x)^4 - (-x)^2 = 2x^4 - x^2 = f(x)$
Therefore, f is even.

39. $g(x) = 10 - x^2$
$g(-x) = 10 - (-x)^2 = 10 - x^2 = g(x)$
Therefore, g is even.

40. $h(x) = 3x^3 + 5$
$h(-x) = 3(-x)^3 + 5 = -3x^3 + 5$
h is neither even nor odd.

41. $F(x) = \sqrt[3]{4x}$
$F(-x) = \sqrt[3]{-4x} = -\sqrt[3]{4x} = -F(x)$
Therefore, F is odd.

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42. $G(x) = \sqrt{x}$

$G(-x) = \sqrt{-x}$

G is neither even nor odd.

43. $f(x) = x + |x|$

$f(-x) = -x + |-x| = -x + |x|$

f is neither even nor odd.

44. $f(x) = \sqrt[3]{2x^2 + 1}$

$f(-x) = \sqrt[3]{2(-x)^2 + 1} = \sqrt[3]{2x^2 + 1} = f(x)$

Therefore, f is even.

45. $g(x) = \dfrac{1}{x^2 + 8}$

$g(-x) = \dfrac{1}{(-x)^2 + 8} = \dfrac{1}{x^2 + 8} = g(x)$

Therefore, g is even.

46. $h(x) = \dfrac{x}{x^2 - 1}$

$h(-x) = \dfrac{-x}{(-x)^2 - 1} = \dfrac{-x}{x^2 - 1} = -h(x)$

Therefore, h is odd.

47. $h(x) = \dfrac{-x^3}{3x^2 - 9}$

$h(-x) = \dfrac{-(-x)^3}{3(-x)^2 - 9} = \dfrac{x^3}{3x^2 - 9} = -h(x)$

Therefore, h is odd.

48. $F(x) = \dfrac{2x}{|x|}$

$F(-x) = \dfrac{2(-x)}{|-x|} = \dfrac{-2x}{|x|} = -F(x)$

Therefore, F is odd.

49. f has an absolute maximum of 4 at $x = 1$.
f has an absolute minimum of 1 at $x = 5$.
f has an local maximum value of 3 at $x = 3$.
f has an local minimum value of 2 at $x = 2$.

50. f has an absolute maximum of 4 at $x = 4$.
f has an absolute minimum of 0 at $x = 5$.
f has an local maximum value of 4 at $x = 4$.
f has an local minimum value of 1 at $x = 1$.

51. f has an absolute minimum of 1 at $x = 1$.
f has an absolute maximum of 4 at $x = 3$.
f has an local minimum value of 1 at $x = 1$.
f has an local maximum value of 4 at $x = 3$.

52. f has an absolute minimum of 1 at $x = 0$.
f has no absolute maximum.
f has no local minimum.
f has no local maximum.

53. f has an absolute minimum of 0 at $x = 0$.
f has no absolute maximum.
f has an local minimum value of 0 at $x = 0$.
f has an local minimum value of 2 at $x = 3$.
f has an local maximum value of 3 at $x = 2$.

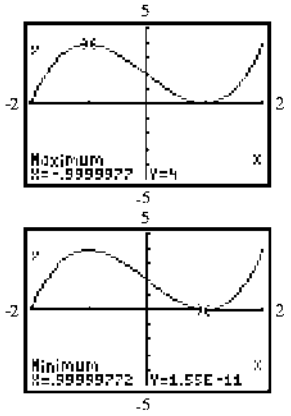
54. f has an absolute maximum of 4 at $x = 2$.
f has no absolute minimum.
f has an local maximum value of 4 at $x = 2$.
f has an local minimum value of 2 at $x = 0$.

55. f has no absolute maximum or minimum.
f has no local maximum or minimum.

56. f has no absolute maximum or minimum.
f has no local maximum or minimum.

57. $f(x) = x^3 - 3x + 2$ on the interval $(-2, 2)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = x^3 - 3x + 2$.



local maximum: $f(-1) = 4$

local minimum: $f(1) = 0$

f is increasing on: $[-2, -1]$ and $[1, 2]$;

f is decreasing on: $[-1, 1]$

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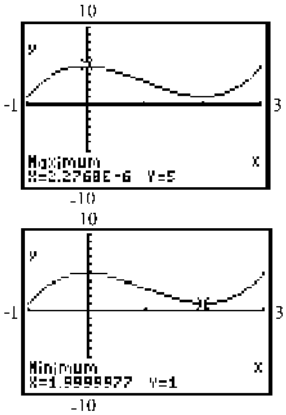
58. $f(x) = x^3 - 3x^2 + 5$ on the interval $(-1, 3)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = x^3 - 3x^2 + 5$.



local maximum: $f(0) = 5$

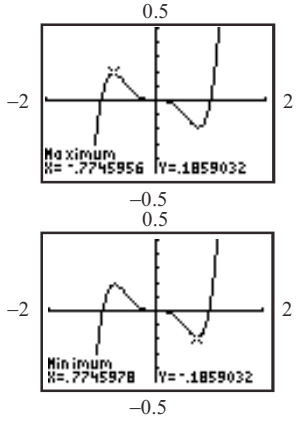
local minimum: $f(2) = 1$

f is increasing on: $[-1, 0]$ and $[2, 3]$;

f is decreasing on: $[0, 2]$

59. $f(x) = x^5 - x^3$ on the interval $(-2, 2)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = x^5 - x^3$.



local maximum: $f(-0.77) = 0.19$

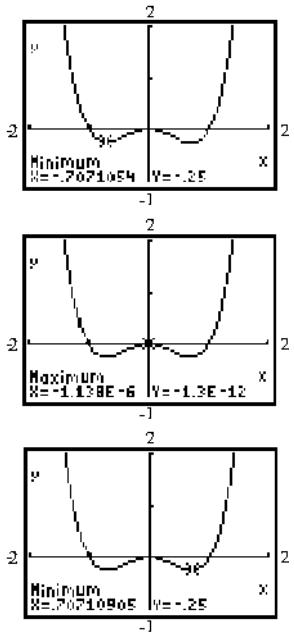
local minimum: $f(0.77) = -0.19$

f is increasing on: $[-2, -0.77]$ and $[0.77, 2]$;

f is decreasing on: $[-0.77, 0.77]$

60. $f(x) = x^4 - x^2$ on the interval $(-2, 2)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = x^4 - x^2$.



local maximum: $f(0) = 0$

local minimum:

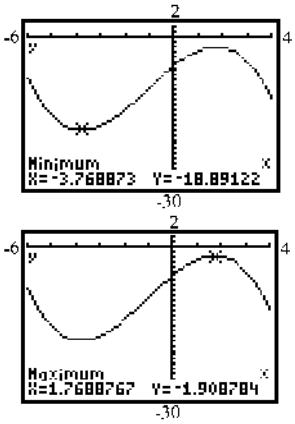
$f(-0.71) = -0.25$; $f(0.71) = -0.25$

f is increasing on: $[-0.71, 0]$ and $[0.71, 2]$;

f is decreasing on: $[-2, -0.71]$ and $[0, 0.71]$

61. $f(x) = -0.2x^3 - 0.6x^2 + 4x - 6$ on the interval $(-6, 4)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = -0.2x^3 - 0.6x^2 + 4x - 6$.



local maximum: $f(1.77) = -1.91$

local minimum: $f(-3.77) = -18.89$

f is increasing on: $[-3.77, 1.77]$;

f is decreasing on: $[-6, -3.77]$ and $[1.77, 4]$

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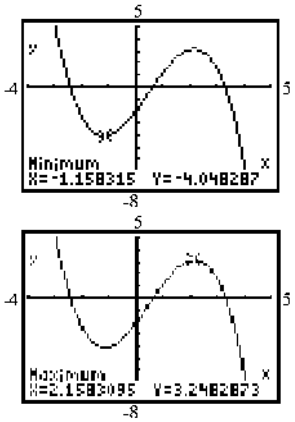
62. $f(x) = -0.4x^3 + 0.6x^2 + 3x - 2$ on the interval $(-4, 5)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = -0.4x^3 + 0.6x^2 + 3x - 2$.



local maximum: $f(2.16) = 3.25$

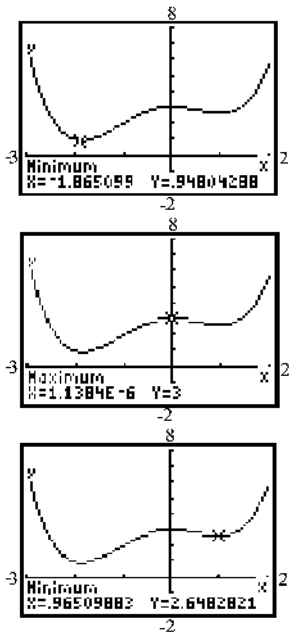
local minimum: $f(-1.16) = -4.05$

f is increasing on: $[-1.16, 2.16]$;

f is decreasing on: $[-4, -1.16]$ and $[2.16, 5]$

63. $f(x) = 0.25x^4 + 0.3x^3 - 0.9x^2 + 3$ on the interval $(-3, 2)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = 0.25x^4 + 0.3x^3 - 0.9x^2 + 3$.



local maximum: $f(0) = 3$

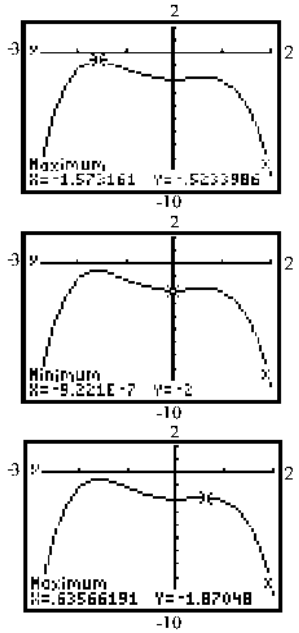
local minimum: $f(-1.87) = 0.95$, $f(0.97) = 2.65$

f is increasing on: $[-1.87, 0]$ and $[0.97, 2]$;

f is decreasing on: $[-3, -1.87]$ and $[0, 0.97]$

64. $f(x) = -0.4x^4 - 0.5x^3 + 0.8x^2 - 2$ on the interval $(-3, 2)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = -0.4x^4 - 0.5x^3 + 0.8x^2 - 2$.



local maxima: $f(-1.57) = -0.52$, $f(0.64) = -1.87$

local minimum: $(0, -2)$ $f(0) = -2$

f is increasing on: $[-3, -1.57]$ and $[0, 0.64]$;

f is decreasing on: $[-1.57, 0]$ and $[0.64, 2]$

65. $f(x) = -2x^2 + 4$

a. Average rate of change of f from $x = 0$ to $x = 2$

$$\frac{f(2) - f(0)}{2 - 0} = \frac{\left(-2(2)^2 + 4\right) - \left(-2(0)^2 + 4\right)}{2}$$

$$= \frac{(-4) - (4)}{2} = \frac{-8}{2} = -4$$

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b. Average rate of change of f from $x = 1$ to $x = 3$:

$$\frac{f(3)-f(1)}{3-1} = \frac{\left(-2(3)^2+4\right)-\left(-2(1)^2+4\right)}{2}$$
$$= \frac{(-14)-(2)}{2} = \frac{-16}{2} = -8$$

c. Average rate of change of f from $x = 1$ to $x = 4$:

$$\frac{f(4)-f(1)}{4-1} = \frac{\left(-2(4)^2+4\right)-\left(-2(1)^2+4\right)}{3}$$
$$= \frac{(-28)-(2)}{3} = \frac{-30}{3} = -10$$

66. $f(x) = -x^3 + 1$

a. Average rate of change of f from $x = 0$ to $x = 2$:

$$\frac{f(2)-f(0)}{2-0} = \frac{\left(-(2)^3+1\right)-\left(-(0)^3+1\right)}{2}$$
$$= \frac{-7-1}{2} = \frac{-8}{2} = -4$$

b. Average rate of change of f from $x = 1$ to $x = 3$:

$$\frac{f(3)-f(1)}{3-1} = \frac{\left(-(3)^3+1\right)-\left(-(1)^3+1\right)}{2}$$
$$= \frac{-26-(0)}{2} = \frac{-26}{2} = -13$$

c. Average rate of change of f from $x = -1$ to $x = 1$:

$$\frac{f(1)-f(-1)}{1-(-1)} = \frac{\left(-(1)^3+1\right)-\left(-(-1)^3+1\right)}{2}$$
$$= \frac{0-2}{2} = \frac{-2}{2} = -1$$

67. $g(x) = x^3 - 4x + 7$

a. Average rate of change of g from $x = -3$ to $x = -2$:

$$\frac{g(-2)-g(-3)}{-2-(-3)}$$
$$= \frac{\left[(-2)^3-4(-2)+7\right]-\left[(-3)^3-4(-3)+7\right]}{1}$$
$$= \frac{(7)-(-8)}{1} = \frac{15}{1} = 15$$

b. Average rate of change of g from $x = -1$ to $x = 1$:

$$\frac{g(1)-g(-1)}{1-(-1)}$$
$$= \frac{\left[(1)^3-4(1)+7\right]-\left[(-1)^3-4(-1)+7\right]}{2}$$
$$= \frac{(4)-(10)}{2} = \frac{-6}{2} = -3$$

c. Average rate of change of g from $x = 1$ to $x = 3$:

$$\frac{g(3)-g(1)}{3-1}$$
$$= \frac{\left[(3)^3-4(3)+7\right]-\left[(1)^3-4(1)+7\right]}{2}$$
$$= \frac{(22)-(4)}{2} = \frac{18}{2} = 9$$

68. $h(x) = x^2 - 2x + 3$

a. Average rate of change of h from $x = -1$ to $x = 1$:

$$\frac{h(1)-h(-1)}{1-(-1)}$$
$$= \frac{\left[(1)^2-2(1)+3\right]-\left[(-1)^2-2(-1)+3\right]}{2}$$
$$= \frac{(2)-(6)}{2} = \frac{-4}{2} = -2$$

b. Average rate of change of h from $x = 0$ to $x = 2$:

$$\frac{h(2)-h(0)}{2-0}$$
$$= \frac{\left[(2)^2-2(2)+3\right]-\left[(0)^2-2(0)+3\right]}{2}$$
$$= \frac{(3)-(3)}{2} = \frac{0}{2} = 0$$

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c. Average rate of change of h from $x=2$ to $x=5$:

$$\frac{h(5)-h(2)}{5-2}$$
$$=\frac{\left[(5)^2-2(5)+3\right]-\left[(2)^2-2(2)+3\right]}{3}$$
$$=\frac{(18)-(3)}{3}=\frac{15}{3}=5$$

69. $f(x)=5x-2$

a. Average rate of change of f from 1 to 3:

$$\frac{\Delta y}{\Delta x}=\frac{f(3)-f(1)}{3-1}=\frac{13-3}{3-1}=\frac{10}{2}=5$$

Thus, the average rate of change of f from 1 to 3 is 5.

b. From (a), the slope of the secant line joining $(1, f(1))$ and $(3, f(3))$ is 5. We use the point-slope form to find the equation of the secant line:

$$y-y_1=m_{\text{sec}}(x-x_1)$$
$$y-3=5(x-1)$$
$$y-3=5x-5$$
$$y=5x-2$$

70. $f(x)=-4x+1$

a. Average rate of change of f from 2 to 5:

$$\frac{\Delta y}{\Delta x}=\frac{f(5)-f(2)}{5-2}=\frac{-19-(-7)}{5-2}$$
$$=\frac{-12}{3}=-4$$

Therefore, the average rate of change of f from 2 to 5 is -4.

b. From (a), the slope of the secant line joining $(2, f(2))$ and $(5, f(5))$ is -4. We use the point-slope form to find the equation of the secant line:

$$y-y_1=m_{\text{sec}}(x-x_1)$$
$$y-(-7)=-4(x-2)$$
$$y+7=-4x+8$$
$$y=-4x+1$$

71. $g(x)=x^2-2$

a. Average rate of change of g from -2 to 1:

$$\frac{\Delta y}{\Delta x}=\frac{g(1)-g(-2)}{1-(-2)}=\frac{-1-2}{1-(-2)}=\frac{-3}{3}=-1$$

Therefore, the average rate of change of g from -2 to 1 is -1.

b. From (a), the slope of the secant line joining $(-2, g(-2))$ and $(1, g(1))$ is -1. We use the point-slope form to find the equation of the secant line:

$$y-y_1=m_{\text{sec}}(x-x_1)$$
$$y-2=-1(x-(-2))$$
$$y-2=-x-2$$
$$y=-x$$

72. $g(x)=x^2+1$

a. Average rate of change of g from -1 to 2:

$$\frac{\Delta y}{\Delta x}=\frac{g(2)-g(-1)}{2-(-1)}=\frac{5-2}{2-(-1)}=\frac{3}{3}=1$$

Therefore, the average rate of change of g from -1 to 2 is 1.

b. From (a), the slope of the secant line joining $(-1, g(-1))$ and $(2, g(2))$ is 1. We use the point-slope form to find the equation of the secant line:

$$y-y_1=m_{\text{sec}}(x-x_1)$$
$$y-2=1(x-(-1))$$
$$y-2=x+1$$
$$y=x+3$$

73. $h(x)=x^2-2x$

a. Average rate of change of h from 2 to 4:

$$\frac{\Delta y}{\Delta x}=\frac{h(4)-h(2)}{4-2}=\frac{8-0}{4-2}=\frac{8}{2}=4$$

Therefore, the average rate of change of h from 2 to 4 is 4.

b. From (a), the slope of the secant line joining $(2, h(2))$ and $(4, h(4))$ is 4. We use the point-slope form to find the equation of the secant line:

$$y-y_1=m_{\text{sec}}(x-x_1)$$
$$y-0=4(x-2)$$
$$y=4x-8$$

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74. $h(x) = -2x^2 + x$

a. Average rate of change from 0 to 3:

$$\frac{\Delta y}{\Delta x} = \frac{h(3) - h(0)}{3 - 0} = \frac{-15 - 0}{3 - 0}$$
$$= \frac{-15}{3} = -5$$

Therefore, the average rate of change of h from 0 to 3 is -5.

b. From (a), the slope of the secant line joining $(0, h(0))$ and $(3, h(3))$ is -5. We use the point-slope form to find the equation of the secant line:

$$y - y_1 = m_{\text{sec}}(x - x_1)$$
$$y - 0 = -5(x - 0)$$
$$y = -5x$$

75. **a.** $g(x) = x^3 - 27x$

$$g(-x) = (-x)^3 - 27(-x)$$
$$= -x^3 + 27x$$
$$= -(x^3 - 27x)$$
$$= -g(x)$$

Since $g(-x) = -g(x)$, the function is odd.

b. Since $g(x)$ is odd then it is symmetric about the origin so there exist a local maximum at $x = -3$.

$$g(-3) = (-3)^3 - 27(-3) = -27 + 81 = 54$$

So there is a local maximum of 54 at $x = -3$.

76. $f(x) = -x^3 + 12x$

a. $f(-x) = -(-x)^3 + 12(-x)$
$$= x^3 - 12x$$
$$= -(-x^3 + 12x)$$
$$= -f(x)$$

Since $f(-x) = -f(x)$, the function is odd.

b. Since $f(x)$ is odd then it is symmetric about the origin so there exist a local maximum at $x = -3$.

$$f(-2) = -(-2)^3 + 12(-2) = 8 - 24 = -16$$

So there is a local minimum value of -16 at $x = -2$.

77. $F(x) = -x^4 + 8x^2 + 9$

a. $F(-x) = -(-x)^4 + 8(-x)^2 + 9$
$$= -x^4 + 8x + 9$$
$$= F(x)$$

Since $F(-x) = F(x)$, the function is even.

b. Since the function is even, its graph has y-axis symmetry. The second local maximum value is 25 and occurs at $x = -2$.

c. Because the graph has y-axis symmetry, the area under the graph between $x = 0$ and $x = 3$ bounded below by the x-axis is the same as the area under the graph between $x = -3$ and $x = 0$ bounded below the x-axis. Thus, the area is 50.4 square units.

78. $G(x) = -x^4 + 32x^2 + 144$

a. $G(-x) = -(-x)^4 + 32(-x)^2 + 144$
$$= -x^4 + 32x^2 + 144$$
$$= G(x)$$

Since $G(-x) = G(x)$, the function is even.

b. Since the function is even, its graph has y-axis symmetry. The second local maximum is in quadrant II and is 400 and occurs at $x = -4$.

c. Because the graph has y-axis symmetry, the area under the graph between $x = 0$ and $x = 6$ bounded below by the x-axis is the same as the area under the graph between $x = -6$ and $x = 0$ bounded below the x-axis. Thus, the area is 1612.8 square units.

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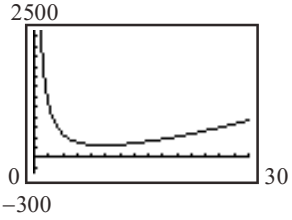
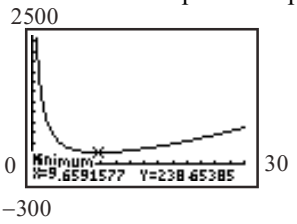
79. $\overline{C}(x) = 0.3x^2 + 21x - 251 + \dfrac{2500}{x}$

a. $y_1 = 0.3x^2 + 21x - 251 + \dfrac{2500}{x}$



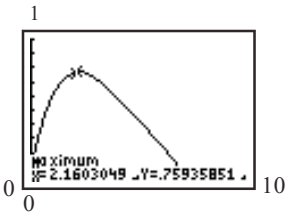
b. Use MINIMUM. Rounding to the nearest whole number, the average cost is minimized when approximately 10 lawnmowers are produced per hour.



c. The minimum average cost is approximately \$239 per mower.

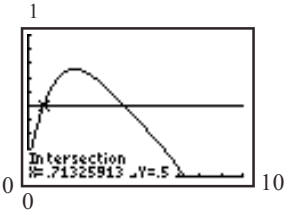
80. a. $C(t) = -.002t^4 + .039t^3 - .285t^2 + .766t + .085$

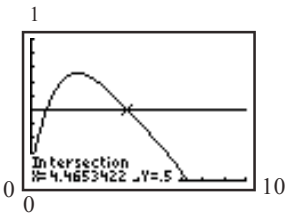
Graph the function on a graphing utility and use the Maximum option from the CALC menu.



The concentration will be highest after about 2.16 hours.

b. Enter the function in Y1 and 0.5 in Y2. Graph the two equations in the same window and use the Intersect option from the CALC menu.





After taking the medication, the woman can feed her child within the first 0.71 hours (about 42 minutes) or after 4.47 hours (about 4hours 28 minutes) have elapsed.

81. a. avg. rate of change $= \dfrac{P(2.5) - P(0)}{2.5 - 0}$

$= \dfrac{0.18 - 0.09}{2.5 - 0}$

$= \dfrac{0.09}{2.5}$

$= 0.036$ gram per hour

On average, the population is increasing at a rate of 0.036 gram per hour from 0 to 2.5 hours.

b. avg. rate of change $= \dfrac{P(6) - P(4.5)}{6 - 4.5}$

$= \dfrac{0.50 - 0.35}{6 - 4.5}$

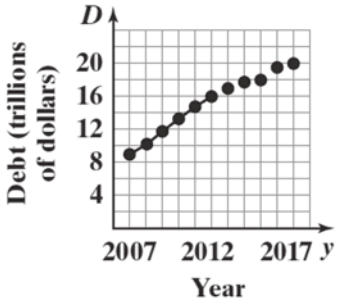
$= \dfrac{0.15}{1.5}$

$= 0.1$ gram per hour

On average, the population is increasing at a rate of 0.1 gram per hour from 4.5 to 6 hours.

c. The average rate of change is increasing as time passes. This indicates that the population is increasing at an increasing rate.

82. a.



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b. The slope represents the average rate of change of the debt from 2007 to 2012.

c. $$\text{avg. rate of change} = \frac{P(2010)-P(2008)}{2010-2008} = \frac{13562-10025}{2} = \frac{3537}{2} = \$\ 1{,}768.5 \text{ billion/yr}$$

d. $$\text{avg. rate of change} = \frac{P(2013)-P(2011)}{2013-2011} = \frac{16738-14790}{2} = \frac{1948}{2} = \$\ 974 \text{ billion/yr}$$

e. $$\text{avg. rate of change} = \frac{P(2016)-P(2014)}{2016-2014} = \frac{19573-17824}{2} = \frac{1749}{2} = \$\ 874.5 \text{ billion}$$

f. The average rate of change is decreasing as time passes.

83. $f(x)=x^2$

a. Average rate of change of f from $x=0$ to $x=1$:

$$\frac{f(1)-f(0)}{1-0} = \frac{1^2-0^2}{1} = \frac{1}{1} = 1$$

b. Average rate of change of f from $x=0$ to $x=0.5$:

$$\frac{f(0.5)-f(0)}{0.5-0} = \frac{(0.5)^2-0^2}{0.5} = \frac{0.25}{0.5} = 0.5$$

c. Average rate of change of f from $x=0$ to $x=0.1$:

$$\frac{f(0.1)-f(0)}{0.1-0} = \frac{(0.1)^2-0^2}{0.1} = \frac{0.01}{0.1} = 0.1$$

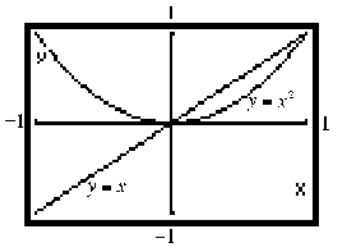
d. Average rate of change of f from $x=0$ to $x=0.01$:

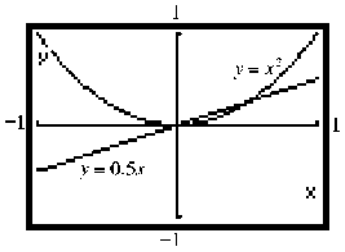
$$\frac{f(0.01)-f(0)}{0.01-0} = \frac{(0.01)^2-0^2}{0.01} = \frac{0.0001}{0.01} = 0.01$$

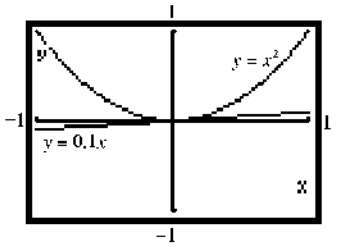
e. Average rate of change of f from $x=0$ to $x=0.001$:

$$\frac{f(0.001)-f(0)}{0.001-0} = \frac{(0.001)^2-0^2}{0.001} = \frac{0.000001}{0.001} = 0.001$$

f. Graphing the secant lines:







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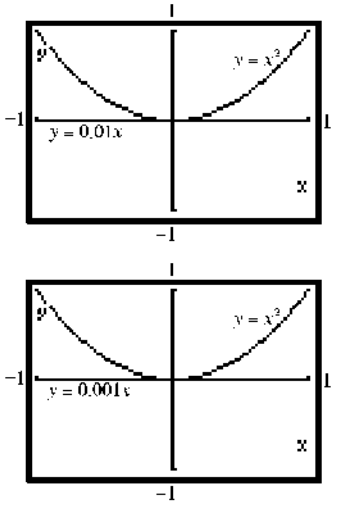


g. The secant lines are beginning to look more and more like the tangent line to the graph of f at the point where $x = 0$.

h. The slopes of the secant lines are getting smaller and smaller. They seem to be approaching the number zero.

84. $f(x) = x^2$

a. Average rate of change of f from $x = 1$ to $x = 2$:

$$\frac{f(2) - f(1)}{2 - 1} = \frac{2^2 - 1^2}{1} = \frac{3}{1} = 3$$

b. Average rate of change of f from $x = 1$ to $x = 1.5$:

$$\frac{f(1.5) - f(1)}{1.5 - 1} = \frac{(1.5)^2 - 1^2}{0.5} = \frac{1.25}{0.5} = 2.5$$

c. Average rate of change of f from $x = 1$ to $x = 1.1$:

$$\frac{f(1.1) - f(1)}{1.1 - 1} = \frac{(1.1)^2 - 1^2}{0.1} = \frac{0.21}{0.1} = 2.1$$

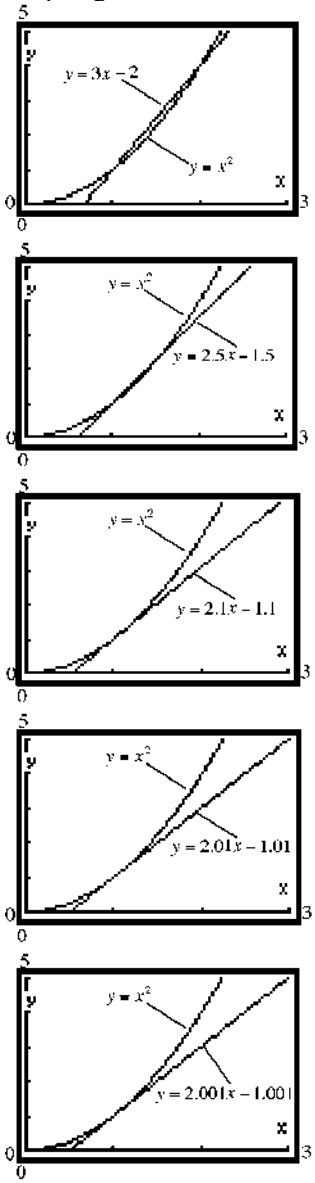
d. Average rate of change of f from $x = 1$ to $x = 1.01$:

$$\frac{f(1.01) - f(1)}{1.01 - 1} = \frac{(1.01)^2 - 1^2}{0.01} = \frac{0.0201}{0.01} = 2.01$$

e. Average rate of change of f from $x = 1$ to $x = 1.001$:

$$\frac{f(1.001) - f(1)}{1.001 - 1} = \frac{(1.001)^2 - 1^2}{0.001} = \frac{0.002001}{0.001} = 2.001$$

f. Graphing the secant lines:



g. The secant lines are beginning to look more and more like the tangent line to the graph of f at the point where $x = 1$.

h. The slopes of the secant lines are getting smaller and smaller. They seem to be approaching the number 2.

85. $f(x) = 2x + 5$

a. $m_{\text{sec}} = \dfrac{f(x+h) - f(x)}{h}$

$$= \frac{2(x+h) + 5 - 2x - 5}{h} = \frac{2h}{h} = 2$$

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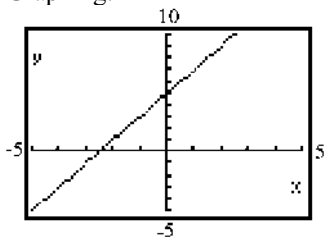
b. When $x = 1$:
$h = 0.5 \Rightarrow m_{\text{sec}} = 2$
$h = 0.1 \Rightarrow m_{\text{sec}} = 2$
$h = 0.01 \Rightarrow m_{\text{sec}} = 2$
as $h \to 0$, $m_{\text{sec}} \to 2$

c. Using the point $(1, f(1)) = (1, 7)$ and slope, $m = 2$, we get the secant line:
$y - 7 = 2(x - 1)$
$y - 7 = 2x - 2$
$y = 2x + 5$

d. Graphing:



The graph and the secant line coincide.

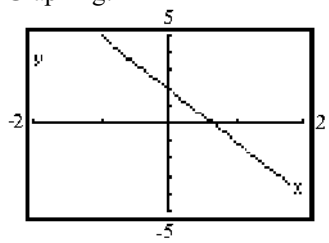
86. $f(x) = -3x + 2$

a. $m_{\text{sec}} = \dfrac{f(x+h) - f(x)}{h}$
$= \dfrac{-3(x+h) + 2 - (-3x + 2)}{h} = \dfrac{-3h}{h} = -3$

b. When $x = 1$,
$h = 0.5 \Rightarrow m_{\text{sec}} = -3$
$h = 0.1 \Rightarrow m_{\text{sec}} = -3$
$h = 0.01 \Rightarrow m_{\text{sec}} = -3$
as $h \to 0$, $m_{\text{sec}} \to -3$

c. Using point $(1, f(1)) = (1, -1)$ and slope = -3, we get the secant line:
$y - (-1) = -3(x - 1)$
$y + 1 = -3x + 3$
$y = -3x + 2$

d. Graphing:



The graph and the secant line coincide.

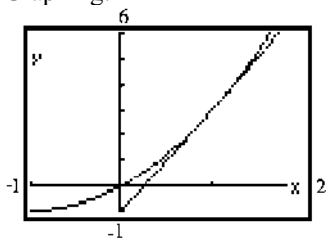
87. $f(x) = x^2 + 2x$

a. $m_{\text{sec}} = \dfrac{f(x+h) - f(x)}{h}$
$= \dfrac{(x+h)^2 + 2(x+h) - (x^2 + 2x)}{h}$
$= \dfrac{x^2 + 2xh + h^2 + 2x + 2h - x^2 - 2x}{h}$
$= \dfrac{2xh + h^2 + 2h}{h}$
$= 2x + h + 2$

b. When $x = 1$,
$h = 0.5 \Rightarrow m_{\text{sec}} = 2 \cdot 1 + 0.5 + 2 = 4.5$
$h = 0.1 \Rightarrow m_{\text{sec}} = 2 \cdot 1 + 0.1 + 2 = 4.1$
$h = 0.01 \Rightarrow m_{\text{sec}} = 2 \cdot 1 + 0.01 + 2 = 4.01$
as $h \to 0$, $m_{\text{sec}} \to 2 \cdot 1 + 0 + 2 = 4$

c. Using point $(1, f(1)) = (1, 3)$ and slope = 4.01, we get the secant line:
$y - 3 = 4.01(x - 1)$
$y - 3 = 4.01x - 4.01$
$y = 4.01x - 1.01$

d. Graphing:



88. $f(x) = 2x^2 + x$

a. $m_{\text{sec}} = \dfrac{f(x+h) - f(x)}{h}$
$= \dfrac{2(x+h)^2 + (x+h) - (2x^2 + x)}{h}$
$= \dfrac{2(x^2 + 2xh + h^2) + x + h - 2x^2 - x}{h}$
$= \dfrac{2x^2 + 4xh + 2h^2 + x + h - 2x^2 - x}{h}$
$= \dfrac{4xh + 2h^2 + h}{h}$
$= 4x + 2h + 1$

b. When $x = 1$,
$h = 0.5 \Rightarrow m_{\text{sec}} = 4 \cdot 1 + 2(0.5) + 1 = 6$

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$h = 0.1 \Rightarrow m_{\text{sec}} = 4 \cdot 1 + 2(0.1) + 1 = 5.2$

$h = 0.01 \Rightarrow m_{\text{sec}} = 4 \cdot 1 + 2(0.01) + 1 = 5.02$

as $h \to 0$, $m_{\text{sec}} \to 4 \cdot 1 + 2(0) + 1 = 5$

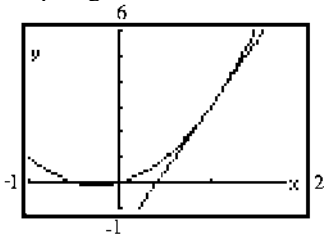
c. Using point $(1, f(1)) = (1, 3)$ and slope = 5.02, we get the secant line:

$y - 3 = 5.02(x - 1)$

$y - 3 = 5.02x - 5.02$

$y = 5.02x - 2.02$

d. Graphing:



89. $f(x) = 2x^2 - 3x + 1$

a. $m_{\text{sec}} = \dfrac{f(x+h) - f(x)}{h}$

$= \dfrac{2(x+h)^2 - 3(x+h) + 1 - (2x^2 - 3x + 1)}{h}$

$= \dfrac{2(x^2 + 2xh + h^2) - 3x - 3h + 1 - 2x^2 + 3x - 1}{h}$

$= \dfrac{2x^2 + 4xh + 2h^2 - 3x - 3h + 1 - 2x^2 + 3x - 1}{h}$

$= \dfrac{4xh + 2h^2 - 3h}{h}$

$= 4x + 2h - 3$

b. When $x = 1$,

$h = 0.5 \Rightarrow m_{\text{sec}} = 4 \cdot 1 + 2(0.5) - 3 = 2$

$h = 0.1 \Rightarrow m_{\text{sec}} = 4 \cdot 1 + 2(0.1) - 3 = 1.2$

$h = 0.01 \Rightarrow m_{\text{sec}} = 4 \cdot 1 + 2(0.01) - 3 = 1.02$

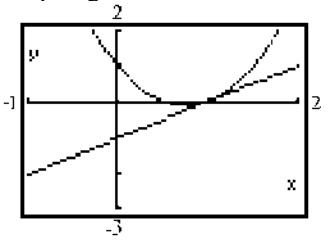
as $h \to 0$, $m_{\text{sec}} \to 4 \cdot 1 + 2(0) - 3 = 1$

c. Using point $(1, f(1)) = (1, 0)$ and slope = 1.02, we get the secant line:

$y - 0 = 1.02(x - 1)$

$y = 1.02x - 1.02$

d. Graphing:



90. $f(x) = -x^2 + 3x - 2$

a. $m_{\text{sec}} = \dfrac{f(x+h) - f(x)}{h}$

$= \dfrac{-(x+h)^2 + 3(x+h) - 2 - (-x^2 + 3x - 2)}{h}$

$= \dfrac{-(x^2 + 2xh + h^2) + 3x + 3h - 2 + x^2 - 3x + 2}{h}$

$= \dfrac{-x^2 - 2xh - h^2 + 3x + 3h - 2 + x^2 - 3x + 2}{h}$

$= \dfrac{-2xh - h^2 + 3h}{h}$

$= -2x - h + 3$

b. When $x = 1$,

$h = 0.5 \Rightarrow m_{\text{sec}} = -2 \cdot 1 - 0.5 + 3 = 0.5$

$h = 0.1 \Rightarrow m_{\text{sec}} = -2 \cdot 1 - 0.1 + 3 = 0.9$

$h = 0.01 \Rightarrow m_{\text{sec}} = -2 \cdot 1 - 0.01 + 3 = 0.99$

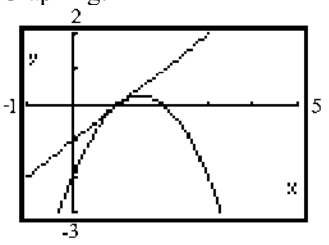
as $h \to 0$, $m_{\text{sec}} \to -2 \cdot 1 - 0 + 3 = 1$

c. Using point $(1, f(1)) = (1, 0)$ and slope = 0.99, we get the secant line:

$y - 0 = 0.99(x - 1)$

$y = 0.99x - 0.99$

d. Graphing:



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91. $f(x)=\dfrac{1}{x}$

a. $m_{\text{sec}}=\dfrac{f(x+h)-f(x)}{h}$

$$=\frac{\left(\frac{1}{x+h}-\frac{1}{x}\right)}{h}=\frac{\left(\frac{x-(x+h)}{(x+h)x}\right)}{h}$$

$$=\left(\frac{x-x-h}{(x+h)x}\right)\left(\frac{1}{h}\right)=\left(\frac{-h}{(x+h)x}\right)\left(\frac{1}{h}\right)$$

$$=-\frac{1}{(x+h)x}$$

b. When $x=1$,

$h=0.5\Rightarrow m_{\text{sec}}=-\dfrac{1}{(1+0.5)(1)}$

$$=-\frac{1}{1.5}=-\frac{2}{3}\approx -0.667$$

$h=0.1\Rightarrow m_{\text{sec}}=-\dfrac{1}{(1+0.1)(1)}$

$$=-\frac{1}{1.1}=-\frac{10}{11}\approx -0.909$$

$h=0.01\Rightarrow m_{\text{sec}}=-\dfrac{1}{(1+0.01)(1)}$

$$=-\frac{1}{1.01}=-\frac{100}{101}\approx -0.990$$

as $h\to 0$, $\quad m_{\text{sec}}\to -\dfrac{1}{(1+0)(1)}=-\dfrac{1}{1}=-1$

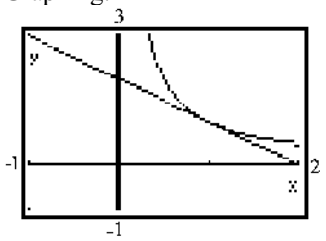
c. Using point $(1, f(1))=(1,1)$ and slope $=-\dfrac{100}{101}$, we get the secant line:

$$y-1=-\frac{100}{101}(x-1)$$

$$y-1=-\frac{100}{101}x+\frac{100}{101}$$

$$y=-\frac{100}{101}x+\frac{201}{101}$$

d. Graphing:



92. $f(x)=\dfrac{1}{x^2}$

a. $m_{\text{sec}}=\dfrac{f(x+h)-f(x)}{h}$

$$=\frac{\left(\frac{1}{(x+h)^2}-\frac{1}{x^2}\right)}{h}$$

$$=\frac{\left(\frac{x^2-(x+h)^2}{(x+h)^2x^2}\right)}{h}$$

$$=\left(\frac{x^2-\left(x^2+2xh+h^2\right)}{(x+h)^2x^2}\right)\left(\frac{1}{h}\right)$$

$$=\left(\frac{-2xh-h^2}{(x+h)^2x^2}\right)\left(\frac{1}{h}\right)$$

$$=\frac{-2x-h}{(x+h)^2x^2}=\frac{-2x-h}{\left(x^2+2xh+h^2\right)x^2}$$

b. When $x=1$,

$h=0.5\Rightarrow m_{\text{sec}}=\dfrac{-2\cdot 1-0.5}{(1+0.5)^2 1^2}=-\dfrac{10}{9}\approx -1.1111$

$h=0.1\Rightarrow m_{\text{sec}}=\dfrac{-2\cdot 1-0.1}{(1+0.1)^2 1^2}=-\dfrac{210}{121}\approx -1.7355$

$h=0.01\Rightarrow m_{\text{sec}}=\dfrac{-2\cdot 1-0.01}{(1+0.01)^2 1^2}$

$$=-\frac{20{,}100}{10{,}201}\approx -1.9704$$

as $h\to 0$, $\quad m_{\text{sec}}\to \dfrac{-2\cdot 1-0}{(1+0)^2 1^2}=-2$

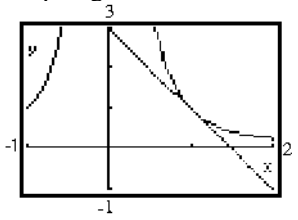
c. Using point $(1, f(1))=(1,1)$ and slope $=-1.9704$, we get the secant line:

$$y-1=-1.9704(x-1)$$

$$y-1=-1.9704x+1.9704$$

$$y=-1.9704x+2.9704$$

d. Graphing:



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93. $f(2)=12$ and $f(-1)=8,$ so

$$\frac{f(2)-f(-1)}{2-(-1)}=\frac{12}{3}=4$$

$f'(x)=4 \rightarrow$

$3x^2+4x-1=4$

$3x^2+4x-5=0$

$$x=\frac{-4\pm\sqrt{4^2-4(3)(-5)}}{2(3)}=\frac{-4\pm\sqrt{76}}{6}$$

$$=\frac{-4\pm 2\sqrt{19}}{6}=\frac{-2\pm\sqrt{19}}{3}$$

$x=\dfrac{-2-\sqrt{19}}{3}\approx -2.1$ is outside the interval

$x=\dfrac{-2+\sqrt{19}}{3}\approx .079$ is in the interval.

The only such number is $\dfrac{-2+\sqrt{19}}{3}$.

94. $g(-x)=-2f\left(-\dfrac{-x}{3}\right)=-2f\left(\dfrac{x}{3}\right)$. Since f is odd,

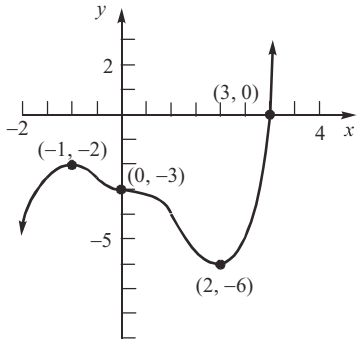
$$f\left(-\frac{x}{3}\right)=-f\left(\frac{x}{3}\right)$$

$$g(-x)=-2f\left(\frac{x}{3}\right)=2f\left(-\frac{x}{3}\right)=-g(x)$$

so g is odd.

So g is odd.

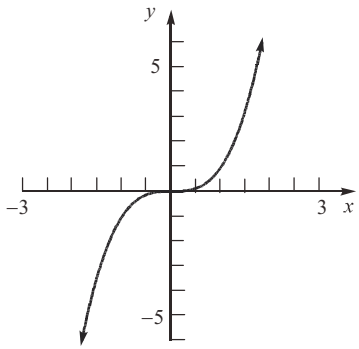
95. Answers will vary. One possibility follows:



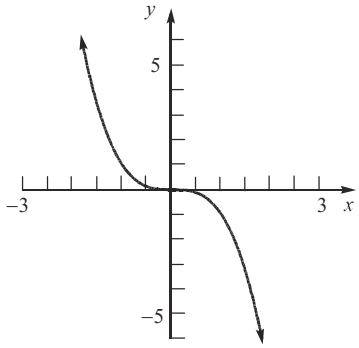
96. Answers will vary. See solution to Problem 89 for one possibility.

97. A function that is increasing on an interval can have at most one x-intercept on the interval. The graph of f could not "turn" and cross it again or it would start to decrease.

98. An increasing function is a function whose graph goes up as you read from left to right.

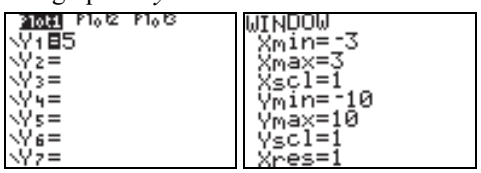


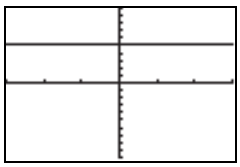
A decreasing function is a function whose graph goes down as you read from left to right.



99. To be an even function we need $f(-x)=f(x)$ and to be an odd function we need $f(-x)=-f(x)$. In order for a function be both even and odd, we would need $f(x)=-f(x)$. This is only possible if $f(x)=0$.

100. The graph of $y=5$ is a horizontal line.





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The local maximum is $y = 5$ and it occurs at each x-value in the interval.

101. Not necessarily. It just means $f(5) > f(2)$. The function could have both increasing and decreasing intervals.

102. $\dfrac{f(x_2) - f(x_1)}{x_2 - x_1} = \dfrac{b - b}{x_2 - x_1} = 0$

$\dfrac{f(2) - f(-2)}{2 - (-2)} = \dfrac{0 - 0}{4} = 0$

103. $\sqrt{540} = \sqrt{36(15)} = 6\sqrt{15}$

104. $(4a - b)^2 = (4a - b)(4a - b)$

$= 16a^2 - 4ab - 4ab + b^2$

$= 16a^2 - 8ab + b^2$

105. $C(x) = 0.80x + 40$

106. $\dfrac{1 \text{ mile}}{33 \text{ hrs}} \cdot \dfrac{24 \text{ hrs}}{1 \text{ day}} = 0.727 \text{ miles/day}$

$\dfrac{1 \text{ day}}{0.727 \text{ miles}} \cdot 6 \text{ miles} = 8.25 \text{ days}$

$S = \dfrac{330}{T}$

$S = \dfrac{330}{10}$

$S = 8.25 \text{ days}$

107. $(x - h)^2 + (y - k)^2 = r^2$

$(x - 3)^2 + (y - (-2))^2 = \left(\dfrac{\sqrt{6}}{2}\right)^2$

$(x - 3)^2 + (y + 2)^2 = \dfrac{3}{2}$

108.

$\left(x^2 - 2\right)^3 2\left(3x^5 + 1\right)15x^4 + \left(3x^5 + 1\right)^2 3\left(x^2 - 2\right)^3 2x$

$= 6x\left(x^2 - 2\right)^2 \left(3x^5 + 1\right)\left[\left(x^2 - 2\right)5x^3 + \left(3x^5 + 1\right)\right]$

$= 6x\left(x^2 - 2\right)^2 \left(3x^5 + 1\right)\left[5x^5 - 10x^3 + 3x^5 + 1\right]$

$= 6x\left(x^2 - 2\right)^2 \left(3x^5 + 1\right)\left[8x^5 - 10x^3 + 1\right]$

109. $\left(\dfrac{x_1 + x_2}{2}, \dfrac{y_1 + y_2}{2}\right) =$

$\left(\dfrac{-2 + \frac{3}{5}}{2}, \dfrac{1 + (-4)}{2}\right) =$

$\left(\dfrac{-\frac{7}{5}}{2}, \dfrac{-3}{2}\right) = \left(-\dfrac{7}{10}, -\dfrac{3}{2}\right)$

110. $|3x + 7| - 3 = 5$

$|3x + 7| = 8$

$3x + 7 = -8 \quad \text{or} \quad 3x + 7 = 8$

$3x = -15 \qquad 3x = 1$

$x = -5 \qquad x = \dfrac{1}{3}$

The solution set is $\left\{-5, \dfrac{1}{3}\right\}$.

111. $x^6 + 7x^3 = 8$

$x^6 + 7x^3 - 8 = 0$

$(x^3 + 8)(x^3 - 1) = 0$

$x^3 + 8 = 0 \quad \text{or} \quad x^3 - 1 = 0$

$x^3 = -8 \qquad x^3 = 1$

$x = -2 \qquad x = 1$

The solution set is $\{-2, 1\}$.

112. $3y^2 \cdot D + 3x^2 - 3xy^2 - 3x^2 y \cdot D = 0$

$3y^2 \cdot D - 3x^2 y \cdot D = -3x^2 + 3xy^2$

$D\left(3y^2 - 3x^2 y\right) = -3x^2 + 3xy^2$

$D = \dfrac{-3x^2 + 3xy^2}{3y^2 - 3x^2 y} = \dfrac{xy^2 - x^2}{y^2 - x^2 y} = \dfrac{x\left(y^2 - x\right)}{y\left(y - x^2\right)}$

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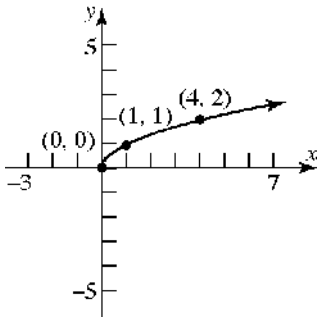
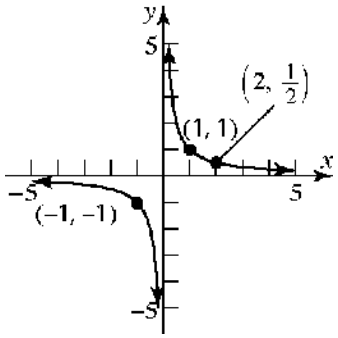
Section 2.4

1. $y = \sqrt{x}$



2. $y = \dfrac{1}{x}$



3. $y = x^3 - 8$

<u>*y*-intercept:</u>

Let $x = 0$, then $y = (0)^3 - 8 = -8$.

<u>*x*-intercept:</u>

Let $y = 0$, then $0 = x^3 - 8$

$x^3 = 8$

$x = 2$

The intercepts are $(0, -8)$ and $(2, 0)$.

4. $(-\infty, 0)$

5. piecewise-defined

6. True

7. False; the cube root function is odd and increasing on the interval $(-\infty, \infty)$.

8. False; the domain and range of the reciprocal function are both the set of real numbers except for 0.

9. b

10. a

11. C

12. A

13. E

14. G

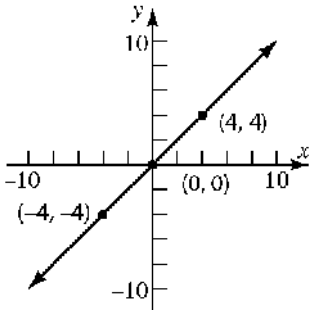
15. B

16. D

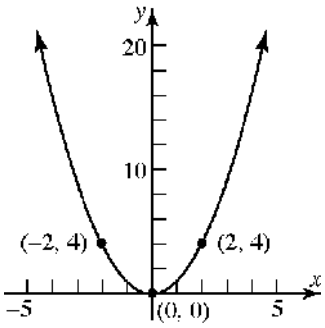
17. F

18. H

19. $f(x) = x$



20. $f(x) = x^2$



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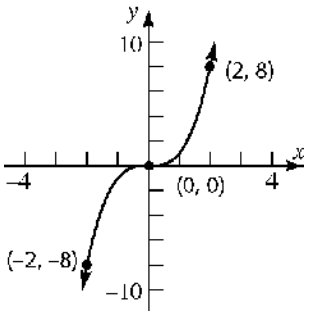
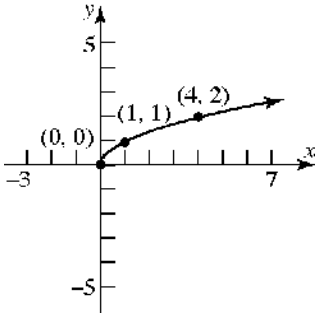
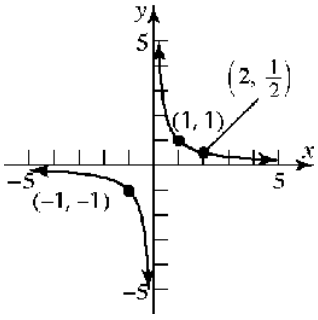
21. $f(x) = x^3$



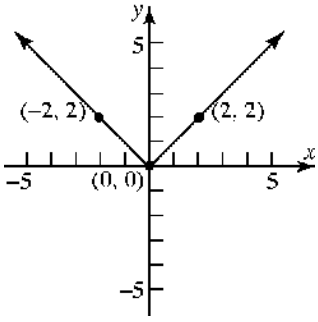
22. $f(x) = \sqrt{x}$



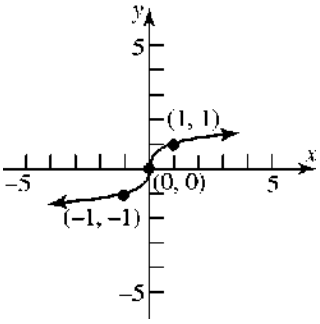
23. $f(x) = \dfrac{1}{x}$



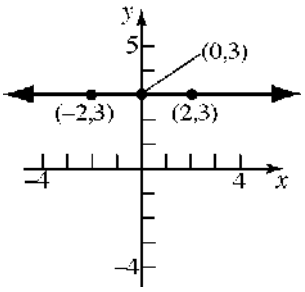
24. $f(x) = |x|$



25. $f(x) = \sqrt[3]{x}$



26. $f(x) = 3$



27. **a.** $f(-3) = -(-3)^2 = -9$

b. $f(0) = 4$

c. $f(2) = 3(3) - 2 = 7$

28. **a.** $f(-2) = -3(-2) = 6$

b. $f(-1) = 0$

c. $f(0) = 2(0)^2 + 1 = 1$

29. **a.** $f(-2) = 2(-2) + 4 = 0$

b. $f(0) = 2(0) + 4 = 4$

c. $f(1) = 2(1) + 4 = 6$

d. $f(3) = (3)^3 - 1 = 26$

30. **a.** $f(-1) = (-1)^3 = -1$

b. $f(0) = (0)^3 = 0$

c. $f(1) = 3(1) + 2 = 5$

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d. $f(3) = 3(3) + 2 = 11$

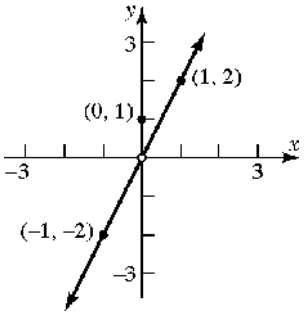
31. $f(x) = \begin{cases} 2x & \text{if } x \neq 0 \\ 1 & \text{if } x = 0 \end{cases}$

a. Domain: $\{x \mid x \text{ is any real number}\}$

b. x-intercept: none
y-intercept:
$f(0) = 1$

The only intercept is $(0,1)$.

c. Graph:



d. Range: $\{y \mid y \neq 0\}$; $(-\infty, 0) \cup (0, \infty)$

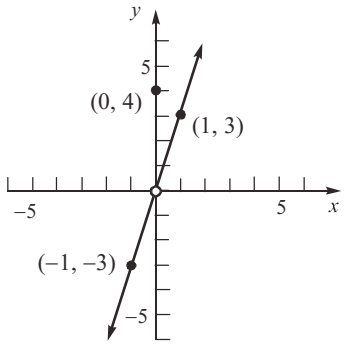
32. $f(x) = \begin{cases} 3x & \text{if } x \neq 0 \\ 4 & \text{if } x = 0 \end{cases}$

a. Domain: $\{x \mid x \text{ is any real number}\}$

b. x-intercept: none
y-intercept: $f(0) = 4$

The only intercept is $(0,4)$.

c. Graph:



d. Range: $\{y \mid y \neq 0\}$; $(-\infty, 0) \cup (0, \infty)$

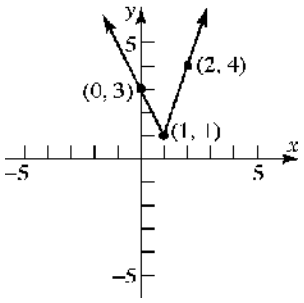
33. $f(x) = \begin{cases} -2x + 3 & \text{if } x < 1 \\ 3x - 2 & \text{if } x \geq 1 \end{cases}$

a. Domain: $\{x \mid x \text{ is any real number}\}$

b. x-intercept: none
y-intercept: $f(0) = -2(0) + 3 = 3$

The only intercept is $(0,3)$.

c. Graph:



d. Range: $\{y \mid y \geq 1\}$; $[1, \infty)$

34. $f(x) = \begin{cases} x + 3 & \text{if } x < -2 \\ -2x - 3 & \text{if } x \geq -2 \end{cases}$

a. Domain: $\{x \mid x \text{ is any real number}\}$

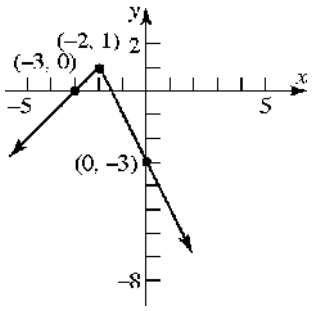
b. $x + 3 = 0$ $\qquad -2x - 3 = 0$
$x = -3$ $\qquad -2x = 3$
$x = -\frac{3}{2}$

x-intercepts: $-3, -\frac{3}{2}$

y-intercept: $f(0) = -2(0) - 3 = -3$

The intercepts are $(-3,0)$, $\left(-\frac{3}{2}, 0\right)$, and $(0,-3)$.

c. Graph:



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d. Range: $\{y \mid y \le 1\}$; $(-\infty, 1]$

35. $f(x) = \begin{cases} x+3 & \text{if } -2 \le x < 1 \\ 5 & \text{if } x = 1 \\ -x+2 & \text{if } x > 1 \end{cases}$

a. Domain: $\{x \mid x \ge -2\}$; $[-2, \infty)$

b. $x+3=0$ $\quad -x+2=0$

$x=-3$ $\quad -x=-2$

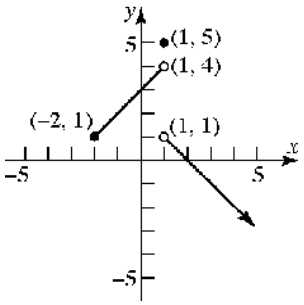
(not in domain) $\quad x=2$

x-intercept: 2

y-intercept: $f(0)=0+3=3$

The intercepts are $(2,0)$ and $(0,3)$.

c. Graph:



d. Range: $\{y \mid y < 4,\ y = 5\}$; $(-\infty, 4) \cup \{5\}$

36. $f(x) = \begin{cases} 2x+5 & \text{if } -3 \le x < 0 \\ -3 & \text{if } x = 0 \\ -5x & \text{if } x > 0 \end{cases}$

a. Domain: $\{x \mid x \ge -3\}$; $[-3, \infty)$

b. $2x+5=0$ $\quad -5x=0$

$2x=-5$ $\quad x=0$

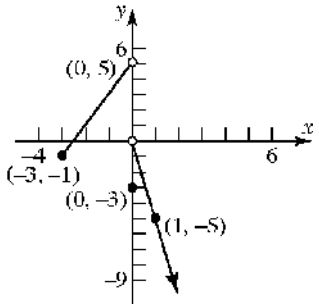
$x=-\frac{5}{2}$ $\quad$ (not in domain of piece)

x-intercept: $-\frac{5}{2}$

y-intercept: $f(0)=-3$

The intercepts are $\left(-\frac{5}{2}, 0\right)$ and $(0,-3)$.

c. Graph:



d. Range: $\{y \mid y < 5\}$; $(-\infty, 5)$

37. $f(x) = \begin{cases} 1+x & \text{if } x < 0 \\ x^2 & \text{if } x \ge 0 \end{cases}$

a. Domain: $\{x \mid x \text{ is any real number}\}$

b. $1+x=0$ $\quad x^2=0$

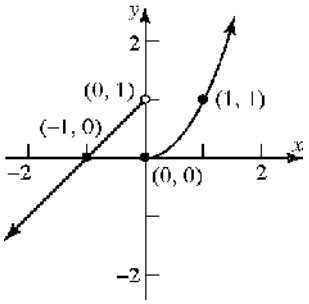
$x=-1$ $\quad x=0$

x-intercepts: $-1, 0$

y-intercept: $f(0)=0^2=0$

The intercepts are $(-1,0)$ and $(0,0)$.

c. Graph:



d. Range: $\{y \mid y \text{ is any real number}\}$

38. $f(x) = \begin{cases} \dfrac{1}{x} & \text{if } x < 0 \\ \sqrt[3]{x} & \text{if } x \ge 0 \end{cases}$

a. Domain: $\{x \mid x \text{ is any real number}\}$

b. $\frac{1}{x}=0$ $\quad \sqrt[3]{x}=0$

(no solution) $\quad x=0$

x-intercept: 0

y-intercept: $f(0)=\sqrt[3]{0}=0$

The only intercept is $(0,0)$.

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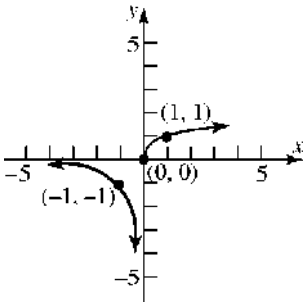
c. Graph:



d. Range: $\{y \mid y \text{ is any real number}\}$

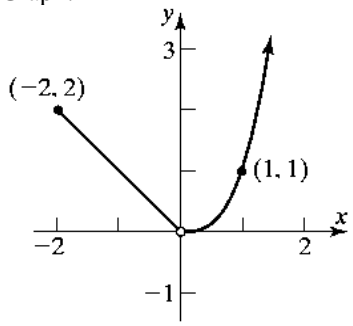
39. $f(x) = \begin{cases} |x| & \text{if } -2 \le x < 0 \\ x^3 & \text{if } x > 0 \end{cases}$

a. Domain: $\{x \mid -2 \le x < 0 \text{ and } x > 0\}$ or $\{x \mid x \ge -2, x \ne 0\}$; $[-2, 0) \cup (0, \infty)$.

b. x-intercept: none
There are no x-intercepts since there are no values for x such that $f(x) = 0$.

y-intercept:
There is no y-intercept since $x = 0$ is not in the domain.

c. Graph:



d. Range: $\{y \mid y > 0\}$; $(0, \infty)$

40. $f(x) = \begin{cases} 2 - x & \text{if } -3 \le x < 1 \\ \sqrt{x} & \text{if } x > 1 \end{cases}$

a. Domain: $\{x \mid -3 \le x < 1 \text{ and } x > 1\}$ or $\{x \mid x \ge -3, x \ne 1\}$; $[-3, 1) \cup (1, \infty)$.

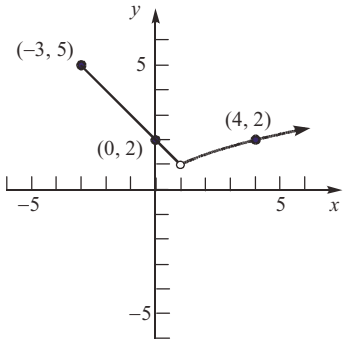
b. $2 - x = 0$ $\quad$ $\sqrt{x} = 0$
$x = 2$ $\quad$ $x = 0$
(not in domain of piece)

no x-intercepts

y-intercept: $f(0) = 2 - 0 = 2$

The intercept is $(0, 2)$.

c. Graph:



d. Range: $\{y \mid y > 1\}$; $(1, \infty)$

41. $f(x) = \begin{cases} x^2 & \text{if } 0 < x \le 2 \\ x + 2 & \text{if } 2 < x < 5 \\ 7 & \text{if } \ge 5 \end{cases}$

a. Domain: $\{x \mid x > 0\}$; $(0, \infty)$.

b. $x^2 = 0$
$x = 0$
(not in domain of piece)

$x + 2 = 0$ $\quad$ $7 = 0$
$x = -2$ $\quad$ (not possible)
(not in domain of piece)

No intercepts.

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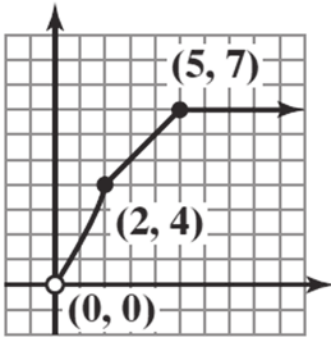
c. Graph:



d. Range: $\{y \mid 0 < y \le 7\}$; $(0, 7]$

42. $f(x) = \begin{cases} 3x+5 & \text{if } -3 \le x < 0 \\ 5 & \text{if } 0 \le x \le 2 \\ x^2+1 & \text{if } x > 2 \end{cases}$

a. Domain: $\{x \mid x \ge -3\}$; $[-3, \infty)$.

b. $3x+5=0$ $\quad 5=0$ $\quad x^2+1=0$

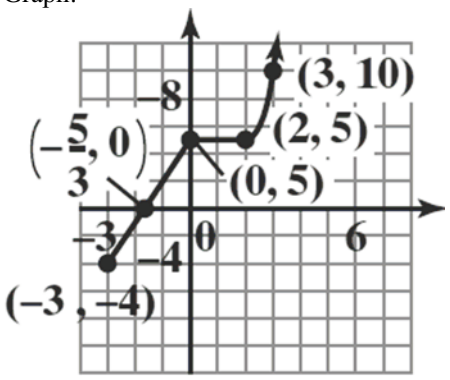
$x = -\frac{5}{3}$ (not possible) $\quad x^2 = -1$ (not possible)

x-intercept: $-\frac{5}{3}$

y-intercept: $f(0) = 5$

The intercepts are $(0, 5)$ and $\left(-\frac{5}{3}, 0\right)$.

c. Graph:



d. Range: $[-4, \infty)$

43. Answers may vary. One possibility follows:

$$f(x) = \begin{cases} -x & \text{if } -1 \le x \le 0 \\ \frac{1}{2}x & \text{if } 0 < x \le 2 \end{cases}$$

44. Answers may vary. One possibility follows:

$$f(x) = \begin{cases} x & \text{if } -1 \le x \le 0 \\ 1 & \text{if } 0 < x \le 2 \end{cases}$$

45. Answers may vary. One possibility follows:

$$f(x) = \begin{cases} -x & \text{if } x \le 0 \\ -x+2 & \text{if } 0 < x \le 2 \end{cases}$$

46. Answers may vary. One possibility follows:

$$f(x) = \begin{cases} 2x+2 & \text{if } -1 \le x \le 0 \\ x & \text{if } x > 0 \end{cases}$$

47. a. $f(1.7) = \text{int}(2(1.7)) = \text{int}(3.4) = 3$

b. $f(2.8) = \text{int}(2(2.8)) = \text{int}(5.6) = 5$

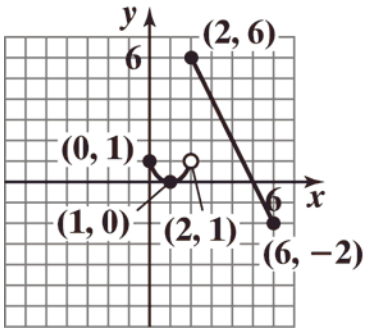
c. $f(-3.6) = \text{int}(2(-3.6)) = \text{int}(-7.2) = -8$

48. a. $f(1.2) = \text{int}\left(\frac{1.2}{2}\right) = \text{int}(0.6) = 0$

b. $f(1.6) = \text{int}\left(\frac{1.6}{2}\right) = \text{int}(0.8) = 0$

c. $f(-1.8) = \text{int}\left(\frac{-1.8}{2}\right) = \text{int}(-0.9) = -1$

49. a.



b. The domain is $[0, 6]$.

c. Absolute max: $f(2) = 6$

Absolute min: $f(6) = -2$

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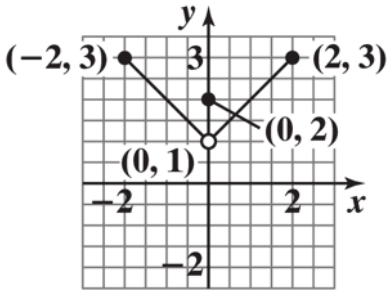
50. a.



b. The domain is $[-2, 2]$.

c. Absolute max: $f(-2) = f(2) = 3$
Absolute min: none

51. $C = \begin{cases} 34.99 & \text{if } 0 < x \le 3 \\ 15x - 10.01 & \text{if } x > 3 \end{cases}$

a. $C(2) = \$34.99$

b. $C(5) = 15(5) - 10.01 = \$64.99$

c. $C(13) = 15(13) - 10.01 = \$184.99$

52. $F(x) = \begin{cases} 2 - 3\,\text{int}(1 - x) & 0 < x \le 4 \\ 2 - 9\,\text{int}(3 - x) & 4 < x \le 9 \\ 74 & 9 < x \le 24 \end{cases}$

a. $F(2) = 2 - 3\,\text{int}(1 - 2) = 5$
Parking for 2 hours costs \$5.

b. $F(7) = 2 - 9\,\text{int}(3 - 7) = 38$
Parking for 7 hours costs \$38.

c. $F(15) = 74$
Parking for 15 hours costs \$74.

d. $24 \text{ min} \cdot \dfrac{1 \text{ hr}}{60 \text{ min}} = 0.4 \text{ hr}$

$F(8.4) = 2 - 9\,\text{int}(3 - 8.4) = 2 - (9)(-6) = 56$

Parking for 8 hours and 24 minutes costs \$56.

53. a. Charge for 20 therms:
$C = 23.44 + 0.91686(20) + 0.26486(20)$
$= \$47.07$

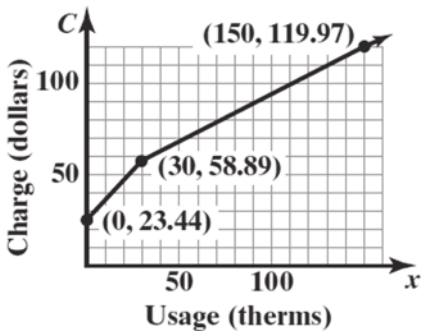
b. Charge for 150 therms:
$C = 23.44 + 0.91686(30) + 0.26486(30) + 0.50897(120)$
$= \$119.97$

c. For $0 \le x \le 30$:
$C = 23.44 + 0.91686x + 0.26486x$
$= 1.18172x + 23.44$

For $x > 30$:
$C = 23.44 + 0.91686(30) + 0.50897(x - 30) + 0.26486(30)$
$= 23.44 + 27.5058 + 0.50897x - 15.2691 + 7.9458$
$= 0.50897x + 43.6225$

The monthly charge function:
$C = \begin{cases} 1.18172x + 23.44 & \text{if } 0 \le x \le 30 \\ 0.50897x + 43.6225 & \text{if } x > 30 \end{cases}$

d. Graph:



54. a. Charge for 1000 therms:
$C = 90.00 + 0.1201(150) + 0.0549(850) + 0.35(1000)$
$= \$504.68$

b. Charge for 6000 therms:
$C = 90.00 + 0.1201(150) + 0.0549(4850) + 0.0482(1000) + 0.35(6000)$
$= \$2522.48$

c. For $0 \le x \le 150$:
$C = 90.00 + 0.1201x + 0.35x$
$= 0.4701x + 90.00$

For $150 < x \le 5000$:
$C = 90.00 + 0.1201(150) + 0.0549(x - 150) + 0.35x$
$= 90.00 + 18.015 + 0.0549x - 8.235 + 0.35x$
$= 0.4049x + 99.78$

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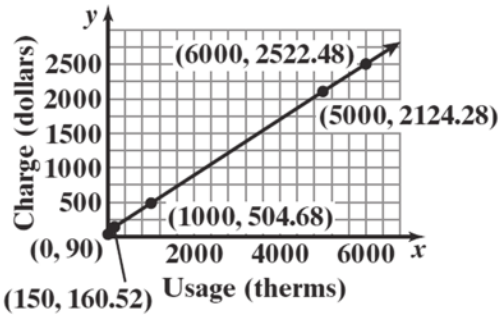
For $x > 5000$:

$$\begin{aligned} C &= 90.00 + 0.1201(150) + 0.0549(4850) \\ &\quad + 0.0482(x - 5000) + 0.35x \\ &= 90.00 + 18.015 + 266.265 + 0.0482x - 241 \\ &\quad + 0.35x \\ &= 0.3982x + 133.28 \end{aligned}$$

The monthly charge function:

$$C(x) = \begin{cases} 0.4701x + 90.00 & \text{if } 0 \le x \le 150 \\ 0.4049x + 82.38 & \text{if } 150 < x \le 5000 \\ 0.3982x + 115.88 & \text{if } x > 5000 \end{cases}$$

d.



55. For schedule X:

$$f(x) = \begin{cases} 0.10x & \text{if } 0 < x \le 9525 \\ 952.50 + 0.12(x - 9525) & \text{if } 9525 < x \le 38,700 \\ 4453.50 + 0.22(x - 38,700) & \text{if } 38,700 < x \le 82,500 \\ 14,089.50 + 0.24(x - 82,500) & \text{if } 82,500 < x \le 157,500 \\ 32,089.75 + 0.32(x - 157,500) & \text{if } 157,500 < x \le 200,000 \\ 45,689.50 + 0.35(x - 200,000) & \text{if } 200,000 < x \le 500,000 \\ 150,689.50 + 0.37(x - 500,000) & \text{if } x > 500,000 \end{cases}$$

56. For Schedule Y−1:

$$f(x) = \begin{cases} 0.10x & \text{if } 0 < x \le 19,050 \\ 1905.00 + 0.12(x - 19,050) & \text{if } 19,050 < x \le 77,400 \\ 8,907.00 + 0.22(x - 77,400) & \text{if } 77,400 < x \le 165,000 \\ 28,179.00 + 0.24(x - 165,000) & \text{if } 165,000 < x \le 315,000 \\ 64,179.00 + 0.32(x - 315,000) & \text{if } 315,000 < x \le 400,000 \\ 91,379.00 + 0.35(x - 400,000) & \text{if } 400,000 < x \le 600,000 \\ 161,379.00 + 0.37(x - 600,000) & \text{if } x > 600,000 \end{cases}$$

57. a. Let x represent the number of miles and C be the cost of transportation.

$$C(x) = \begin{cases} 0.50x & \text{if } 0 \le x \le 100 \\ 0.50(100) + 0.40(x - 100) & \text{if } 100 < x \le 400 \\ 0.50(100) + 0.40(300) + 0.25(x - 400) & \text{if } 400 < x \le 800 \\ 0.50(100) + 0.40(300) + 0.25(400) + 0(x - 800) & \text{if } 800 < x \le 960 \end{cases}$$

$$C(x) = \begin{cases} 0.50x & \text{if } 0 \le x \le 100 \\ 10 + 0.40x & \text{if } 100 < x \le 400 \\ 70 + 0.25x & \text{if } 400 < x \le 800 \\ 270 & \text{if } 800 < x \le 960 \end{cases}$$

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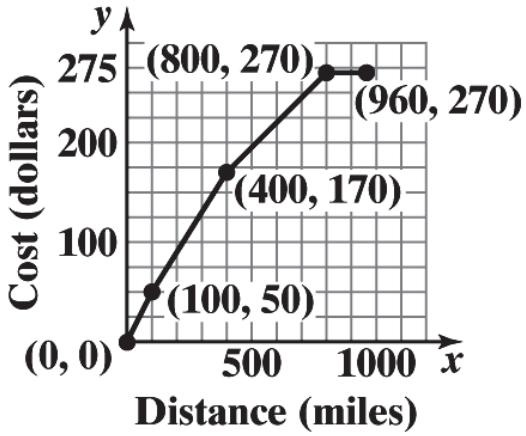
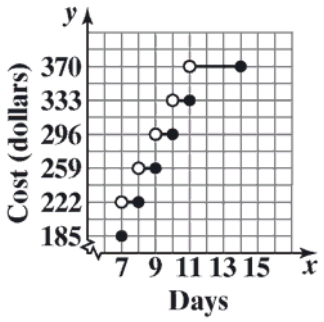


b. For hauls between 100 and 400 miles the cost is: $C(x) = 10 + 0.40x$.

c. For hauls between 400 and 800 miles the cost is: $C(x) = 70 + 0.25x$.

58. Let x = number of days car is used. The cost of renting is given by

$$C(x) = \begin{cases} 185 & \text{if } x = 7 \\ 222 & \text{if } 7 < x \le 8 \\ 259 & \text{if } 8 < x \le 9 \\ 296 & \text{if } 9 < x \le 10 \\ 333 & \text{if } 10 < x \le 11 \\ 370 & \text{if } 11 < x \le 14 \end{cases}$$



59. a. Let s = the credit score of an individual who wishes to borrow $300,000 with an 80% LTV ratio. The adverse market delivery charge is given by

$$C(s) = \begin{cases} 9000 & \text{if } s \le 659 \\ 8250 & \text{if } 660 \le s \le 679 \\ 5250 & \text{if } 680 \le s \le 699 \\ 3750 & \text{if } 700 \le s \le 719 \\ 2250 & \text{if } 720 \le s \le 739 \\ 1500 & \text{if } s \ge 740 \end{cases}$$

b. 725 is between 720 and 739 so the charge would be $2250.

c. 670 is between 660 and 679 so the charge would be $8250.

60. Let x = the amount of the bill in dollars. The minimum payment due is given by

$$f(x) = \begin{cases} x & \text{if } 0 \le x < 10 \\ 10 & \text{if } 10 \le x < 500 \\ 30 & \text{if } 500 \le x < 1000 \\ 50 & \text{if } 1000 \le x < 1500 \\ 70 & \text{if } x \ge 1500 \end{cases}$$

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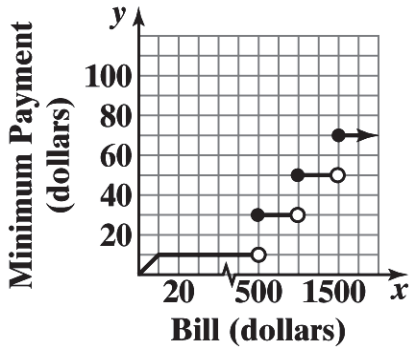


61. **a.** $W = 10°C$

b. $W = 33 - \dfrac{(10.45 + 10\sqrt{5} - 5)(33 - 10)}{22.04} \approx 4°C$

c. $W = 33 - \dfrac{(10.45 + 10\sqrt{15} - 15)(33 - 10)}{22.04} \approx -3°C$

d. $W = 33 - 1.5958(33 - 10) = -4°C$

e. When $0 \le v < 1.79$, the wind speed is so small that there is no effect on the temperature.

f. When the wind speed exceeds 20, the wind chill depends only on the air temperature.

62. **a.** $W = -10°C$

b. $W = 33 - \dfrac{\left(10.45 + 10\sqrt{5} - 5\right)\left(33 - \left(-10\right)\right)}{22.04}$

$\approx -21°C$

c. $W = 33 - \dfrac{\left(10.45 + 10\sqrt{15} - 15\right)\left(33 - \left(-10\right)\right)}{22.04}$

$\approx -34°C$

d. $W = 33 - 1.5958\left(33 - \left(-10\right)\right) = -36°C$

63. Let x = the number of ounces and $C\left(x\right)$ = the postage due.

For $0 < x \le 1$: $C\left(x\right) = \$1.00$

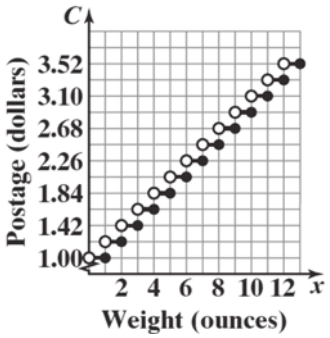
For $1 < x \le 2$: $C\left(x\right) = 1.00 + 0.21 = \$1.21$

For $2 < x \le 3$: $C\left(x\right) = 1.00 + 2\left(0.21\right) = \$1.42$

For $3 < x \le 4$: $C\left(x\right) = 1.0 + 3\left(0.21\right) = \$1.63$

$\vdots$

For $12 < x \le 13$: $C\left(x\right) = 1.00 + 12\left(0.21\right) = \$3.52$



64. Use intervals $\left(0,8\right),\left[8,16\right),\left[16,32\right),\left[32,38\right)$ (exclude 0 and 38 since those would be the walls). Depth for the intervals $\left[8,16\right)$ and $\left[32,38\right)$ are constant (8 ft and 3 ft respectively). The other two are linear functions. On $\left(0,8\right)$ the endpoint coordinates can be thought or as $\left(0,3\right)$ and $\left(8,8\right)$.

$$m = \frac{8-3}{8-0} = \frac{5}{8} \quad y = \frac{5}{8}x + 3$$

On $\left[16,32\right)$ the endpoint coordinates can be thought of as $\left(16,8\right)$ and $\left(32,3\right)$.

$$m = \frac{3-8}{32-16} = -\frac{5}{16}$$

$$8 = -\frac{5}{16}(16) + b$$

$$13 = b$$

$$y = -\frac{5}{16}x + 13$$

Therefore,

$$d(x) = \begin{cases} \dfrac{5}{8}x + 3 & \text{if } 0 < x < 8 \\ 8 & \text{if } 8 \le x < 16 \\ -\dfrac{5}{16}x + 13 & \text{if } 16 \le x < 32 \\ 3 & \text{if } 32 \le x < 38 \end{cases}$$

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65. The function *f* changes definition at 2 and the function *g* changes definition at 0. Combining these together, the sum function will change definitions at 0 and 2.

On the interval $(-\infty, 0]$:

$$(f+g)(x) = f(x) + g(x) = (2x+3) + (-4x+1) \cdot$$
$$= -2x + 4$$

On the interval $(0, 2)$:

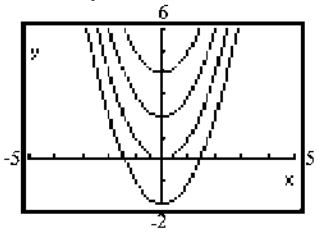
$$(f+g)(x) = f(x) + g(x) = (2x+3) + (x-7) \cdot$$
$$= 3x - 4$$

On the interval $[2, \infty)$:

$$(f+g)(x) = f(x) + g(x) = (x^2 + 5x) + (x-7)$$
$$= x^2 + 6x - 7$$

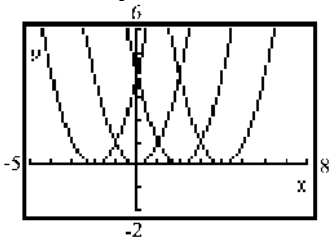
So, $(f+g)(x) = \begin{cases} -2x+4 & \text{if } x \le 0 \\ 3x-4 & \text{if } 0 < x \le 2 \\ x^2+6x-7 & \text{if } x \ge 2 \end{cases}$

66. Each graph is that of $y = x^2$, but shifted vertically.



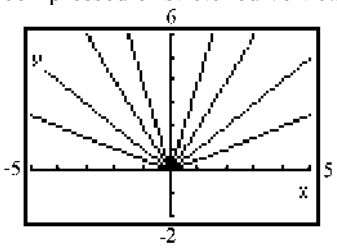
If $y = x^2 + k,\ k > 0$, the shift is up k units; if $y = x^2 - k,\ k > 0$, the shift is down *k* units. The graph of $y = x^2 - 4$ is the same as the graph of $y = x^2$, but shifted down 4 units. The graph of $y = x^2 + 5$ is the graph of $y = x^2$, but shifted up 5 units.

67. Each graph is that of $y = x^2$, but shifted horizontally.



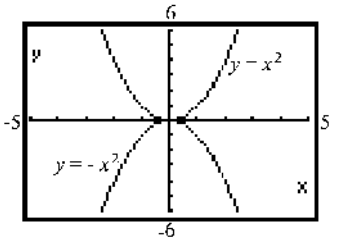
If $y = (x-k)^2,\ k > 0$, the shift is to the right k units; if $y = (x+k)^2,\ k > 0$, the shift is to the left *k* units. The graph of $y = (x+4)^2$ is the same as the graph of $y = x^2$, but shifted to the left 4 units. The graph of $y = (x-5)^2$ is the graph of $y = x^2$, but shifted to the right 5 units.

68. Each graph is that of $y = |x|$, but either compressed or stretched vertically.

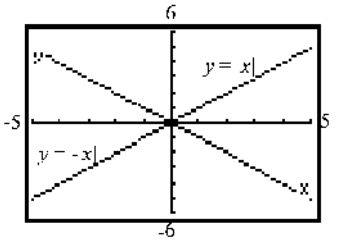


If $y = k|x|$ and $k > 1$, the graph is stretched vertically; if $y = k|x|$ and $0 < k < 1$, the graph is compressed vertically. The graph of $y = \frac{1}{4}|x|$ is the same as the graph of $y = |x|$, but compressed vertically. The graph of $y = 5|x|$ is the same as the graph of $y = |x|$, but stretched vertically.

69. The graph of $y = -x^2$ is the reflection of the graph of $y = x^2$ about the *x*-axis.



The graph of $y = -|x|$ is the reflection of the graph of $y = |x|$ about the *x*-axis.



Multiplying a function by –1 causes the graph to be a reflection about the *x*-axis of the original function's graph.

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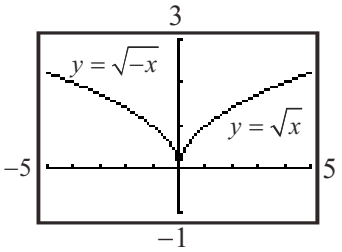
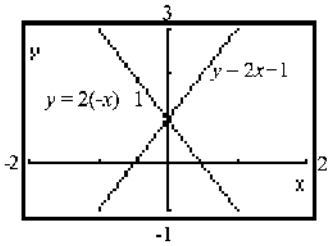
70. The graph of $y = \sqrt{-x}$ is the reflection about the y-axis of the graph of $y = \sqrt{x}$.

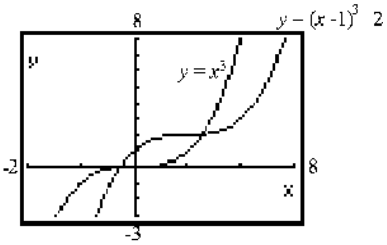


The same type of reflection occurs when graphing $y = 2x + 1$ and $y = 2(-x) + 1$.

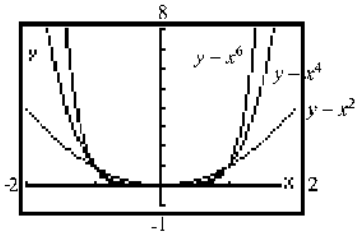


The graph of $y = f(-x)$ is the reflection about the y-axis of the graph of $y = f(x)$.

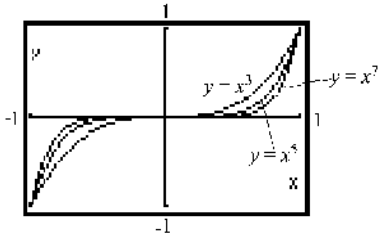
71. The graph of $y = (x-1)^3 + 2$ is a shifting of the graph of $y = x^3$ one unit to the right and two units up. Yes, the result could be predicted.



72. The graphs of $y = x^n$, n a positive even integer, **are all U-shaped and open upward. All go** through the points $(-1, 1)$, $(0, 0)$, and $(1, 1)$. As n increases, the graph of the function is narrower for $|x| > 1$ and flatter for $|x| < 1$.



73. The graphs of $y = x^n$, n a positive odd integer, all have the same general shape. All go through the points $(-1, -1)$, $(0, 0)$, and $(1, 1)$. As n increases, the graph of the function increases at a greater rate for $|x| > 1$ and is flatter around 0 for $|x| < 1$.



74. $f(x) = \begin{cases} 1 & \text{if } x \text{ is rational} \\ 0 & \text{if } x \text{ is irrational} \end{cases}$

Yes, it is a function.

Domain = $\{x \mid x \text{ is any real number}\}$ or $(-\infty, \infty)$

Range = $\{0, 1\}$ or $\{y \mid y = 0 \text{ or } y = 1\}$

y-intercept: $x = 0 \Rightarrow x$ is rational $\Rightarrow y = 1$

So the y-intercept is $y = 1$.

x-intercept: $y = 0 \Rightarrow x$ is irrational

So the graph has infinitely many x-intercepts, namely, there is an x-intercept at each irrational value of x.

$f(-x) = 1 = f(x)$ when x is rational;

$f(-x) = 0 = f(x)$ when x is irrational.

Thus, f is even.

The graph of f consists of 2 infinite clusters of distinct points, extending horizontally in both directions. One cluster is located 1 unit above the x-axis, and the other is located along the x-axis.

75. Answers will vary.

76. $(x^{-3}y^5)^{-2} = x^6 y^{-10} = \dfrac{x^6}{y^{10}}$

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77. $x^2 + y^2 = 6y + 16$

$x^2 + y^2 - 6y = 16$

$x^2 + (y^2 - 6y + 9) = 16 + 9$

$x^2 + (y-3)^2 = 5^2$

Center (h,k): (0, 3); Radius = 5

78. $4x - 5(2x-1) = 4 - 7(x+1)$

$4x - 10x + 5 = 4 - 7x - 7$

$-6x + 5 = -7x - 3$

$x = -8$

The solution set is: $\{-8\}$

79. Let x represent the amount of money invested in a mutual fund. Then $60,000 - x$ represents the amount of money invested in CD's. Since the total interest is to be \$3700, we have:

$0.08x + 0.03(60,000 - x) = 3700$

$(100)(0.08x + 0.03(60,000 - x)) = (3700)(100)$

$8x + 3(60,000 - x) = 370,000$

$8x + 180,000 - 3x = 370,000$

$5x + 180,000 = 370,000$

$5x = 190,000$

$x = 38,000$

\$38,000 should be invested in a mutual fund at 8% and \$22,000 should be invested in CD's at 3%.

80.

$$\begin{array}{r|rrrr} -2 & 1 & 3 & 0 & -6 \\ & & -2 & -2 & 4 \\ \hline & 1 & 1 & 6 & -2 \end{array}$$

Quotient: $x^2 + x - 2$

Remainder: -2

81. $\frac{3}{2} + 2i$

82. $-2x^7$

83. $\sqrt{\left(5t^2\right)^2 + \left(25t^{7/2}\right)^2} = \sqrt{25t^4 + 625t^7}$

$= \sqrt{25t^4\left(1 + 25t^3\right)}$

$= 5t^2\sqrt{1 + 25t^3}$

84. The radicand cannot be negative so:

$x + 7 \geq 0$

$x \geq -7$

The domain is $\{x \mid x \geq -7\}$.

85. $3x^3y - 2x^2y^2 + 18x - 12y =$

$\left(3x^3y - 2x^2y^2\right) + (18x - 12y) =$

$x^2y(3x - 2y) + 6(3x - 4y) =$

$(3x - 2y)\left(x^2y + 6\right)$

Section 2.5

1. horizontal; right

2. y

3. False

4. True; the graph of $y = -f(x)$ is the reflection about the x-axis of the graph of $y = f(x)$.

5. d

6. b

7. B

8. E

9. H

10. D

11. I

12. A

13. L

14. C

15. F

16. J

17. G

18. K

19. $y = (x-4)^3$

20. $y = (x+4)^3$

21. $y = x^3 + 4$

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22. $y = x^3 - 4$

23. $y = (-x)^3 = -x^3$

24. $y = -x^3$

25. $y = 5x^3$

26. $y = \left(\frac{1}{4}x\right)^3 = \frac{1}{64}x^3$

27. $y = (2x)^3 = 8x^3$

28. $y = \frac{1}{4}x^3$

29. (1) $y = \sqrt{x} + 2$

(2) $y = -\left(\sqrt{x} + 2\right)$

(3) $y = -\left(\sqrt{-x} + 2\right) = -\sqrt{-x} - 2$

30. (1) $y = -\sqrt{x}$

(2) $y = -\sqrt{x-3}$

(3) $y = -\sqrt{x-3} - 2$

31. (1) $y = 3\sqrt{x}$

(2) $y = 3\sqrt{x} + 4$

(3) $y = 3\sqrt{x+5} + 4$

32. (1) $y = \sqrt{x} + 2$

(2) $y = \sqrt{-x} + 2$

(3) $y = \sqrt{-(x+3)} + 2 = \sqrt{-x-3} + 2$

33. (c); To go from $y = f(x)$ to $y = -f(x)$ we reflect about the *x*-axis. This means we change the sign of the *y*-coordinate for each point on the graph of $y = f(x)$. Thus, the point $(3, 6)$ would become $(3, -6)$.

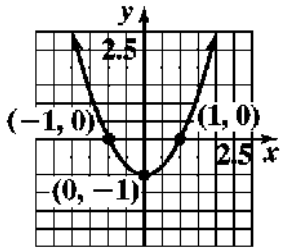
34. (d); To go from $y = f(x)$ to $y = f(-x)$, we reflect each point on the graph of $y = f(x)$ about the *y*-axis. This means we change the sign of the *x*-coordinate for each point on the graph of $y = f(x)$. Thus, the point $(3, 6)$ would become $(-3, 6)$.

35. (c); To go from $y = f(x)$ to $y = 2f(x)$, we stretch vertically by a factor of 2. Multiply the *y*-coordinate of each point on the graph of $y = f(x)$ by 2. Thus, the point $(1, 3)$ would become $(1, 6)$.

36. (c); To go from $y = f(x)$ to $y = f(2x)$, we compress horizontally by a factor of 2. Divide the *x*-coordinate of each point on the graph of $y = f(x)$ by 2. Thus, the point $(4, 2)$ would become $(2, 2)$.

37. $f(x) = x^2 - 1$

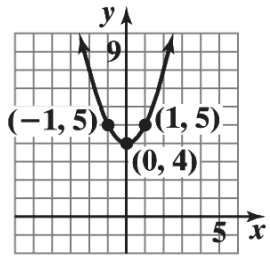
Using the graph of $y = x^2$, vertically shift downward 1 unit.



The domain is $(-\infty, \infty)$ and the range is $[-1, \infty)$.

38. $f(x) = x^2 + 4$

Using the graph of $y = x^2$, vertically shift upward 4 units.



The domain is $(-\infty, \infty)$ and the range is $[4, \infty)$.

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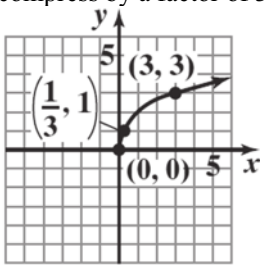
39. $g(x) = \sqrt{3x}$

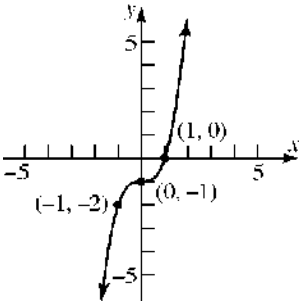
Using the graph of $y = \sqrt{x}$, horizontally compress by a factor of 3.



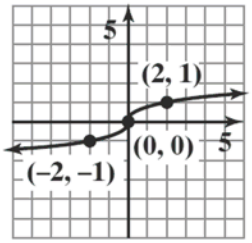
The domain is $[0, \infty)$ and the range is $[0, \infty)$.

40. $g(x) = \sqrt[3]{\frac{1}{2}x}$

Using the graph of $y = \sqrt[3]{x}$, horizontally stretch by a factor of ½.

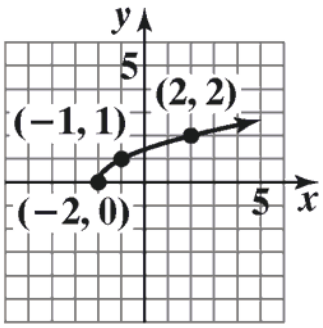


The domain is $(-\infty, \infty)$ and the range is $(-\infty, \infty)$.



41. $h(x) = \sqrt{x+2}$

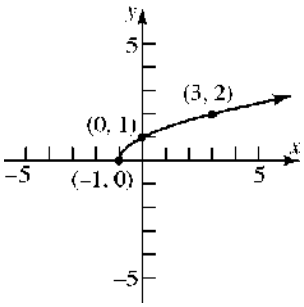
Using the graph of $y = \sqrt{x}$, horizontally shift to the left 2 units.



The domain is $[-2, \infty)$ and the range is $[0, \infty)$.

42. $h(x) = \sqrt{x+1}$

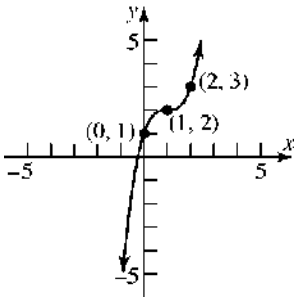
Using the graph of $y = \sqrt{x}$, horizontally shift to the left 1 unit.



The domain is $[-1, \infty)$ and the range is $[0, \infty)$.

43. $f(x) = (x-1)^3 + 2$

Using the graph of $y = x^3$, horizontally shift to the right 1 unit $\left[y = (x-1)^3\right]$, then vertically shift up 2 units $\left[y = (x-1)^3 + 2\right]$.



The domain is $(-\infty, \infty)$ and the range is $(-\infty, \infty)$.

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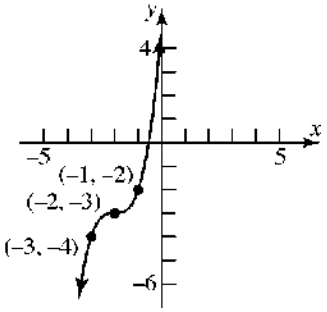
44. $f(x) = (x+2)^3 - 3$

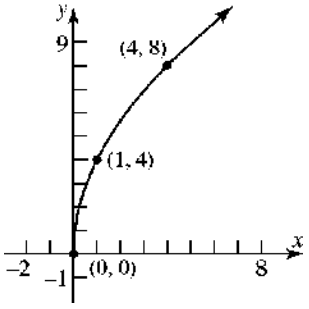
Using the graph of $y = x^3$, horizontally shift to the left 2 units $\left[y = (x+2)^3 \right]$, then vertically shift down 3 units $\left[y = (x+2)^3 - 3 \right]$.



The domain is $(-\infty, \infty)$ and the range is $(-\infty, \infty)$.

45. $g(x) = 4\sqrt{x}$

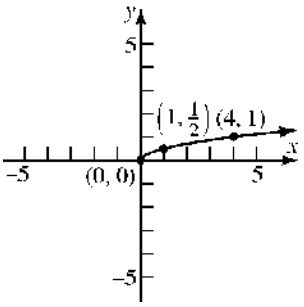
Using the graph of $y = \sqrt{x}$, vertically stretch by a factor of 4.



The domain is $[0, \infty)$ and the range is $[0, \infty)$.

46. $g(x) = \frac{1}{2}\sqrt{x}$

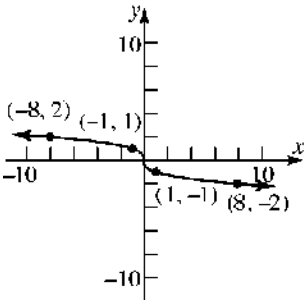
Using the graph of $y = \sqrt{x}$, vertically compress by a factor of $\frac{1}{2}$.



The domain is $[0, \infty)$ and the range is $[0, \infty)$.

47. $f(x) = -\sqrt[3]{x}$

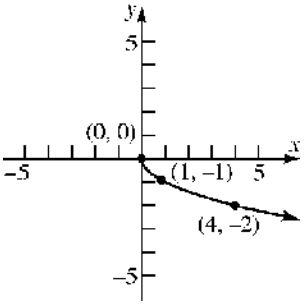
Using the graph of $y = \sqrt[3]{x}$, reflect the graph about the *x*-axis.



The domain is $(-\infty, \infty)$ and the range is $(-\infty, \infty)$.

48. $f(x) = -\sqrt{x}$

Using the graph of $y = \sqrt{x}$, reflect the graph about the *x*-axis.



The domain is $[0, \infty)$ and the range is $(-\infty, 0]$.

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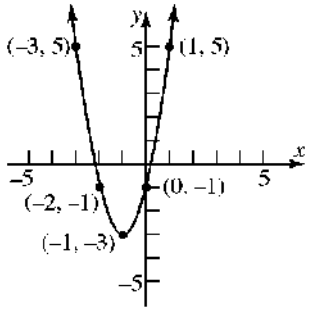
49. $f(x) = 2(x+1)^2 - 3$

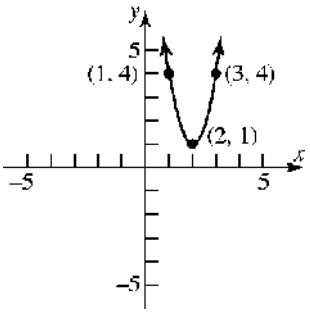
Using the graph of $y = x^2$, horizontally shift to the left 1 unit $\left[y = (x+1)^2 \right]$, vertically stretch by a factor of 2 $\left[y = 2(x+1)^2 \right]$, and then vertically shift downward 3 units $\left[y = 2(x+1)^2 - 3 \right]$.



The domain is $(-\infty, \infty)$ and the range is $[-3, \infty)$.

50. $f(x) = 3(x-2)^2 + 1$

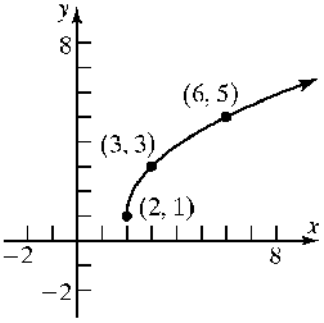
Using the graph of $y = x^2$, horizontally shift to the right 2 units $\left[y = (x-2)^2 \right]$, vertically stretch by a factor of 3 $\left[y = 3(x-2)^2 \right]$, and then vertically shift upward 1 unit $\left[y = 3(x-2)^2 + 1 \right]$.



The domain is $(-\infty, \infty)$ and the range is $[1, \infty)$.

51. $g(x) = 2\sqrt{x-2} + 1$

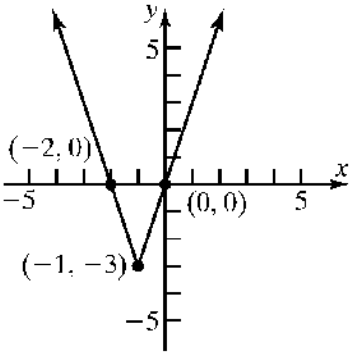
Using the graph of $y = \sqrt{x}$, horizontally shift to the right 2 units $\left[y = \sqrt{x-2} \right]$, vertically stretch by a factor of 2 $\left[y = 2\sqrt{x-2} \right]$, and vertically shift upward 1 unit $\left[y = 2\sqrt{x-2} + 1 \right]$.



The domain is $[2, \infty)$ and the range is $[1, \infty)$.

52. $g(x) = 3|x+1| - 3$

Using the graph of $y = |x|$, horizontally shift to the left 1 unit $\left[y = |x+1| \right]$, vertically stretch by a factor of 3 $\left[y = 3|x+1| \right]$, and vertically shift downward 3 units $\left[y = 3|x+1| - 3 \right]$.



The domain is $(-\infty, \infty)$ and the range is $[-3, \infty)$.

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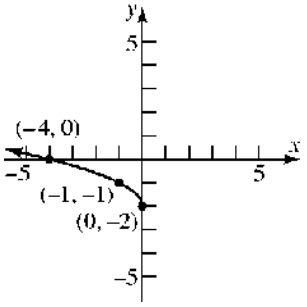
53. $h(x) = \sqrt{-x} - 2$

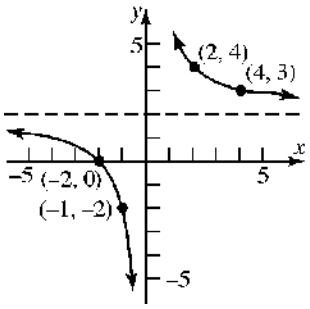
Using the graph of $y = \sqrt{x}$, reflect the graph about the *y*-axis $\left[y = \sqrt{-x} \right]$ and vertically shift downward 2 units $\left[y = \sqrt{-x} - 2 \right]$.



The domain is $(-\infty, 0]$ and the range is $[-2, \infty)$.

54. $h(x) = \frac{4}{x} + 2 = 4\left(\frac{1}{x}\right) + 2$

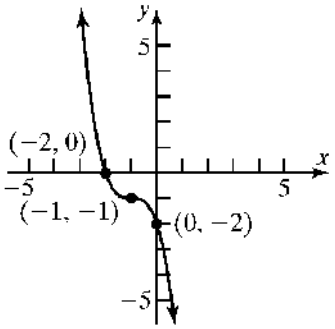
Stretch the graph of $y = \frac{1}{x}$ vertically by a factor of 4 $\left[y = 4 \cdot \frac{1}{x} = \frac{4}{x} \right]$ and vertically shift upward 2 units $\left[y = \frac{4}{x} + 2 \right]$.



The domain is $(-\infty, 0) \cup (0, \infty)$ and the range is $(-\infty, 2) \cup (2, \infty)$.

55. $f(x) = -(x+1)^3 - 1$

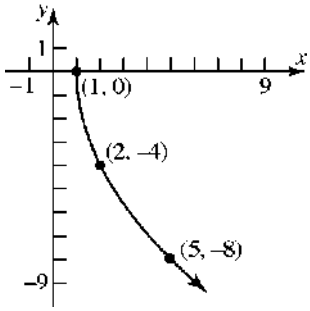
Using the graph of $y = x^3$, horizontally shift to the left 1 unit $\left[y = (x+1)^3 \right]$, reflect the graph about the *x*-axis $\left[y = -(x+1)^3 \right]$, and vertically shift downward 1 unit $\left[y = -(x+1)^3 - 1 \right]$.



The domain is $(-\infty, \infty)$ and the range is $(-\infty, \infty)$.

56. $f(x) = -4\sqrt{x-1}$

Using the graph of $y = \sqrt{x}$, horizontally shift to the right 1 unit $\left[y = \sqrt{x-1} \right]$, reflect the graph about the *x*-axis $\left[y = -\sqrt{x-1} \right]$, and stretch vertically by a factor of 4 $\left[y = -4\sqrt{x-1} \right]$.



The domain is $[1, \infty)$ and the range is $(-\infty, 0]$.

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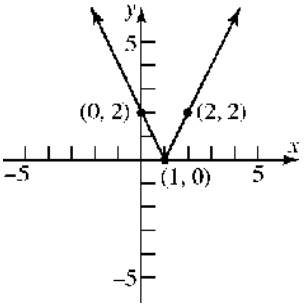
57. $g(x) = 2|1-x| = 2|-(-1+x)| = 2|x-1|$

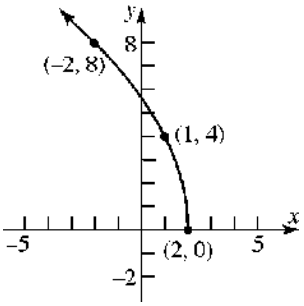
Using the graph of $y = |x|$, horizontally shift to the right 1 unit $\left[y = |x-1|\right]$, and vertically stretch by a factor or 2 $\left[y = 2|x-1|\right]$.



The domain is $(-\infty, \infty)$ and the range is $[0, \infty)$.

58. $g(x) = 4\sqrt{2-x} = 4\sqrt{-(x-2)}$

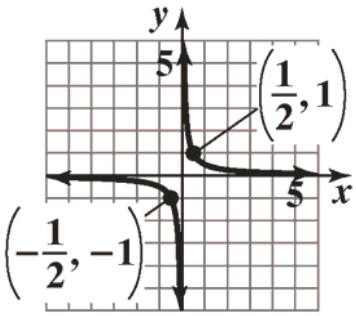
Using the graph of $y = \sqrt{x}$, reflect the graph about the y-axis $\left[y = \sqrt{-x}\right]$, horizontally shift to the right 2 units $\left[y = \sqrt{-(x-2)}\right]$, and vertically stretch by a factor of 4 $\left[y = 4\sqrt{-(x-2)}\right]$.



The domain is $(-\infty, 2]$ and the range is $[0, \infty)$.

59. $h(x) = \dfrac{1}{2x}$

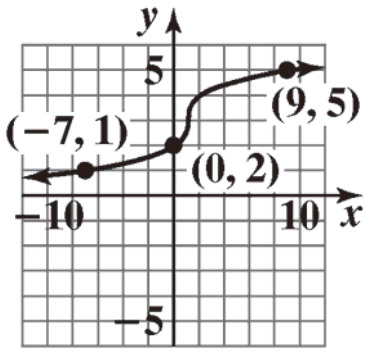
Using the graph of $y = \dfrac{1}{x}$, vertically compress by a factor of $\dfrac{1}{2}$.



The domain is $(-\infty, 0) \cup (0, \infty)$ and the range is $(-\infty, 0) \cup (0, \infty)$.

60. $f(x) = \sqrt[3]{x-1} + 3$

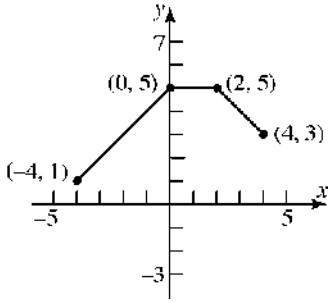
Using the graph of $f(x) = \sqrt[3]{x}$, horizontally shift to the right 1 unit $\left[y = \sqrt[3]{x-1}\right]$, then vertically shift up 3 units $\left[y = \sqrt[3]{x-1} + 3\right]$.



The domain is $(-\infty, \infty)$ and the range is $(-\infty, \infty)$.

61. a. $F(x) = f(x) + 3$

Shift up 3 units.



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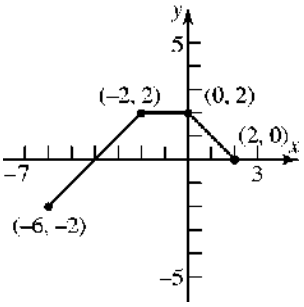
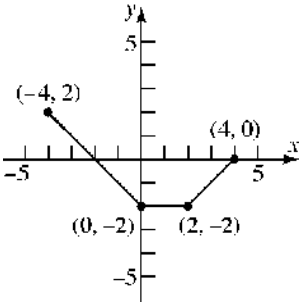
b. $G(x) = f(x+2)$

Shift left 2 units.



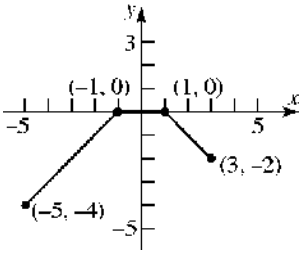
c. $P(x) = -f(x)$

Reflect about the x-axis.



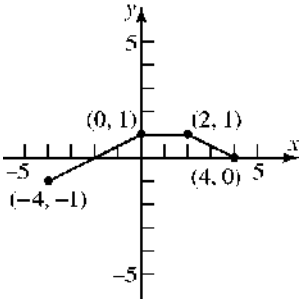
d. $H(x) = f(x+1) - 2$

Shift left 1 unit and shift down 2 units.



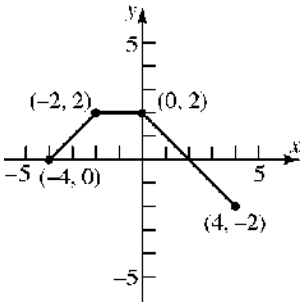
e. $Q(x) = \frac{1}{2} f(x)$

Compress vertically by a factor of $\frac{1}{2}$.



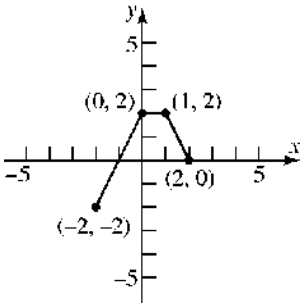
f. $g(x) = f(-x)$

Reflect about the y-axis.



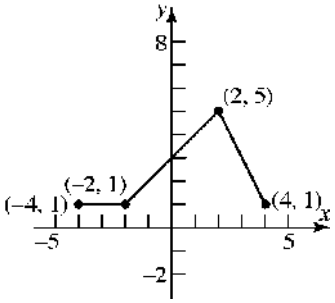
g. $h(x) = f(2x)$

Compress horizontally by a factor of $\frac{1}{2}$.



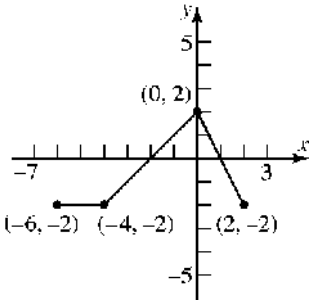
62. a. $F(x) = f(x) + 3$

Shift up 3 units.



b. $G(x) = f(x+2)$

Shift left 2 units.



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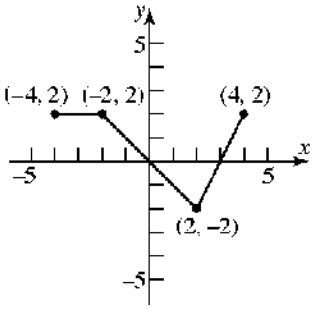
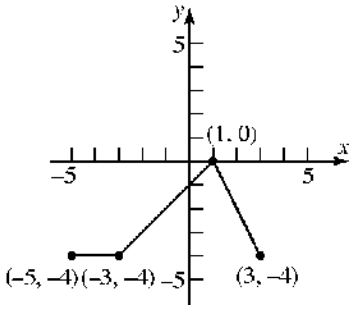
c. $P(x) = -f(x)$

Reflect about the x-axis.



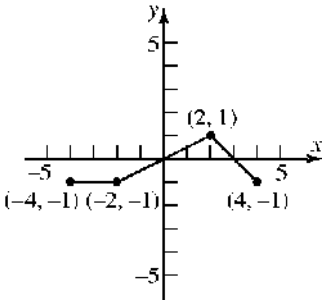
d. $H(x) = f(x+1) - 2$

Shift left 1 unit and shift down 2 units.



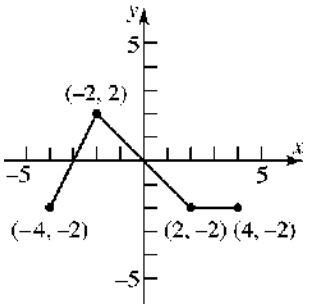
e. $Q(x) = \frac{1}{2} f(x)$

Compress vertically by a factor of $\frac{1}{2}$.



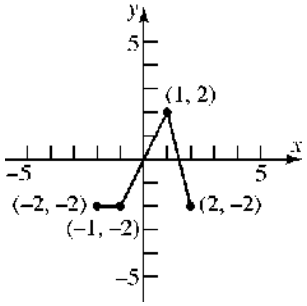
f. $g(x) = f(-x)$

Reflect about the y-axis.



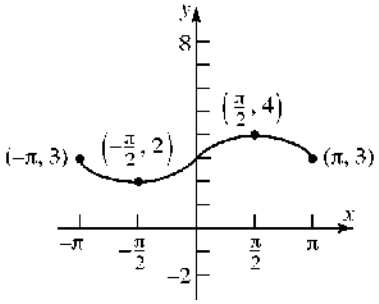
g. $h(x) = f(2x)$

Compress horizontally by a factor of $\frac{1}{2}$.



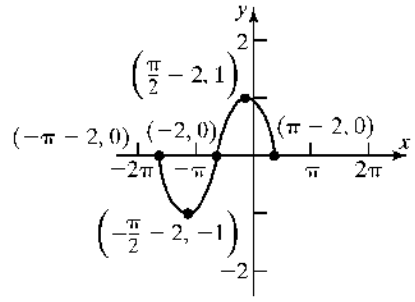
63. a. $F(x) = f(x) + 3$

Shift up 3 units.



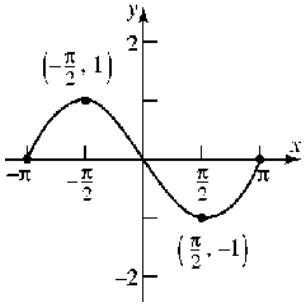
b. $G(x) = f(x+2)$

Shift left 2 units.



c. $P(x) = -f(x)$

Reflect about the x-axis.



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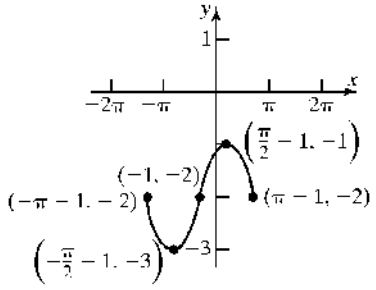
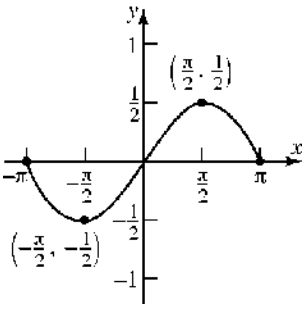
d. $H(x) = f(x+1) - 2$

Shift left 1 unit and shift down 2 units.



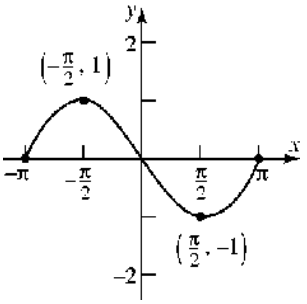
e. $Q(x) = \frac{1}{2} f(x)$

Compress vertically by a factor of $\frac{1}{2}$.



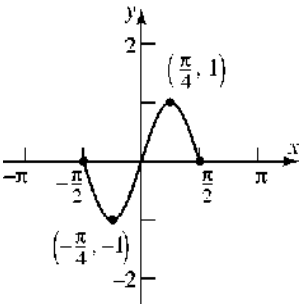
f. $g(x) = f(-x)$

Reflect about the y-axis.



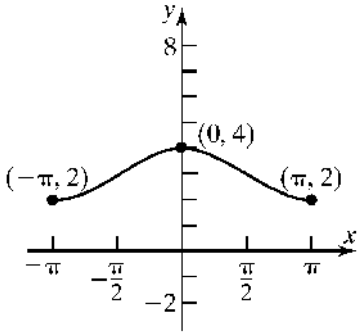
g. $h(x) = f(2x)$

Compress horizontally by a factor of $\frac{1}{2}$.



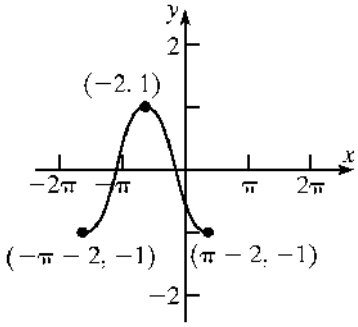
64. a. $F(x) = f(x) + 3$

Shift up 3 units.



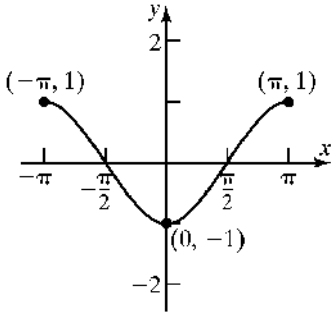
b. $G(x) = f(x+2)$

Shift left 2 units.



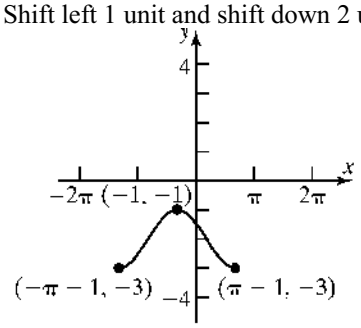
c. $P(x) = -f(x)$

Reflect about the x-axis.



d. $H(x) = f(x+1) - 2$

Shift left 1 unit and shift down 2 units.



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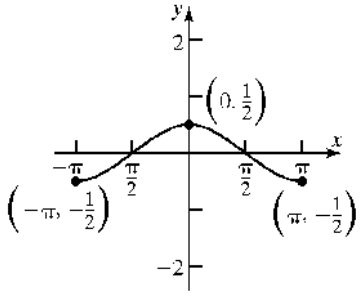
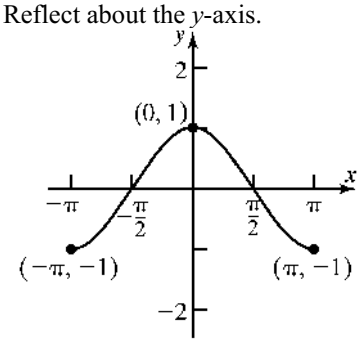
e. $Q(x) = \frac{1}{2} f(x)$

Compress vertically by a factor of $\frac{1}{2}$.



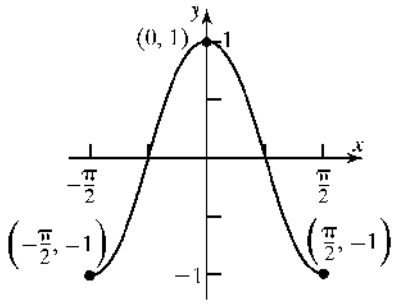
f. $g(x) = f(-x)$

Reflect about the y-axis.



g. $h(x) = f(2x)$

Compress horizontally by a factor of $\frac{1}{2}$.

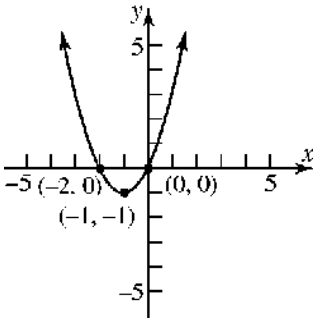


65. $f(x) = x^2 + 2x$

$f(x) = (x^2 + 2x + 1) - 1$

$f(x) = (x+1)^2 - 1$

Using $f(x) = x^2$, shift left 1 unit and shift down 1 unit.

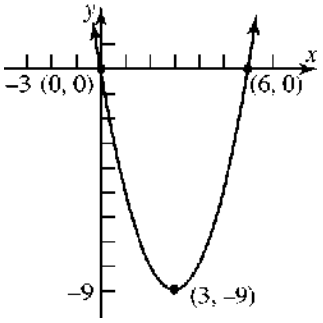


66. $f(x) = x^2 - 6x$

$f(x) = (x^2 - 6x + 9) - 9$

$f(x) = (x-3)^2 - 9$

Using $f(x) = x^2$, shift right 3 units and shift down 9 units.

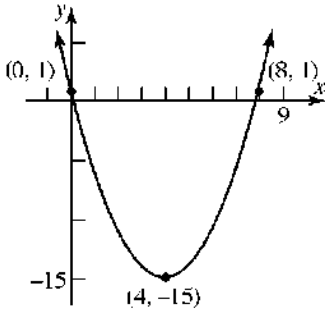


67. $f(x) = x^2 - 8x + 1$

$f(x) = \left(x^2 - 8x + 16\right) + 1 - 16$

$f(x) = (x-4)^2 - 15$

Using $f(x) = x^2$, shift right 4 units and shift down 15 units.



68. $f(x) = x^2 + 4x + 2$

$f(x) = \left(x^2 + 4x + 4\right) + 2 - 4$

$f(x) = (x+2)^2 - 2$

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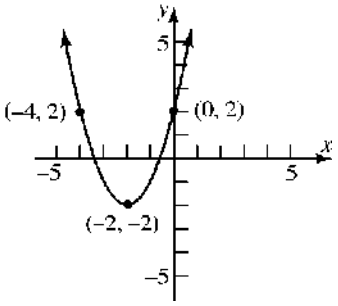
Using $f(x)=x^2$, shift left 2 units and shift down 2 units.



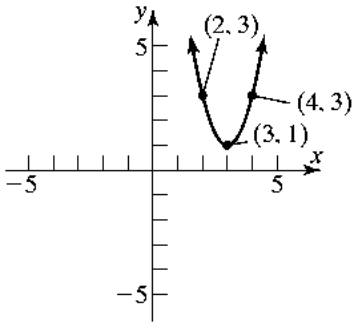
69. $f(x)=2x^2-12x+19$

$=2\left(x^2-6x\right)+19$

$=2\left(x^2-6x+9\right)+19-18$

$=2(x-3)^2+1$

Using $f(x)=x^2$, shift right 3 units, vertically stretch by a factor of 2, and then shift up 1 unit.



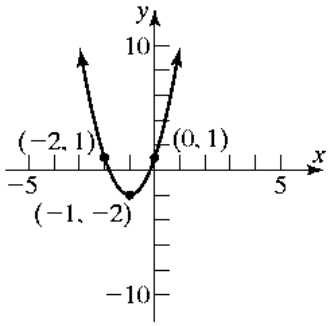
70. $f(x)=3x^2+6x+1$

$=3\left(x^2+2x\right)+1$

$=3\left(x^2+2x+1\right)+1-3$

$=3(x+1)^2-2$

Using $f(x)=x^2$, shift left 1 unit, vertically stretch by a factor of 3, and shift down 2 units.



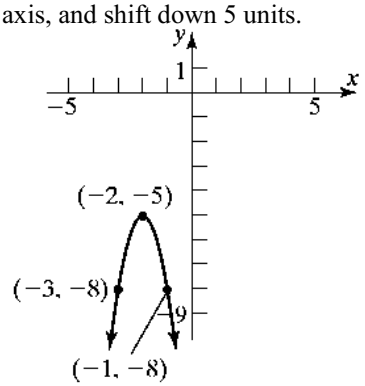
71. $f(x)=-3x^2-12x-17$

$=-3\left(x^2+4x\right)-17$

$=-3\left(x^2+4x+4\right)-17+12$

$=-3(x+2)^2-5$

Using $f(x)=x^2$, shift left 2 units, stretch vertically by a factor of 3, reflect about the x-axis, and shift down 5 units.



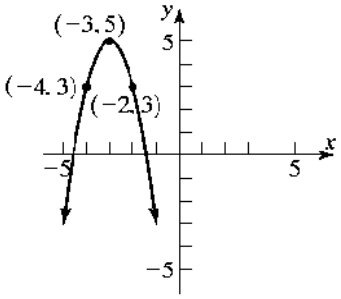
72. $f(x)=-2x^2-12x-13$

$=-2\left(x^2+6x\right)-13$

$=-2\left(x^2+6x+9\right)-13+18$

$=-2(x+3)^2+5$

Using $f(x)=x^2$, shift left 3 units, stretch vertically by a factor of 2, reflect about the x-axis, and shift up 5 units.



73. a. The graph of $y=f(x+2)$ is the same as the graph of $y=f(x)$, but shifted 2 units to the left. Therefore, the x-intercepts are -7 and 1.

b. The graph of $y=f(x-2)$ is the same as the graph of $y=f(x)$, but shifted 2 units to

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the right. Therefore, the *x*-intercepts are -3 and 5.

c. The graph of $y = 4f(x)$ is the same as the graph of $y = f(x)$, but stretched vertically by a factor of 4. Therefore, the *x*-intercepts are still -5 and 3 since the *y*-coordinate of each is 0.

d. The graph of $y = f(-x)$ is the same as the graph of $y = f(x)$, but reflected about the y-axis. Therefore, the *x*-intercepts are 5 and -3.

74. a. The graph of $y = f(x+4)$ is the same as the graph of $y = f(x)$, but shifted 4 units to the left. Therefore, the *x*-intercepts are -12 and -3.

b. The graph of $y = f(x-3)$ is the same as the graph of $y = f(x)$, but shifted 3 units to the right. Therefore, the *x*-intercepts are -5 and 4.

c. The graph of $y = 2f(x)$ is the same as the graph of $y = f(x)$, but stretched vertically by a factor of 2. Therefore, the *x*-intercepts are still -8 and 1 since the *y*-coordinate of each is 0.

d. The graph of $y = f(-x)$ is the same as the graph of $y = f(x)$, but reflected about the *y*-axis. Therefore, the *x*-intercepts are 8 and -1.

75. a. The graph of $y = f(x+2)$ is the same as the graph of $y = f(x)$, but shifted 2 units to the left. Therefore, the graph of $f(x+2)$ is increasing on the interval $[-3,3]$.

b. The graph of $y = f(x-5)$ is the same as the graph of $y = f(x)$, but shifted 5 units to the right. Therefore, the graph of $f(x-5)$ is increasing on the interval $[4,10]$.

c. The graph of $y = -f(x)$ is the same as the graph of $y = f(x)$, but reflected about the *x*-axis. Therefore, we can say that the graph of $y = -f(x)$ must be *decreasing* on the interval $[-1,5]$.

d. The graph of $y = f(-x)$ is the same as the graph of $y = f(x)$, but reflected about the *y*-axis. Therefore, we can say that the graph of $y = f(-x)$ must be *decreasing* on the interval $[-5,1]$.

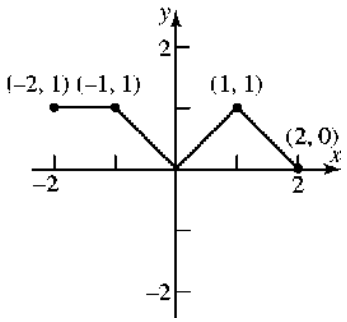
76. a. The graph of $y = f(x+2)$ is the same as the graph of $y = f(x)$, but shifted 2 units to the left. Therefore, the graph of $f(x+2)$ is decreasing on the interval $[-4,5]$.

b. The graph of $y = f(x-5)$ is the same as the graph of $y = f(x)$, but shifted 5 units to the right. Therefore, the graph of $f(x-5)$ is decreasing on the interval $[3,12]$.

c. The graph of $y = -f(x)$ is the same as the graph of $y = f(x)$, but reflected about the *x*-axis. Therefore, we can say that the graph of $y = -f(x)$ must be *increasing* on the interval $[-2,7]$.

d. The graph of $y = f(-x)$ is the same as the graph of $y = f(x)$, but reflected about the *y*-axis. Therefore, we can say that the graph of $y = f(-x)$ must be *increasing* on the interval $[-7,2]$.

77. a. $y = |f(x)|$



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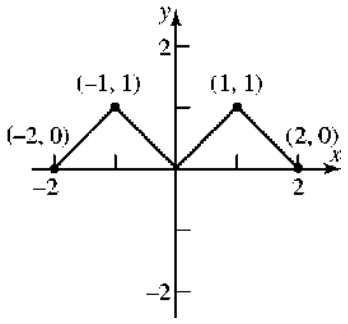
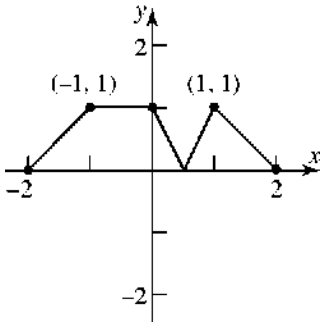
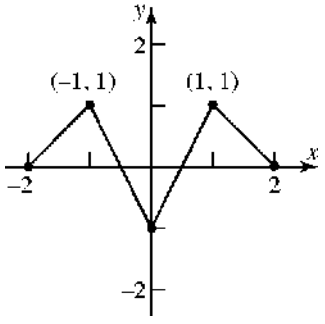
b. $y = f(|x|)$



78. a. To graph $y = |f(x)|$, the part of the graph for *f* that lies in quadrants III or IV is reflected about the *x*-axis.



b. To graph $y = f(|x|)$, the part of the graph for *f* that lies in quadrants II or III is replaced by the reflection of the part in quadrants I and IV reflected about the *y*-axis.



79. a. The graph of $y = f(x+3) - 5$ is the graph of $y = f(x)$ but shifted left 3 units and down 5 units. Thus, the point $(1,3)$ becomes the point $(-2,-2)$.

b. The graph of $y = -2f(x-2) + 1$ is the graph of $y = f(x)$ but shifted right 2 units, stretched vertically by a factor of 2, reflected about the *x*-axis, and shifted up 1 unit. Thus, the point $(1,3)$ becomes the point $(3,-5)$.

c. The graph of $y = f(2x+3)$ is the graph of $y = f(x)$ but shifted left 3 units and horizontally compressed by a factor of 2. Thus, the point $(1,3)$ becomes the point $(-1,3)$.

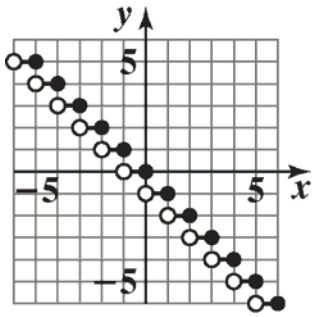
80. a. The graph of $y = g(x+1) - 3$ is the graph of $y = g(x)$ but shifted left 1 unit and down 3 units. Thus, the point $(-3,5)$ becomes the point $(-4,2)$.

b. The graph of $y = -3g(x-4) + 3$ is the graph of $y = g(x)$ but shifted right 4 units, stretched vertically by a factor of 3, reflected about the *x*-axis, and shifted up 3 units. Thus, the point $(-3,5)$ becomes the point $(1,-12)$.

c. The graph of $y = g(3x+9)$ is the graph of $y = f(x)$ but shifted left 9 units and horizontally compressed by a factor of 3. Thus, the point $(-3,5)$ becomes the point $(-4,5)$.

81. a. $f(x) = \text{int}(-x)$

Reflect the graph of $y = \text{int}(x)$ about the *y*-axis.



b. $g(x) = -\text{int}(x)$

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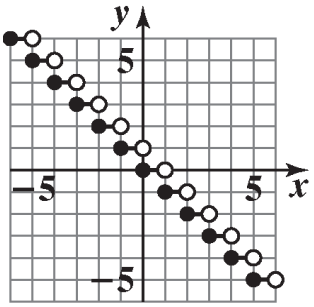
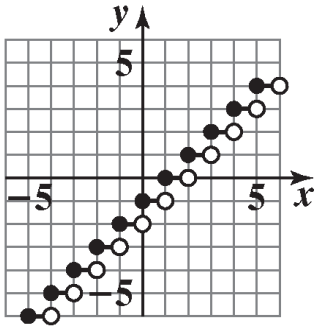
Reflect the graph of $y = \text{int}(x)$ about the x-axis.



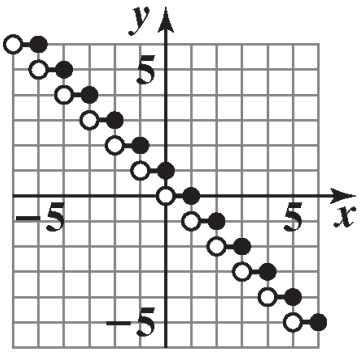
82. a. $f(x) = \text{int}(x-1)$

Shift the graph of $y = \text{int}(x)$ right 1 unit.



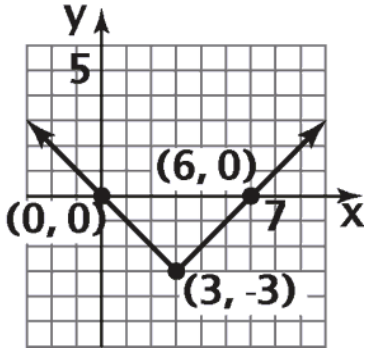
b. $g(x) = \text{int}(1-x) = \text{int}(-(x-1))$

Using the graph of $y = \text{int}(x)$, reflect the graph about the y-axis $\left[y = \text{int}(-x)\right]$, horizontally shift to the right 1 unit $\left[y = \text{int}(-(x-1))\right]$.



83. a. $f(x) = |x-3|-3$

Using the graph of $y = |x|$, horizontally shift to the right 3 units $\left[y = |x-3|\right]$ and vertically shift downward 3 units $\left[y = |x-3|-3\right]$.



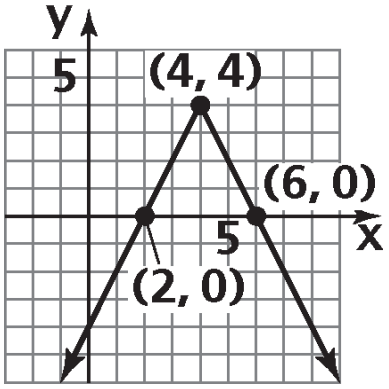
b. $A = \frac{1}{2}bh$

$= \frac{1}{2}(6)(3) = 9$

The area is 9 square units.

84. a. $f(x) = -2|x-4|+4$

Using the graph of $y = |x|$, horizontally shift to the right 4 units $\left[y = |x-4|\right]$, vertically stretch by a factor of 2 and flip on the x-axis $\left[y = -2|x-4|\right]$, and vertically shift upward 4 units $\left[y = -2|x-4|+4\right]$.



b. $A = \frac{1}{2}bh$

$= \frac{1}{2}(4)(4) = 8$

The area is 8 square units.

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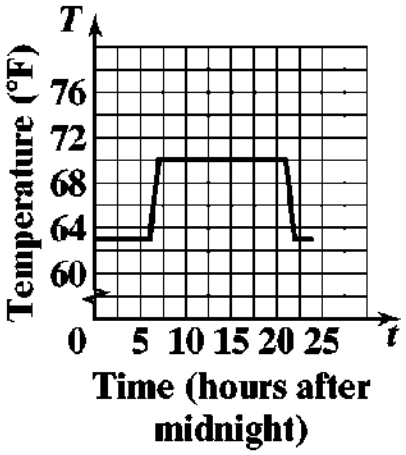
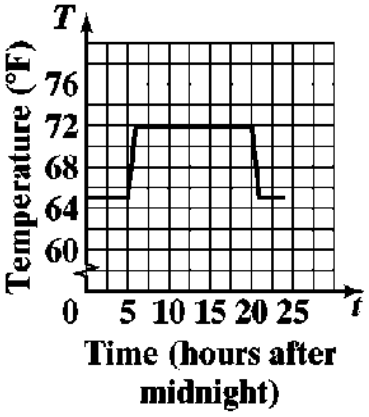
85. a. From the graph, the thermostat is set at 72°F during the daytime hours. The thermostat appears to be set at 65°F overnight.

b. To graph $y = T(t) - 2$, the graph of $T(t)$ is shifted down 2 units. This change will lower the temperature in the house by 2 degrees.



c. To graph $y = T(t+1)$, the graph of $T(t)$ should be shifted left one unit. This change will cause the program to switch between the daytime temperature and overnight temperature one hour sooner. The home will begin warming up at 5am instead of 6am and will begin cooling down at 8pm instead of 9pm.



86. a. $R(0) = 0.15(0)^2 - 0.03(0) + 5.46 = 5.46$

The estimated worldwide music revenue for 2012 is \$5.46 billion.

$R(3) = 0.15(3)^2 - 0.03(3) + 5.46$
$= 6.72$

The estimated worldwide music revenue for 2015 is \$6.72 billion.

$R(5) = 0.15(5)^2 - 0.03(5) + 5.46$
$= 9.06$

The estimated worldwide music revenue for 2017 is \$5.46 billion.

b. $r(x) = R(x-2)$
$= 0.15(x-2)^2 - 0.03(x-2) + 5.46$
$= 0.15(x^2 - 4x + 4) - 0.03(x-2)$
$+ 5.46$
$= 0.15x^2 - 0.6x + 0.6 - 0.03x$
$+ 0.06 + 5.46$
$= 0.15x^2 - 0.63x + 6.12$

c. The graph of $r(x)$ is the graph of $R(x)$ shifted 2 units to the left. Thus, $r(x)$ represents the estimated worldwide music revenue, x years after 2010.

$r(2) = 0.15(2)^2 - 0.63(2) + 6.12 = 5.46$

The estimated worldwide music revenue for 2012 is \$5.46 billion.

$r(5) = 0.15(5)^2 - 0.63(5) + 6.12$
$= 6.72$

The estimated worldwide music revenue for 2015 is \$6.72 billion.

$r(7) = 0.15(7)^2 - 0.63(7) + 6.12$
$= 9.06$

The estimated worldwide music revenue for 2017 is \$9.06 billion.

d. In $r(x)$, x represents the number of years after 2010 (see the previous part).

e. Answers will vary. One advantage might be that it is easier to determine what value should be substituted for x when using $r(x)$ instead of $R(x)$ to estimate worldwide music revenue.

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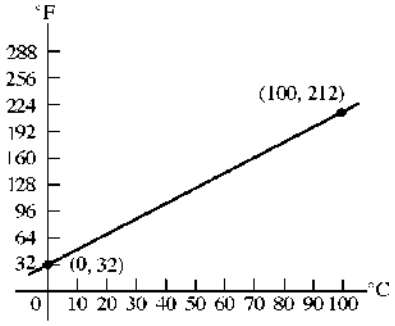
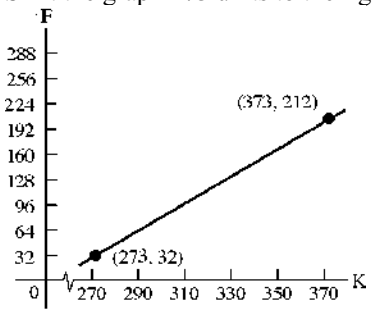
87. $F = \frac{9}{5}C + 32$

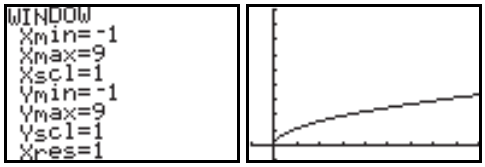


$F = \frac{9}{5}(K - 273) + 32$

Shift the graph 273 units to the right.

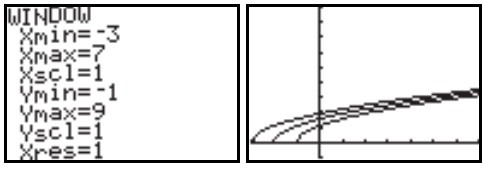


88. a. $T = 2\pi\sqrt{\frac{l}{g}}$



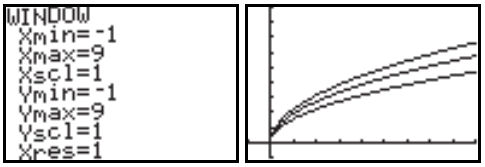
b. $T_1 = 2\pi\sqrt{\frac{l+1}{g}}$; $T_2 = 2\pi\sqrt{\frac{l+2}{g}}$;

$T_3 = 2\pi\sqrt{\frac{l+3}{g}}$



c. As the length of the pendulum increases, the period increases.

d. $T_1 = 2\pi\sqrt{\frac{2l}{g}}$; $T_2 = 2\pi\sqrt{\frac{3l}{g}}$; $T_3 = 2\pi\sqrt{\frac{4l}{g}}$



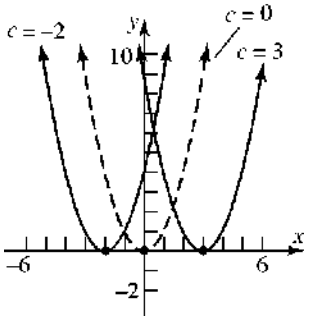
e. If the length of the pendulum is multiplied by k, the period is multiplied by $\sqrt{k}$.

89. $y = (x - c)^2$

If $c = 0$, $y = x^2$.

If $c = 3$, $y = (x - 3)^2$; shift right 3 units.

If $c = -2$, $y = (x + 2)^2$; shift left 2 units.

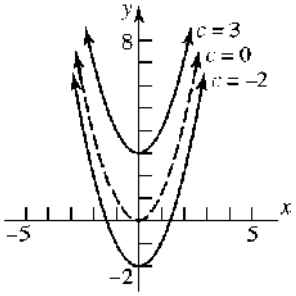


90. $y = x^2 + c$

If $c = 0$, $y = x^2$.

If $c = 3$, $y = x^2 + 3$; shift up 3 units.

If $c = -2$, $y = x^2 - 2$; shift down 2 units.



91. $f(x-5)$ is a shift right 5 units; increasing on $[2,8]$ and $[16,24]$; decreasing of $[8,16]$. $f(2x-5)$ compresses horizontally by a factor of ½; increasing on $[1,4]$ and $[8,12]$; decreasing on $[4,8]$. $-f(2x-5)$ reflects about the x-axis; increasing on $[4,8]$; decreasing on $[1,4]$ and $[8,12]$. $-3f(2x-5)$ stretches vertically by a factor or 3 but does not affect

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increasing/decreasing. Therefore $-3f(2x-5)$ is increasing on $[4,8]$.

92. Write the general normal density as $f(x)=\frac{1}{\sigma}\cdot\frac{1}{\sqrt{2\pi}}\exp\left[-\frac{\left(\frac{x-\mu}{\sigma}\right)^2}{2}\right]$. Starting with the standard normal density, $f(x)=\frac{1}{\sqrt{2\pi}}\exp\left[-\frac{x^2}{2}\right]$, stretch/compress horizontally by a factor of σ to get

$$f(x)=\frac{1}{\sqrt{2\pi}}\exp\left[-\frac{\left(\frac{x}{\sigma}\right)^2}{2}\right]$$

$\left[\text{multiply all the } x\text{-coordinates by } \frac{1}{\sigma}\right]$, then shift the graph horizontally $|\mu|$ units (left if $\mu<0$ and right if $\mu>0$) to get

$$f(x)=\frac{1}{\sqrt{2\pi}}\exp\left[-\frac{\left(\frac{x-\mu}{\sigma}\right)^2}{2}\right].$$ Then stretch/compress vertically by a factor of $\frac{1}{\sigma}$ to get

$$f(x)=\frac{1}{\sigma}\cdot\frac{1}{\sqrt{2\pi}}\exp\left[-\frac{\left(\frac{x-\mu}{\sigma}\right)^2}{2}\right]$$

$\left[\text{multiply all the } y\text{-coordinates by } \frac{1}{\sigma}\right]$.

1. Stretch/compress horizontally by a factor or σ (stretch if $\sigma>1$)
2. Shift horizontally $|\mu|$ units (left if $\mu<0$ and right if $\mu>0$).
3. Stretch/compress vertically by a factor of $\frac{1}{\sigma}$ (compress if $\sigma>1$)

93. The graph of $y=4f(x)$ is a vertical stretch of the graph of f by a factor of 4, while the graph of $y=f(4x)$ is a horizontal compression of the graph of f by a factor of $\frac{1}{4}$.

94. The graph of $y=f(x)-2$ will shift the graph of $y=f(x)$ down by 2 units. The graph of $y=f(x-2)$ will shift the graph of $y=f(x)$ to the right by 2 units.

95. The graph of $y=\sqrt{-x}$ is the graph of $y=\sqrt{x}$ but reflected about the *y*-axis. Therefore, our region is simply rotated about the *y*-axis and does not change shape. Instead of the region being bounded on the right by $x=4$, it is bounded on the left by $x=-4$. Thus, the area of the second region would also be $\frac{16}{3}$ square units.

96. The range of $f(x)=x^2$ is $[0,\infty)$. The graph of $g(x)=f(x)+k$ is the graph of f shifted up k units if k > 0 and shifted down $|k|$ units if k < 0, so the range of g is $[k,\infty)$.

97. The domain of $g(x)=\sqrt{x}$ is $[0,\infty)$. The graph of $g(x-k)$ is the graph of g shifted k units to the right, so the domaine of g is $[k,\infty)$.

98.
$$\begin{aligned}3x-5y&=30\\-5y&=-3x+30\\y&=\frac{3}{5}x-6\end{aligned}$$

The slope is $\frac{3}{5}$ and the y-intercept is -6.

99. The total time run is $\frac{13.1}{7}+\frac{13.1}{2}=8.4214$. The total distance is 26.2 mile. Thus the average speed is $\frac{26.2}{8.4214}=3.11$ mph.

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100. $g = 1.75m$

$g = 1.75(9)$

$= 15.75$ gal

101. $y^2 = x + 4$

x-intercepts:	y-intercepts:
$(0)^2 = x + 4$	$y^2 = 0 + 4$
$0 = x + 4$	$y^2 = 4$
$x = -4$	$y = \pm 2$

The intercepts are $(-4, 0)$, $(0, -2)$ and $(0, 2)$.

Test x-axis symmetry: Let $y = -y$

$(-y)^2 = x + 4$

$y^2 = x + 4$ same

Test y-axis symmetry: Let $x = -x$

$y^2 = -x + 4$ different

Test origin symmetry: Let $x = -x$ and $y = -y$.

$(-y)^2 = -x + 4$

$y^2 = -x + 4$ different

Therefore, the graph will have x-axis symmetry.

102. The denominator must not be zero.

$x^2 - 5x - 14 = 0$

$(x - 7)(x + 2) = 0$

$x = 7, x = -2$

So the domain is: $\{x \mid x \neq 7, x \neq -2\}$

103. $-16t^2 + 96t + 200 = 88$

$-16t^2 + 96t + 112 = 0$

$-16(t^2 - 6t - 7) = 0$

$-16(t - 7)(t + 1) = 0$

$t = 7, t = -1$

Since t represents time the only answer that is reasonable is 7 seconds.

104. $\sqrt[3]{16x^5y^6z} = \sqrt[3]{8 \cdot 2x^3x^2y^6z} = 2xy^2\sqrt[3]{2x^2z}$

105. $\dfrac{f(x+h) - f(x)}{h} =$

$\dfrac{3(x+h)^2 + 2(x+h) - 1 - (3x^2 + 2x - 1)}{h} =$

$\dfrac{3(x^2 + 2xh + h^2) + 2x + 2h - 1 - 3x^2 - 2x + 1}{h} =$

$\dfrac{3x^2 + 6xh + 3h^2 + 2x + 2h - 1 - 3x^2 - 2x + 1}{h}$

$\dfrac{6xh + h^2 + 2h}{h} = \dfrac{h(6x + h + 2)}{h} = 6x + h + 2$

106. $z^3 + 216 = (z)^3 + (6)^3$

$= (z + 6)(z^2 - 6z + 36)$

Section 2.6

1. a. The distance d from P to the origin is $d = \sqrt{x^2 + y^2}$. Since P is a point on the graph of $y = x^2 - 8$, we have:

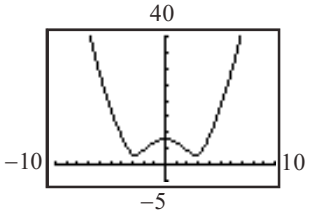
$d(x) = \sqrt{x^2 + (x^2 - 8)^2} = \sqrt{x^4 - 15x^2 + 64}$

b. $d(0) = \sqrt{0^4 - 15(0)^2 + 64} = \sqrt{64} = 8$

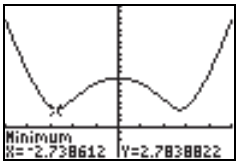
c. $d(1) = \sqrt{(1)^4 - 15(1)^2 + 64}$

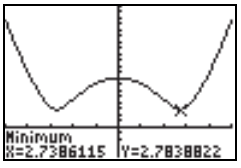
$= \sqrt{1 - 15 + 64} = \sqrt{50} = 5\sqrt{2} \approx 7.07$

d.



e. d is smallest when $x \approx -2.74$ or when $x \approx 2.74$.





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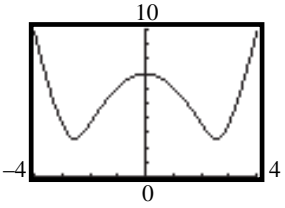
2. a. The distance d from P to $(0, -1)$ is $d = \sqrt{x^2 + (y+1)^2}$. Since P is a point on the graph of $y = x^2 - 8$, we have:

$$d(x) = \sqrt{x^2 + (x^2 - 8 + 1)^2}$$
$$= \sqrt{x^2 + \left(x^2 - 7\right)^2} = \sqrt{x^4 - 13x^2 + 49}$$

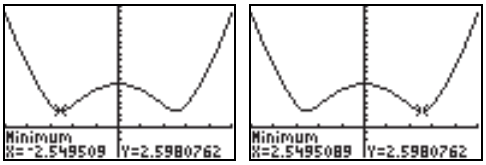
b. $d(0) = \sqrt{0^4 - 13(0)^2 + 49} = \sqrt{49} = 7$

c. $d(-1) = \sqrt{(-1)^4 - 13(-1)^2 + 49} = \sqrt{37} \approx 6.08$

d.



e. d is smallest when $x \approx -2.55$ or when $x \approx 2.55$.

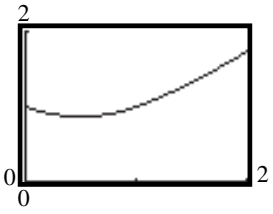


3. a. The distance d from P to the point $(1, 0)$ is $d = \sqrt{(x-1)^2 + y^2}$. Since P is a point on the graph of $y = \sqrt{x}$, we have:

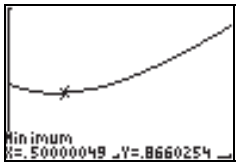
$$d(x) = \sqrt{(x-1)^2 + \left(\sqrt{x}\right)^2} = \sqrt{x^2 - x + 1}$$

where $x \geq 0$.

b.



c. d is smallest when $x = \frac{1}{2}$.

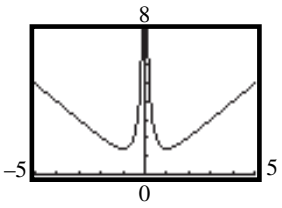


d. $d(x) = \sqrt{\left(\frac{1}{2}\right)^2 - \frac{1}{2} + 1} = \frac{\sqrt{3}}{2}$

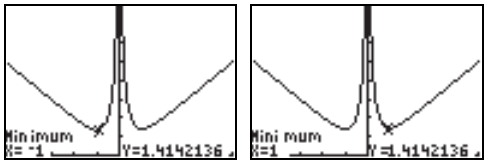
4. a. The distance d from P to the origin is $d = \sqrt{x^2 + y^2}$. Since P is a point on the graph of $y = \frac{1}{x}$, we have:

$$d(x) = \sqrt{x^2 + \left(\frac{1}{x}\right)^2} = \sqrt{x^2 + \frac{1}{x^2}}$$

b.



c. d is smallest when $x = -1$ or $x = 1$.



d.

$$d(1) = \frac{\sqrt{1^2 + 1}}{|1|} = \sqrt{2}; d(-1) = \frac{\sqrt{(-1)^2 + 1}}{|-1|} = \sqrt{2}$$

5. By definition, a triangle has area $A = \frac{1}{2}bh$, b = base, h = height. From the figure, we know that $b = x$ and $h = y$. Expressing the area of the triangle as a function of x, we have:

$$A(x) = \frac{1}{2}xy = \frac{1}{2}x\left(x^3\right) = \frac{1}{2}x^4.$$

6. By definition, a triangle has area $A = \frac{1}{2}bh$, b=base, h = height. Because one vertex of the triangle is at the origin and the other is on the x-axis, we know that $b = x$ and $h = y$. Expressing the area of the triangle as a function of x, we have:

$$A(x) = \frac{1}{2}xy = \frac{1}{2}x\left(9 - x^2\right) = \frac{9}{2}x - \frac{1}{2}x^3.$$

7. a. $A(x) = xy = x\left(16 - x^2\right)$

b. Domain: $\{x \mid 0 < x < 4\}$

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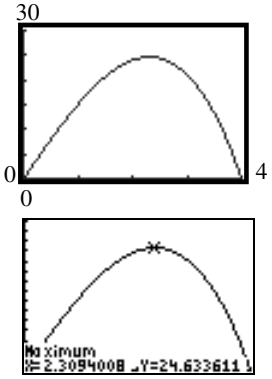
c. The area is largest when $x \approx 2.31$.

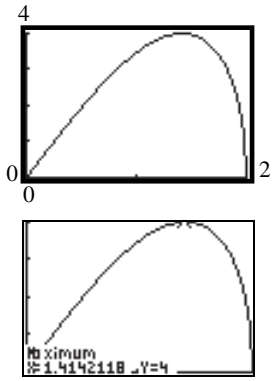


d. The largest area is $A(2.31) = 2.31\left(16 - 2.31^2\right) \approx 24.63$ square units.

8. a. $A(x) = 2xy = 2x\sqrt{4 - x^2}$

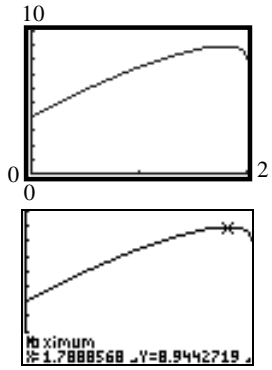
b. $p(x) = 2(2x) + 2(y) = 4x + 2\sqrt{4 - x^2}$

c. Graphing the area equation:



The area is largest when $x \approx 1.41$.

d. Graphing the perimeter equation:



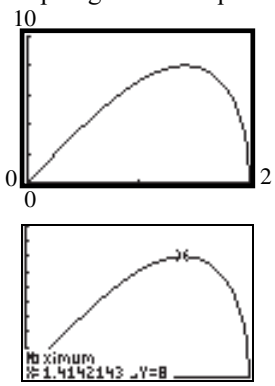
The perimeter is largest when $x \approx 1.79$.

e. The largest area is $A(1.41) = 2(1.41)\sqrt{4 - 1.41^2} \approx 4$ square units.
The largest perimeter is $p(1.79) = 4(1.79) + 2\sqrt{4 - 1.79^2} \approx 8.94$ units.

9. a. In Quadrant I, $x^2 + y^2 = 4 \rightarrow y = \sqrt{4 - x^2}$
$A(x) = (2x)(2y) = 4x\sqrt{4 - x^2}$

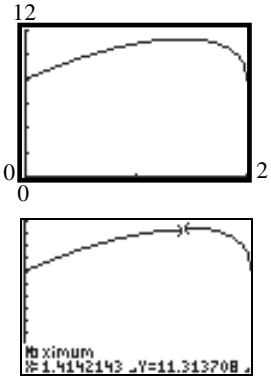
b. $p(x) = 2(2x) + 2(2y) = 4x + 4\sqrt{4 - x^2}$

c. Graphing the area equation:



The area is largest when $x \approx 1.41$.

d. Graphing the perimeter equation:



The perimeter is largest when $x \approx 1.41$.

10. a. $A(r) = (2r)(2r) = 4r^2$

b. $p(r) = 4(2r) = 8r$

11. a. $C =$ circumference, $A =$ total area, $r =$ radius, $x =$ side of square
$C = 2\pi r = 10 - 4x \quad \Rightarrow \quad r = \frac{5 - 2x}{\pi}$

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$$\text{Total Area} = \text{area}_{\text{square}} + \text{area}_{\text{circle}} = x^2 + \pi r^2$$

$$A(x) = x^2 + \pi\left(\frac{5-2x}{\pi}\right)^2 = x^2 + \frac{25-20x+4x^2}{\pi}$$

b. Since the lengths must be positive, we have:

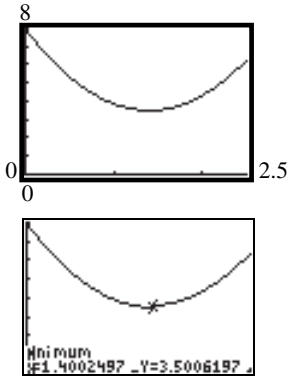
$10-4x>0$ and $x>0$

$-4x>-10$ and $x>0$

$x<2.5$ and $x>0$

Domain: $\{x \mid 0<x<2.5\}$

c. The total area is smallest when $x \approx 1.40$ meters.



12. a. C = circumference, A = total area,
r = radius, x = side of equilateral triangle

$$C = 2\pi r = 10-3x \Rightarrow r = \frac{10-3x}{2\pi}$$

The height of the equilateral triangle is $\frac{\sqrt{3}}{2}x$.

$$\text{Total Area} = \text{area}_{\text{triangle}} + \text{area}_{\text{circle}}$$

$$= \frac{1}{2}x\left(\frac{\sqrt{3}}{2}x\right) + \pi r^2$$

$$A(x) = \frac{\sqrt{3}}{4}x^2 + \pi\left(\frac{10-3x}{2\pi}\right)^2$$

$$= \frac{\sqrt{3}}{4}x^2 + \frac{100-60x+9x^2}{4\pi}$$

b. Since the lengths must be positive, we have:

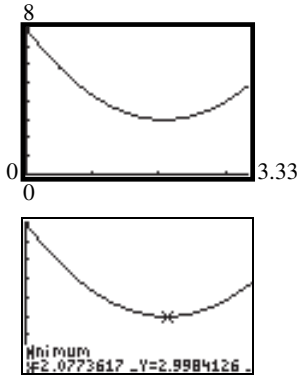
$10-3x>0$ and $x>0$

$-3x>-10$ and $x>0$

$x<\frac{10}{3}$ and $x>0$

Domain: $\left\{x \mid 0<x<\frac{10}{3}\right\}$

c. The area is smallest when $x \approx 2.08$ meters.



13. a. Since the wire of length x is bent into a circle, the circumference is x. Therefore, $C(x) = x$.

b. Since $C = x = 2\pi r$, $r = \frac{x}{2\pi}$.

$$A(x) = \pi r^2 = \pi\left(\frac{x}{2\pi}\right)^2 = \frac{x^2}{4\pi}.$$

14. a. Since the wire of length x is bent into a square, the perimeter is x. Therefore, $p(x) = x$.

b. Since $P = x = 4s$, $s = \frac{1}{4}x$, we have

$$A(x) = s^2 = \left(\frac{1}{4}x\right)^2 = \frac{1}{16}x^2.$$

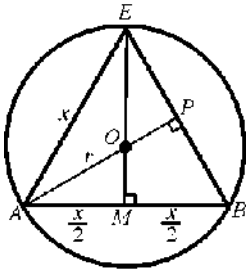
15. a. A = area, r = radius; diameter = $2r$

$A(r) = (2r)(r) = 2r^2$

b. p = perimeter

$p(r) = 2(2r) + 2r = 6r$

16. C = circumference, r = radius;
x = length of a side of the triangle



Since ΔABC is equilateral, $EM = \frac{\sqrt{3}x}{2}$.

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Therefore, $OM = \frac{\sqrt{3}x}{2} - OE = \frac{\sqrt{3}x}{2} - r$

In ΔOAM, $r^2 = \left(\frac{x}{2}\right)^2 + \left(\frac{\sqrt{3}x}{2} - r\right)^2$

$$r^2 = \frac{x^2}{4} + \frac{3}{4}x^2 - \sqrt{3}rx + r^2$$

$$\sqrt{3}rx = x^2$$

$$r = \frac{x}{\sqrt{3}}$$

Therefore, the circumference of the circle is

$$C(x) = 2\pi r = 2\pi\left(\frac{x}{\sqrt{3}}\right) = \frac{2\pi\sqrt{3}}{3}x$$

17. Area of the equilateral triangle

$$A = \frac{1}{2}x \cdot \frac{\sqrt{3}}{2}x = \frac{\sqrt{3}}{4}x^2$$

From problem 16, we have $r^2 = \frac{x^2}{3}$.

Area inside the circle, but outside the triangle:

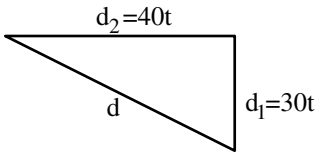
$$A(x) = \pi r^2 - \frac{\sqrt{3}}{4}x^2$$

$$= \pi\frac{x^2}{3} - \frac{\sqrt{3}}{4}x^2 = \left(\frac{\pi}{3} - \frac{\sqrt{3}}{4}\right)x^2$$

18. $d^2 = d_1^2 + d_2^2$

$$d^2 = (30t)^2 + (40t)^2$$

$$d(t) = \sqrt{900t^2 + 1600t^2} = \sqrt{2500t^2} = 50t$$



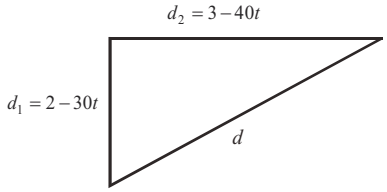
19. a. $d^2 = d_1^2 + d_2^2$

$$d^2 = (2 - 30t)^2 + (3 - 40t)^2$$

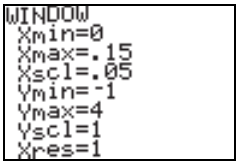
$$d(t) = \sqrt{(2 - 30t)^2 + (3 - 40t)^2}$$

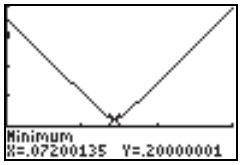
$$= \sqrt{4 - 120t + 900t^2 + 9 - 240t + 1600t^2}$$

$$= \sqrt{2500t^2 - 360t + 13}$$



b. The distance is smallest at $t \approx 0.07$ hours.





20. r = radius of cylinder, h = height of cylinder, V = volume of cylinder

$$r^2 + \left(\frac{h}{2}\right)^2 = R^2 \Rightarrow r^2 + \frac{h^2}{4} = R^2 \Rightarrow r^2 = R^2 - \frac{h^2}{4}$$

$$V = \pi r^2 h$$

$$V(h) = \pi\left(R^2 - \frac{h^2}{4}\right)h = \pi h\left(R^2 - \frac{h^2}{4}\right)$$

21. r = radius of cylinder, h = height of cylinder, V = volume of cylinder

By similar triangles: $\frac{H}{R} = \frac{H - h}{r}$

$$Hr = R(H - h)$$

$$Hr = RH - Rh$$

$$Rh = RH - Hr$$

$$h = \frac{RH - Hr}{R} = \frac{H(R - r)}{R}$$

$$V(r) = \pi r^2 h = \pi r^2\left(\frac{H(R - r)}{R}\right) = \frac{\pi H(R - r)r^2}{R}$$

22. a. The total cost of installing the cable along the road is $500x$. If cable is installed x miles along the road, there are $5 - x$ miles between the road to the house and where the cable ends along the road.

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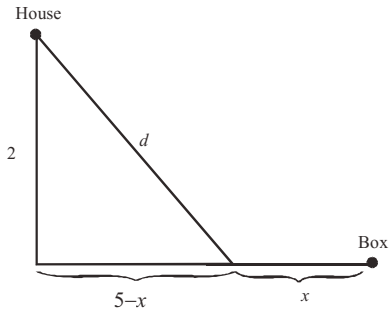


$d = \sqrt{(5-x)^2 + 2^2}$

$= \sqrt{25 - 10x + x^2 + 4} = \sqrt{x^2 - 10x + 29}$

The total cost of installing the cable is:

$C(x) = 500x + 700\sqrt{x^2 - 10x + 29}$

Domain: $\{x \mid 0 \le x \le 5\}$

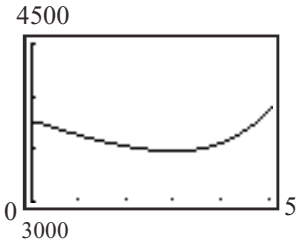
b. $C(1) = 500(1) + 700\sqrt{1^2 - 10(1) + 29}$

$= 500 + 700\sqrt{20} = \$3630.50$

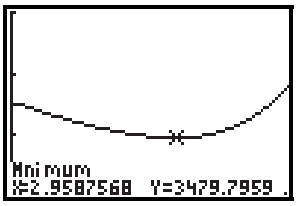
c. $C(3) = 500(3) + 700\sqrt{3^2 - 10(3) + 29}$

$= 1500 + 700\sqrt{8} = \$3479.90$

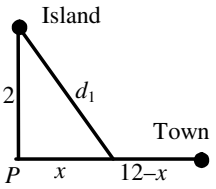
d.



e. Using MINIMUM, the graph indicates that $x \approx 2.96$ miles results in the least cost.



23. a. The time on the boat is given by $\frac{d_1}{3}$. The time on land is given by $\frac{12-x}{5}$.



$d_1 = \sqrt{x^2 + 2^2} = \sqrt{x^2 + 4}$

The total time for the trip is:

$T(x) = \frac{12-x}{5} + \frac{d_1}{3} = \frac{12-x}{5} + \frac{\sqrt{x^2+4}}{3}$

b. Domain: $\{x \mid 0 \le x \le 12\}$

c. $T(4) = \frac{12-4}{5} + \frac{\sqrt{4^2+4}}{3}$

$= \frac{8}{5} + \frac{\sqrt{20}}{3} \approx 3.09$ hours

d. $T(8) = \frac{12-8}{5} + \frac{\sqrt{8^2+4}}{3}$

$= \frac{4}{5} + \frac{\sqrt{68}}{3} \approx 3.55$ hours

24. a. Let A = amount of material, x = length of the base, h = height, and V = volume.

$V = x^2 h = 10 \Rightarrow h = \frac{10}{x^2}$

Total Area $A = (\text{Area}_{\text{base}}) + (4)(\text{Area}_{\text{side}})$

$= x^2 + 4xh$

$= x^2 + 4x\left(\frac{10}{x^2}\right)$

$= x^2 + \frac{40}{x}$

$A(x) = x^2 + \frac{40}{x}$

b. $A(1) = 1^2 + \frac{40}{1} = 1 + 40 = 41 \text{ ft}^2$

c. $A(2) = 2^2 + \frac{40}{2} = 4 + 20 = 24 \text{ ft}^2$

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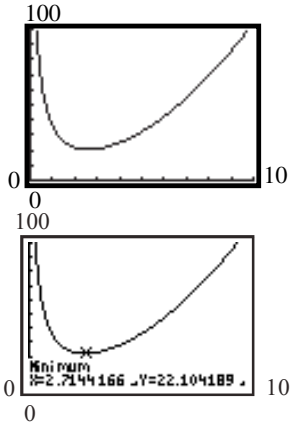
d. $y_1 = x^2 + \dfrac{40}{x}$



The amount of material is least when $x = 2.71$ ft.

e. The largest area is

$$A(2.71) = 2.71^2 + \frac{40}{2.71} = 22.1 \text{ ft}^2$$

25. **a.** length = $24 - 2x$; width = $24 - 2x$; height = x

$$V(x) = x(24-2x)(24-2x) = x(24-2x)^2$$

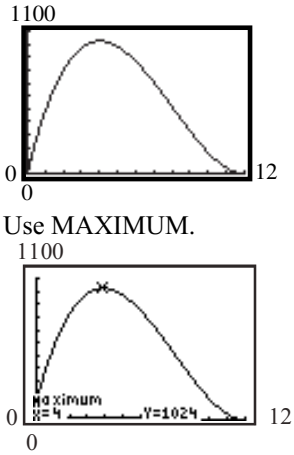
b. $V(3) = 3(24-2(3))^2 = 3(18)^2$

$= 3(324) = 972 \text{ in}^3.$

c. $V(10) = 10(24-2(10))^2 = 10(4)^2$

$= 10(16) = 160 \text{ in}^3.$

d. $y_1 = x(24-2x)^2$



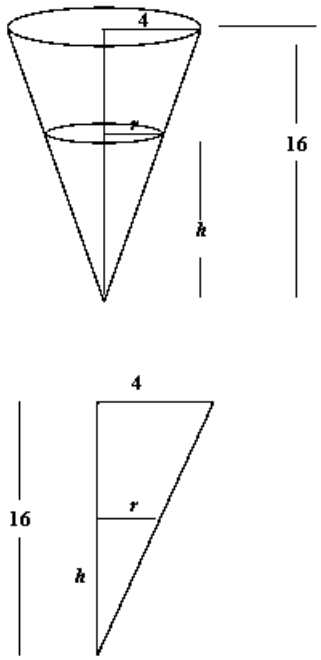
Use MAXIMUM.

The volume is largest when $x = 4$ inches.

e. The largest volume is

$$V(4) = 4(24-2(4))^2 = 1024 \text{ in}^3$$

26. Consider the diagrams shown below.



There is a pair of similar triangles in the diagram. This allows us to write

$$\frac{r}{h} = \frac{4}{16} \Rightarrow \frac{r}{h} = \frac{1}{4} \Rightarrow r = \frac{1}{4}h$$

Substituting into the volume formula for the conical portion of water gives

$$V(h) = \frac{1}{3}\pi r^2 h = \frac{1}{3}\pi\left(\frac{1}{4}h\right)^2 h = \frac{\pi}{48}h^3.$$

27. **a.** The total cost is the sum of the shipment cost, storage cost, and product cost. Since each shipment will contain x units, there are $600/x$ shipments per year, each costing \$15. So the shipment cost is $15\left(\dfrac{600}{x}\right) = \left(\dfrac{9000}{x}\right)$.

The storage cost for the year is given as $1.60x$. The product costs is $600(4.85) = 2910$. So, the total cost is

$$C(x) = \frac{9000}{x} + 1.60x + 2910.$$

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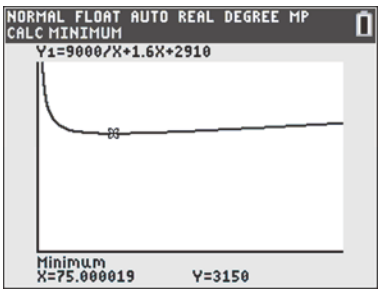
b.



The retailer should order 75 drives per order for a minimum yearly cost of $3150.

28. $|2x-3|-5=-2$

$|2x-3|=3$

$2x-3=-3$ or $2x-3=3$

$2x=0$ or $2x=6$

$x=0$ or $x=3$

The solution set is $\{0,3\}$.

29. In order for the 16-foot long Ford Fusion to pass the 50-foot truck, the Ford Fusion must travel the length of the truck and the length of itself in the time frame of 5 seconds. Thus the Fusion must travel an additional 66 feet in 5 seconds.

Convert this to miles-per-hour.

$5 \text{ sec} = \frac{5}{60} \text{ min} = \frac{5}{3600} \text{ hr} = \frac{1}{720} \text{ hr.}$

$66 \text{ ft} = \frac{66}{5280} \text{ mi}$

$\text{speed} = \frac{\text{distance}}{\text{time}} = \frac{\frac{66}{5280}}{\frac{1}{720}} = 9 \text{ mph}$

Since the truck is traveling 55 mph, the Fusion must travel 55 + 9 = 64 mph.

30. $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{6-(-2)}{1-3} = \frac{8}{-2} = -4$

31. $\frac{10}{4} = \frac{14}{x}$

$10x = 4(14)$

$10x = 56$

$x = 5.6$

32. $x = u - 1$

$y = \frac{u-1}{u-1+1} = \frac{u-1}{u}$

33. $\frac{x+5}{3x^{2/3}} + x^{1/3} = \frac{x+5}{3x^{2/3}} + \frac{3x}{3x^{2/3}}$

$= \frac{x+5+3x}{3x^{2/3}}$

$= \frac{4x+5}{3x^{2/3}}$

34. $-\sqrt{3x-2} \geq 4$

$\sqrt{3x-2} \leq -4$

No solution since a square root cannot be negative.

35. Since the graph is symmetric is symmetric about the origin then (3, -2) is symmetric to (-3, 2).

36. $v = \frac{2.6t}{d^2}\sqrt{\frac{E}{P}}$

$\frac{vd^2}{2.6t} = \sqrt{\frac{E}{P}}$

$\left(\frac{vd^2}{2.6t}\right)^2 = \frac{E}{P}$

$\frac{v^2d^4}{6.76t^2} = \frac{E}{P}$

$\frac{Pv^2d^4}{6.76t^2} = E$

$P = \frac{6.76t^2E}{v^2d^4}$

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37. $3x^2 - 7x = 4x - 2$

$3x^2 - 11x + 2 = 0$

$b^2 - 4ac = (-11)^2 - 4(3)(2)$

$= 121 - 24 = 97$

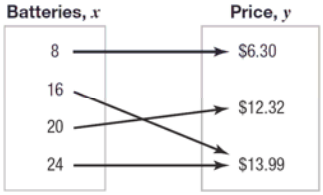
Chapter 2 Review Exercises

1. a. Domain {8, 16, 20, 24}

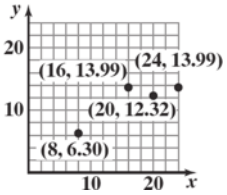
Range {\$6.30, \$12.32, \$13.99}

b. {(8,\$6.30), (16,\$13.99), (20,\$12.32), (24,\$13.99)}

c.



d.



2. This relation represents a function.
Domain = {–1, 2, 4}; Range = {0, 3}.

3. Domain {2,4}; Range {-1,1,2}
Not a function

4. not a function; domain [-1, 3]; range [-2, 2]

5. function; domain: all real numbers; range $[-3, \infty)$

6. $f(x) = \dfrac{3x}{x^2 - 1}$

a. $f(2) = \dfrac{3(2)}{(2)^2 - 1} = \dfrac{6}{4-1} = \dfrac{6}{3} = 2$

b. $f(-2) = \dfrac{3(-2)}{(-2)^2 - 1} = \dfrac{-6}{4-1} = \dfrac{-6}{3} = -2$

c. $f(-x) = \dfrac{3(-x)}{(-x)^2 - 1} = \dfrac{-3x}{x^2 - 1}$

d. $-f(x) = -\left(\dfrac{3x}{x^2 - 1}\right) = \dfrac{-3x}{x^2 - 1}$

e. $f(x-2) = \dfrac{3(x-2)}{(x-2)^2 - 1}$

$= \dfrac{3x - 6}{x^2 - 4x + 4 - 1} = \dfrac{3(x-2)}{x^2 - 4x + 3}$

f. $f(2x) = \dfrac{3(2x)}{(2x)^2 - 1} = \dfrac{6x}{4x^2 - 1}$

7. $f(x) = \sqrt{x^2 - 4}$

a. $f(2) = \sqrt{2^2 - 4} = \sqrt{4-4} = \sqrt{0} = 0$

b. $f(-2) = \sqrt{(-2)^2 - 4} = \sqrt{4-4} = \sqrt{0} = 0$

c. $f(-x) = \sqrt{(-x)^2 - 4} = \sqrt{x^2 - 4}$

d. $-f(x) = -\sqrt{x^2 - 4}$

e. $f(x-2) = \sqrt{(x-2)^2 - 4}$

$= \sqrt{x^2 - 4x + 4 - 4}$

$= \sqrt{x^2 - 4x}$

f. $f(2x) = \sqrt{(2x)^2 - 4} = \sqrt{4x^2 - 4}$

$= \sqrt{4\left(x^2 - 1\right)} = 2\sqrt{x^2 - 1}$

8. $f(x) = \dfrac{x^2 - 4}{x^2}$

a. $f(2) = \dfrac{2^2 - 4}{2^2} = \dfrac{4-4}{4} = \dfrac{0}{4} = 0$

b. $f(-2) = \dfrac{(-2)^2 - 4}{(-2)^2} = \dfrac{4-4}{4} = \dfrac{0}{4} = 0$

c. $f(-x) = \dfrac{(-x)^2 - 4}{(-x)^2} = \dfrac{x^2 - 4}{x^2}$

d. $-f(x) = -\left(\dfrac{x^2 - 4}{x^2}\right) = \dfrac{4 - x^2}{x^2} = -\dfrac{x^2 - 4}{x^2}$

e. $f(x-2) = \dfrac{(x-2)^2 - 4}{(x-2)^2} = \dfrac{x^2 - 4x + 4 - 4}{(x-2)^2}$

$= \dfrac{x^2 - 4x}{(x-2)^2} = \dfrac{x(x-4)}{(x-2)^2}$

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f. $f(2x)=\dfrac{(2x)^2-4}{(2x)^2}=\dfrac{4x^2-4}{4x^2}$

$=\dfrac{4\left(x^2-1\right)}{4x^2}=\dfrac{x^2-1}{x^2}$

9. $f(x)=\dfrac{x}{x^2-9}$

The denominator cannot be zero:

$x^2-9\neq 0$

$(x+3)(x-3)\neq 0$

$x\neq -3$ or 3

Domain: $\{x\,|\,x\neq -3,\ x\neq 3\}$

10. $f(x)=\sqrt{2-x}$

The radicand must be non-negative:

$2-x\geq 0$

$x\leq 2$

Domain: $\{x\,|\,x\leq 2\}$ or $(-\infty,2]$

11. $g(x)=\dfrac{|x|}{x}$

The denominator cannot be zero:

$x\neq 0$

Domain: $\{x\,|\,x\neq 0\}$

12. $f(x)=\dfrac{x}{x^2+2x-3}$

The denominator cannot be zero:

$x^2+2x-3\neq 0$

$(x+3)(x-1)\neq 0$

$x\neq -3$ or 1

Domain: $\{x\,|\,x\neq -3,\ x\neq 1\}$

13. $f(x)=\dfrac{\sqrt{x+1}}{x^2-4}$

The denominator cannot be zero:

$x^2-4\neq 0$

$(x+2)(x-2)\neq 0$

$x\neq -2$ or 2

Also, the radicand must be non-negative:

$x+1\geq 0$

$x\geq -1$

Domain: $[-1,2)\cup(2,\infty)$

14. $f(x)=\dfrac{x}{\sqrt{x+8}}$

The radicand must be non-negative and not zero:

$x+8>0$

$x>-8$

Domain: $\{x\,|\,x>-8\}$

15. $f(x)=2-x \quad g(x)=3x+1$

$(f+g)(x)=f(x)+g(x)$

$=2-x+3x+1=2x+3$

Domain: $\{x\,|\,x$ is any real number$\}$

$(f-g)(x)=f(x)-g(x)$

$=2-x-(3x+1)$

$=2-x-3x-1$

$=-4x+1$

Domain: $\{x\,|\,x$ is any real number$\}$

$(f\cdot g)(x)=f(x)\cdot g(x)$

$=(2-x)(3x+1)$

$=6x+2-3x^2-x$

$=-3x^2+5x+2$

Domain: $\{x\,|\,x$ is any real number$\}$

$\left(\dfrac{f}{g}\right)(x)=\dfrac{f(x)}{g(x)}=\dfrac{2-x}{3x+1}$

$3x+1\neq 0$

$3x\neq -1\Rightarrow x\neq -\dfrac{1}{3}$

Domain: $\left\{x\,\middle|\,x\neq -\dfrac{1}{3}\right\}$

16. $f(x)=3x^2+x+1 \qquad g(x)=3x$

$(f+g)(x)=f(x)+g(x)$

$=3x^2+x+1+3x$

$=3x^2+4x+1$

Domain: $\{x\,|\,x$ is any real number$\}$

$(f-g)(x)=f(x)-g(x)$

$=3x^2+x+1-3x$

$=3x^2-2x+1$

Domain: $\{x\,|\,x$ is any real number$\}$

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$$(f \cdot g)(x) = f(x) \cdot g(x)$$
$$= (3x^2 + x + 1)(3x)$$
$$= 9x^3 + 3x^2 + 3x$$

Domain: $\{x \mid x \text{ is any real number}\}$

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{3x^2 + x + 1}{3x}$$

$3x \neq 0 \Rightarrow x \neq 0$

Domain: $\{x \mid x \neq 0\}$

17. $f(x) = \dfrac{x+1}{x-1} \qquad g(x) = \dfrac{1}{x}$

$$(f+g)(x) = f(x) + g(x)$$
$$= \frac{x+1}{x-1} + \frac{1}{x} = \frac{x(x+1)+1(x-1)}{x(x-1)}$$
$$= \frac{x^2 + x + x - 1}{x(x-1)} = \frac{x^2 + 2x - 1}{x(x-1)}$$

Domain: $\{x \mid x \neq 0, x \neq 1\}$

$$(f-g)(x) = f(x) - g(x)$$
$$= \frac{x+1}{x-1} - \frac{1}{x} = \frac{x(x+1)-1(x-1)}{x(x-1)}$$
$$= \frac{x^2 + x - x + 1}{x(x-1)} = \frac{x^2 + 1}{x(x-1)}$$

Domain: $\{x \mid x \neq 0, x \neq 1\}$

$$(f \cdot g)(x) = f(x) \cdot g(x) = \left(\frac{x+1}{x-1}\right)\left(\frac{1}{x}\right) = \frac{x+1}{x(x-1)}$$

Domain: $\{x \mid x \neq 0, x \neq 1\}$

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{\frac{x+1}{x-1}}{\frac{1}{x}} = \left(\frac{x+1}{x-1}\right)\left(\frac{x}{1}\right) = \frac{x(x+1)}{x-1}$$

Domain: $\{x \mid x \neq 0, x \neq 1\}$

18. $f(x) = -2x^2 + x + 1$

$$\frac{f(x+h) - f(x)}{h}$$
$$= \frac{-2(x+h)^2 + (x+h) + 1 - (-2x^2 + x + 1)}{h}$$
$$= \frac{-2(x^2 + 2xh + h^2) + x + h + 1 + 2x^2 - x - 1}{h}$$
$$= \frac{-2x^2 - 4xh - 2h^2 + x + h + 1 + 2x^2 - x - 1}{h}$$
$$= \frac{-4xh - 2h^2 + h}{h} = \frac{h(-4x - 2h + 1)}{h}$$
$$= -4x - 2h + 1$$

19. **a.** Domain: $\{x \mid -4 \le x \le 3\}$; $[-4, 3]$

Range: $\{y \mid -3 \le y \le 3\}$; $[-3, 3]$

b. Intercept: $(0, 0)$

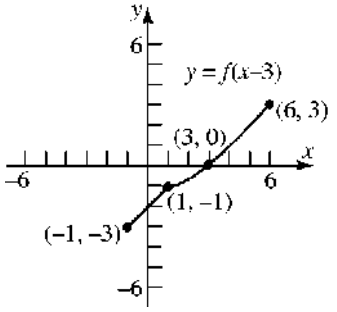
c. $f(-2) = -1$

d. $f(x) = -3$ when $x = -4$

e. $f(x) > 0$ when $0 < x \le 3$

$\{x \mid 0 < x \le 3\}$

f. To graph $y = f(x-3)$, shift the graph of f horizontally 3 units to the right.



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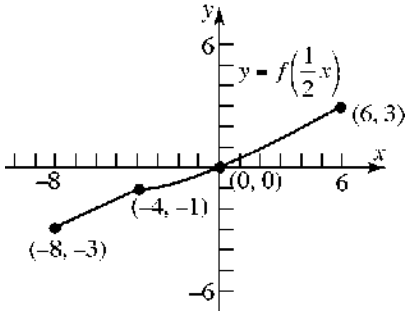
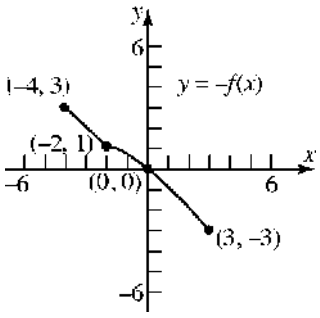
g. To graph $y = f\left(\frac{1}{2}x\right)$, stretch the graph of f horizontally by a factor of 2.



h. To graph $y = -f(x)$, reflect the graph of f vertically about the y-axis.



20. a. Domain: $(-\infty, 4]$
Range: $(-\infty, 3]$

b. Increasing: $(-\infty, -2]$ and $[2, 4]$;
Decreasing: $[-2, 2]$

c. Local minimum is -1 at $x = 2$;
Local maximum is 1 at $x = -2$

d. No absolute minimum;
Absolute maximum is 3 at $x = 4$

e. The graph has no symmetry.

f. The function is neither.

g. x-intercepts: $(-3, 0), (0, 0), (3, 0)$;
y-intercept: (0,0)

21. $f(x) = x^3 - 4x$

$f(-x) = (-x)^3 - 4(-x) = -x^3 + 4x$

$= -\left(x^3 - 4x\right) = -f(x)$

f is odd.

22. $g(x) = \dfrac{4 + x^2}{1 + x^4}$

$g(-x) = \dfrac{4 + (-x)^2}{1 + (-x)^4} = \dfrac{4 + x^2}{1 + x^4} = g(x)$

g is even.

23. $G(x) = 1 - x + x^3$

$G(-x) = 1 - (-x) + (-x)^3$

$= 1 + x - x^3 \neq -G(x)$ or $G(x)$

G is neither even nor odd.

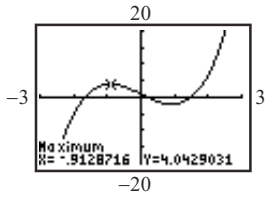
24. $f(x) = \dfrac{x}{1 + x^2}$

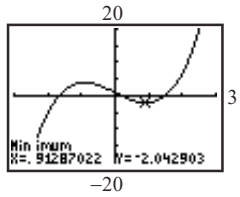
$f(-x) = \dfrac{-x}{1 + (-x)^2} = \dfrac{-x}{1 + x^2} = -f(x)$

f is odd.

25. $f(x) = 2x^3 - 5x + 1$ on the interval $(-3, 3)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = 2x^3 - 5x + 1$.

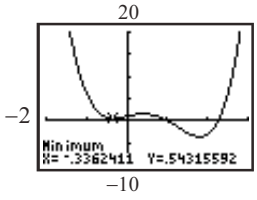


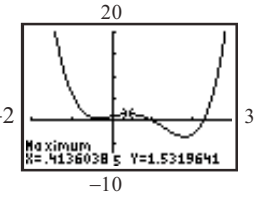


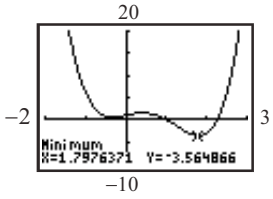
local maximum value: 4.04 when $x \approx -0.91$
local minimum value: -2.04 when $x = 0.91$
f is increasing on: $[-3, -0.91]$ and $[0.91, 3]$;
f is decreasing on: $[-0.91, 0.91]$.

26. $f(x) = 2x^4 - 5x^3 + 2x + 1$ on the interval $(-2, 3)$

Use MAXIMUM and MINIMUM on the graph of $y_1 = 2x^4 - 5x^3 + 2x + 1$.







local maximum: 1.53 when $x = 0.41$

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local minimal values: 0.54 when $x = -0.34$, -3.56 when $x = 1.80$

f is increasing on: $[-0.34, 0.41]$ and $[1.80, 3]$;

f is decreasing on: $[-2, -0.34]$ and $[0.41, 1.80]$.

27. $f(x) = 8x^2 - x$

a. $$\frac{f(2)-f(1)}{2-1} = \frac{8(2)^2 - 2 - [8(1)^2 - 1]}{1}$$
$$= 32 - 2 - (7) = 23$$

b. $$\frac{f(1)-f(0)}{1-0} = \frac{8(1)^2 - 1 - [8(0)^2 - 0]}{1}$$
$$= 8 - 1 - (0) = 7$$

c. $$\frac{f(4)-f(2)}{4-2} = \frac{8(4)^2 - 4 - [8(2)^2 - 2]}{2}$$
$$= \frac{128 - 4 - (30)}{2} = \frac{94}{2} = 47$$

28. $f(x) = 2 - 5x$

$$\frac{f(3)-f(2)}{3-2} = \frac{[2-5(3)] - [2-5(2)]}{3-2}$$
$$= \frac{(2-15)-(2-10)}{1}$$
$$= -13 - (-8) = -5$$

29. $f(x) = 3x - 4x^2$

$$\frac{f(3)-f(2)}{3-2} = \frac{\left[3(3)-4(3)^2\right] - \left[3(2)-4(2)^2\right]}{3-2}$$
$$= \frac{(9-36)-(6-16)}{1}$$
$$= -27 + 10 = -17$$

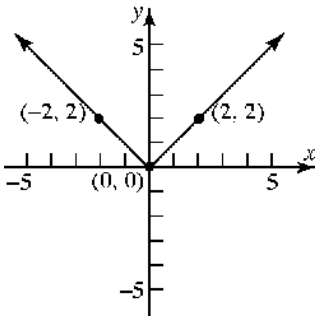
30. Refer to question 29 for the slope.

$$y + 10 = -17(x - 2)$$
$$y + 10 = -17x + 34$$
$$y = -17x + 24$$

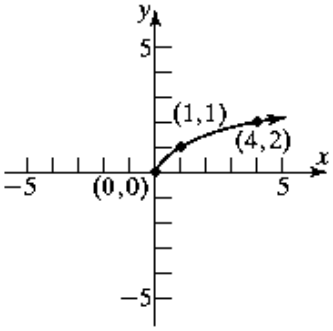
31. The graph does not pass the Vertical Line Test and is therefore not a function.

32. The graph passes the Vertical Line Test and is therefore a function.

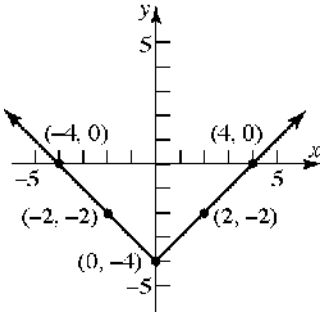
33. $f(x) = |x|$



34. $f(x) = \sqrt{x}$



35. $F(x) = |x| - 4$. Using the graph of $y = |x|$, vertically shift the graph downward 4 units.



Intercepts: (–4,0), (4,0), (0,–4)

Domain: $\{x \mid x \text{ is any real number}\}$

Range: $\{y \mid y \geq -4\}$ or $[-4, \infty)$

36. $g(x) = -2|x|$. Reflect the graph of $y = |x|$ about the *x*-axis and vertically stretch the graph by a factor of 2.

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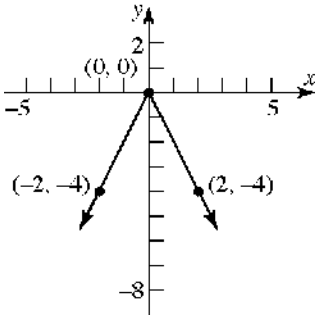
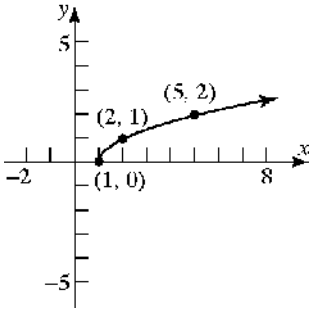


Intercepts: (0, 0)

Domain: $\{x \mid x \text{ is any real number}\}$

Range: $\{y \mid y \le 0\}$ or $(-\infty, 0]$

37. $h(x) = \sqrt{x-1}$. Using the graph of $y = \sqrt{x}$, horizontally shift the graph to the right 1 unit.

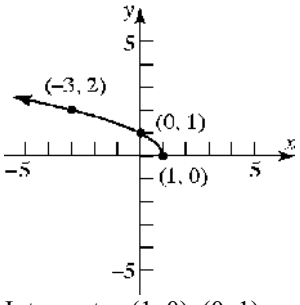


Intercept: (1, 0)

Domain: $\{x \mid x \ge 1\}$ or $[1, \infty)$

Range: $\{y \mid y \ge 0\}$ or $[0, \infty)$

38. $f(x) = \sqrt{1-x} = \sqrt{-(x-1)}$. Reflect the graph of $y = \sqrt{x}$ about the *y*-axis and horizontally shift the graph to the right 1 unit.

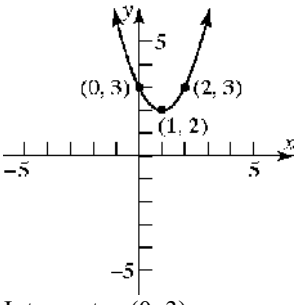


Intercepts: (1, 0), (0, 1)

Domain: $\{x \mid x \le 1\}$ or $(-\infty, 1]$

Range: $\{y \mid y \ge 0\}$ or $[0, \infty)$

39. $h(x) = (x-1)^2 + 2$. Using the graph of $y = x^2$, horizontally shift the graph to the right 1 unit and vertically shift the graph up 2 units.



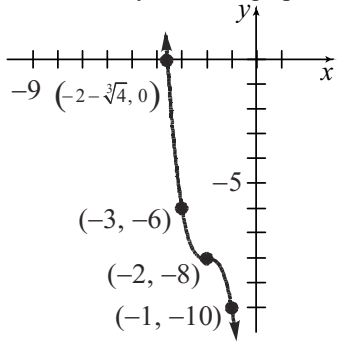
Intercepts: (0, 3)

Domain: $\{x \mid x \text{ is any real number}\}$

Range: $\{y \mid y \ge 2\}$ or $[2, \infty)$

40. $g(x) = -2(x+2)^3 - 8$

Using the graph of $y = x^3$, horizontally shift the graph to the left 2 units, vertically stretch the graph by a factor of 2, reflect about the *x*-axis, and vertically shift the graph down 8 units.



Intercepts: (0,–24), $\left(-2-\sqrt[3]{4}, 0\right) \approx (-3.6, 0)$

Domain: $\{x \mid x \text{ is any real number}\}$

Range: $\{y \mid y \text{ is any real number}\}$

41. $f(x) = \begin{cases} 3x & \text{if } -2 < x \le 1 \\ x+1 & \text{if } x > 1 \end{cases}$

a. Domain: $\{x \mid x > -2\}$ or $(-2, \infty)$

b. Intercept: $(0, 0)$

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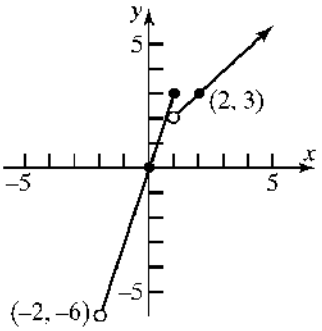
c. Graph:



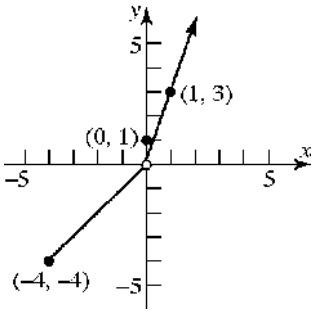
d. Range: $\{ y \mid y > -6 \}$ or $(-6, \infty)$

42. $f(x) = \begin{cases} x & \text{if } -4 \le x < 0 \\ 1 & \text{if } x = 0 \\ 3x & \text{if } x > 0 \end{cases}$

a. Domain: $\{x \mid x \ge -4\}$ or $[-4, \infty)$

b. Intercept: (0, 1)

c. Graph:



d. Range: $\{y \mid y \ge -4, y \ne 0\}$

43. $f(x) = \dfrac{Ax+5}{6x-2}$ and $f(1) = 4$

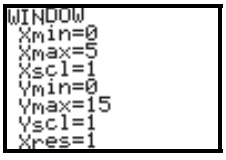
$$\frac{A(1)+5}{6(1)-2} = 4$$

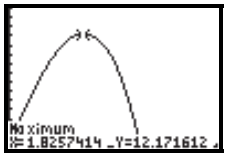
$$\frac{A+5}{4} = 4$$

$$A + 5 = 16$$

$$A = 11$$

b. The maximum value occurs at the vertex:





44. a. $x^2 h = 10 \Rightarrow h = \dfrac{10}{x^2}$

$$A(x) = 2x^2 + 4x\,h$$

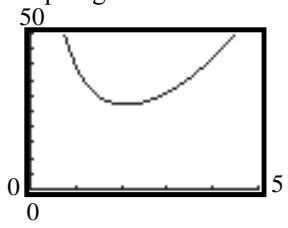
$$= 2x^2 + 4x\left(\frac{10}{x^2}\right)$$

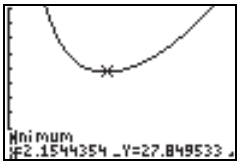
$$= 2x^2 + \frac{40}{x}$$

b. $A(1) = 2 \cdot 1^2 + \dfrac{40}{1} = 2 + 40 = 42 \text{ ft}^2$

c. $A(2) = 2 \cdot 2^2 + \dfrac{40}{2} = 8 + 20 = 28 \text{ ft}^2$

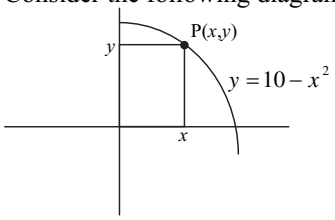
d. Graphing:





The area is smallest when $x \approx 2.15$ feet.

45. a. Consider the following diagram:



The area of the rectangle is $A = xy$. Thus, the area function for the rectangle is:

$$A(x) = x(10 - x^2)$$

The maximum area is roughly:

$$A(1.83) = -(1.83)^3 + 10(1.83)$$

$$\approx 12.17 \text{ square units}$$

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Chapter 2 Test

1. a. $\{(2,5),(4,6),(6,7),(8,8)\}$

This relation is a function because there are no ordered pairs that have the same first element and different second elements.

Domain: $\{2,4,6,8\}$

Range: $\{5,6,7,8\}$

b. $\{(1,3),(4,-2),(-3,5),(1,7)\}$

This relation is not a function because there are two ordered pairs that have the same first element but different second elements.

Domain: $\{-3,1,4\}$

Range: $\{-2,3,5,7\}$

c. This relation is not a function because the graph fails the vertical line test.

Domain: $[-1,\infty)$

Range: $\{x \mid x \text{ is any real number}\}$

d. This relation is a function because it passes the vertical line test.

Domain: $\{x \mid x \text{ is any real number}\}$

Range: $\{y \mid y \geq 2\}$ or $[2,\infty)$

2. $f(x)=\sqrt{4-5x}$

The function tells us to take the square root of $4-5x$. Only nonnegative numbers have real square roots so we need $4-5x \geq 0$.

$$4-5x \geq 0$$
$$4-5x-4 \geq 0-4$$
$$-5x \geq -4$$
$$\frac{-5x}{-5} \leq \frac{-4}{-5}$$
$$x \leq \frac{4}{5}$$

Domain: $\left\{x \middle| x \leq \frac{4}{5}\right\}$ or $\left(-\infty, \frac{4}{5}\right]$

$$f(-1)=\sqrt{4-5(-1)}=\sqrt{4+5}=\sqrt{9}=3$$

3. $g(x)=\dfrac{x+2}{|x+2|}$

The function tells us to divide $x+2$ by $|x+2|$. Division by 0 is undefined, so the denominator can never equal 0. This means that $x \neq -2$.

Domain: $\{x \mid x \neq -2\}$

$$g(-1)=\frac{(-1)+2}{|(-1)+2|}=\frac{1}{|1|}=1$$

4. $h(x)=\dfrac{x-4}{x^2+5x-36}$

The function tells us to divide $x-4$ by $x^2+5x-36$. Since division by 0 is not defined, we need to exclude any values which make the denominator 0.

$$x^2+5x-36=0$$
$$(x+9)(x-4)=0$$
$x=-9$ or $x=4$

Domain: $\{x \mid x \neq -9, x \neq 4\}$

(note: there is a common factor of $x-4$ but we must determine the domain prior to simplifying)

$$h(-1)=\frac{(-1)-4}{(-1)^2+5(-1)-36}=\frac{-5}{-40}=\frac{1}{8}$$

5. a. To find the domain, note that all the points on the graph will have an *x*-coordinate between -5 and 5, inclusive. To find the range, note that all the points on the graph will have a *y*-coordinate between -3 and 3, inclusive.

Domain: $\{x \mid -5 \leq x \leq 5\}$ or $[-5,5]$

Range: $\{y \mid -3 \leq y \leq 3\}$ or $[-3,3]$

b. The intercepts are $(0,2)$, $(-2,0)$, and $(2,0)$.

x-intercepts: -2, 2

y-intercept: 2

c. $f(1)$ is the value of the function when $x=1$. According to the graph, $f(1)=3$.

d. Since $(-5,-3)$ and $(3,-3)$ are the only points on the graph for which $y=f(x)=-3$, we have $f(x)=-3$ when $x=-5$ and $x=3$.

e. To solve $f(x)<0$, we want to find *x*-values such that the graph is below the x-axis. The graph is below the x-axis for values in the domain that are less than -2 and greater than 2. Therefore, the solution set is $\{x \mid -5 \leq x < -2 \text{ or } 2 < x \leq 5\}$. In

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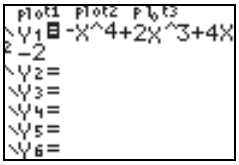
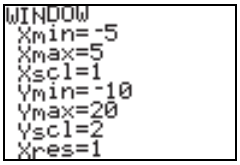
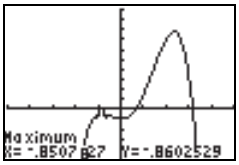
interval notation we would write the solution set as $[-5,-2)\cup(2,5]$.

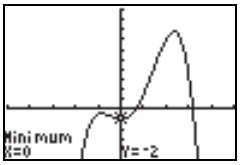
6. $f(x)=-x^4+2x^3+4x^2-2$

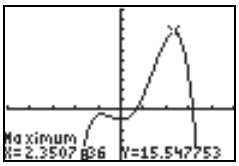
We set Xmin = -5 and Xmax = 5. The standard Ymin and Ymax will not be good enough to see the whole picture so some adjustment must be made.











We see that the graph has a local maximum value of -0.86 (rounded to two places) when $x=-0.85$ and another local maximum value of 15.55 when $x=2.35$. There is a local minimum value of -2 when $x=0$. Thus, we have

Local maxima: $f(-0.85)\approx -0.86$

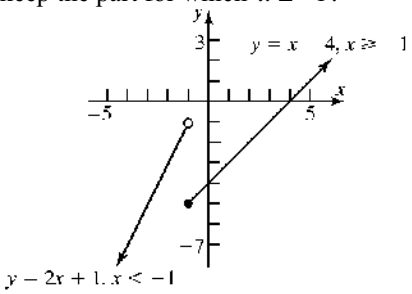
$f(2.35)\approx 15.55$

Local minima: $f(0)=-2$

The function is increasing on the intervals $[-5,-0.85]$ and $[0,2.35]$ and decreasing on the intervals $[-0.85,0]$ and $[2.35,5]$.

7. a. $f(x)=\begin{cases}2x+1 & x<-1\\ x-4 & x\ge -1\end{cases}$

To graph the function, we graph each "piece". First we graph the line $y=2x+1$ but only keep the part for which $x<-1$. Then we plot the line $y=x-4$ but only keep the part for which $x\ge -1$.



b. To find the intercepts, notice that the only piece that hits either axis is $y=x-4$.

$y=x-4$ $\qquad$ $y=x-4$

$y=0-4$ $\qquad$ $0=x-4$

$y=-4$ $\qquad$ $4=x$

The intercepts are $(0,-4)$ and $(4,0)$.

c. To find $g(-5)$ we first note that $x=-5$ so we must use the first "piece" because $-5<-1$.

$g(-5)=2(-5)+1=-10+1=-9$

d. To find $g(2)$ we first note that $x=2$ so we must use the second "piece" because $2\ge -1$.

$g(2)=2-4=-2$

8. a. The average rate of change from 3 to 4 is given by

$$\frac{f(4)-f(3)}{4-3}$$

$$=\frac{\left(3(4)^2-3(4)+4\right)-\left(3(3)^2-3(3)+4\right)}{4-3}$$

$$=\frac{40-22}{4-3}=\frac{18}{1}=18$$

b. $y+40=18(x-4)$

$y+40=18x-72$

$y=18x-32$

9. a. $(f-g)(x)=\left(2x^2+1\right)-(3x-2)$

$=2x^2+1-3x+2=2x^2-3x+3$

b. $(f\cdot g)(x)=\left(2x^2+1\right)(3x-2)$

$=6x^3-4x^2+3x-2$

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c. $f(x+h)-f(x)$

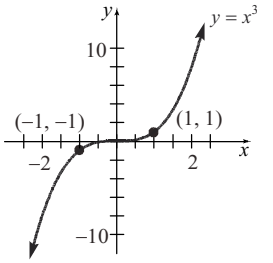
$=\left(2(x+h)^2+1\right)-\left(2x^2+1\right)$

$=\left(2\left(x^2+2xh+h^2\right)+1\right)-\left(2x^2+1\right)$

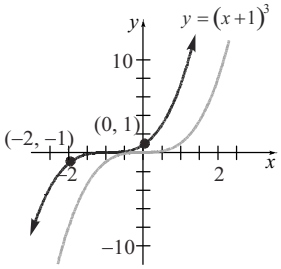
$=2x^2+4xh+2h^2+1-2x^2-1$

$=4xh+2h^2$

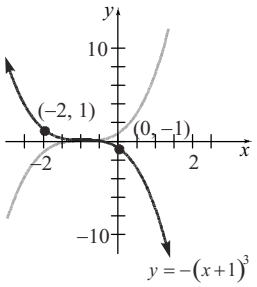
10. a. The basic function is $y=x^3$ so we start with the graph of this function.



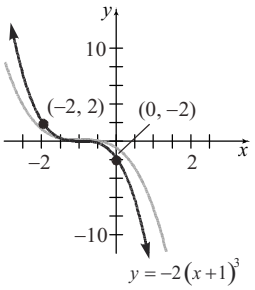
Next we shift this graph 1 unit to the left to obtain the graph of $y=(x+1)^3$.



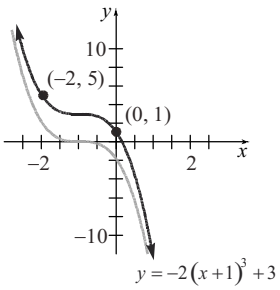
Next we reflect this graph about the x-axis to obtain the graph of $y=-(x+1)^3$.



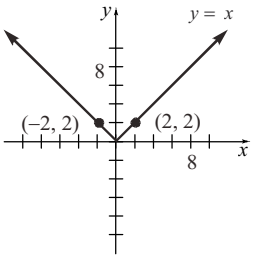
Next we stretch this graph vertically by a factor of 2 to obtain the graph of $y=-2(x+1)^3$.



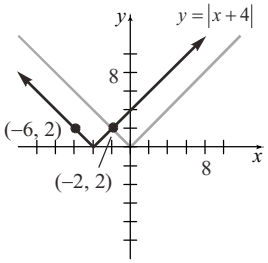
The last step is to shift this graph up 3 units to obtain the graph of $y=-2(x+1)^3+3$.



b. The basic function is $y=|x|$ so we start with the graph of this function.



Next we shift this graph 4 units to the left to obtain the graph of $y=|x+4|$.



Next we shift this graph up 2 units to obtain

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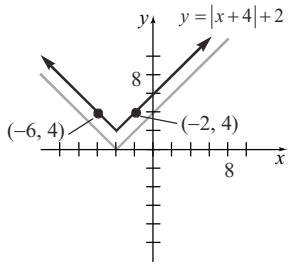
the graph of $y = |x+4|+2$.



11.a.

$$\frac{f(x+h)-f(x)}{h} = \frac{(x+h)^2-3(x+h)-(x^2-3x)}{h}$$
$$= \frac{x^2+2xh+h^2-3x-3h-x^2+3x}{h}$$
$$= \frac{2xh+h^2-3h}{h}$$
$$= \frac{h(2x+h-3)}{h} = 2x+h-3$$

12. a. Let x = width of the rink in feet. Then the length of the rectangular portion is given by $2x-20$. The radius of the semicircular portions is half the width, or $r = \frac{x}{2}$.

To find the volume, we first find the area of the surface and multiply by the thickness of the ice. The two semicircles can be combined to form a complete circle, so the area is given by

$$A = l \cdot w + \pi r^2$$
$$= (2x-20)(x) + \pi\left(\frac{x}{2}\right)^2$$
$$= 2x^2 - 20x + \frac{\pi x^2}{4}$$

We have expressed our measures in feet so we need to convert the thickness to feet as well.

$$2 \text{ in} \cdot \frac{1 \text{ ft}}{12 \text{ in}} = \frac{2}{12} \text{ ft} = \frac{1}{6} \text{ ft}$$

Now we multiply this by the area to obtain the volume. That is,

$$V(x) = \frac{1}{6}\left(2x^2 - 20x + \frac{\pi x^2}{4}\right)$$
$$V(x) = \frac{x^2}{3} - \frac{10x}{3} + \frac{\pi x^2}{24}$$

b. If the rink is 90 feet wide, then we have $x = 90$.

$$V(90) = \frac{90^2}{3} - \frac{10(90)}{3} + \frac{\pi(90)^2}{24} \approx 3460.29$$

The volume of ice is roughly 3460.29 ft^3.

13. $f(-x) = -(-x)^2 - 7$
$= -x^2 - 7$ same

The function is even.

Chapter 2 Cumulative Review

1. $3x - 8 = 10$
$3x - 8 + 8 = 10 + 8$
$3x = 18$
$\frac{3x}{3} = \frac{18}{3}$
$x = 6$

The solution set is $\{6\}$.

2. $3x^2 - x = 0$
$x(3x-1) = 0$
$x = 0$ or $3x - 1 = 0$
$3x = 1$
$x = \frac{1}{3}$

The solution set is $\left\{0, \frac{1}{3}\right\}$.

3. $x^2 - 8x - 9 = 0$
$(x-9)(x+1) = 0$
$x - 9 = 0$ or $x + 1 = 0$
$x = 9$ $\quad$ $x = -1$

The solution set is $\{-1, 9\}$.

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4. $6x^2 - 5x + 1 = 0$

$(3x-1)(2x-1) = 0$

$3x - 1 = 0 \quad \text{or} \quad 2x - 1 = 0$

$3x = 1 \qquad\qquad 2x = 1$

$x = \frac{1}{3} \qquad\qquad x = \frac{1}{2}$

The solution set is $\left\{\frac{1}{3}, \frac{1}{2}\right\}$.

5. $|2x+3| = 4$

$2x + 3 = -4 \quad \text{or} \quad 2x + 3 = 4$

$2x = -7 \qquad\qquad 2x = 1$

$x = -\frac{7}{2} \qquad\qquad x = \frac{1}{2}$

The solution set is $\left\{-\frac{7}{2}, \frac{1}{2}\right\}$.

6. $\sqrt{2x+3} = 2$

$\left(\sqrt{2x+3}\right)^2 = 2^2$

$2x + 3 = 4$

$2x = 1$

$x = \frac{1}{2}$

Check:

$\sqrt{2\left(\frac{1}{2}\right)+3} \stackrel{?}{=} 2$

$\sqrt{1+3} \stackrel{?}{=} 2$

$\sqrt{4} \stackrel{?}{=} 2$

$2 = 2$ T

The solution set is $\left\{\frac{1}{2}\right\}$.

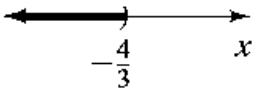
7. $2 - 3x > 6$

$-3x > 4$

$x < -\frac{4}{3}$

Solution set: $\left\{x \mid x < -\frac{4}{3}\right\}$

Interval notation: $\left(-\infty, -\frac{4}{3}\right)$



8. $|2x-5| < 3$

$-3 < 2x - 5 < 3$

$2 < 2x < 8$

$1 < x < 4$

Solution set: $\{x \mid 1 < x < 4\}$

Interval notation: $(1, 4)$

9. $|4x+1| \geq 7$

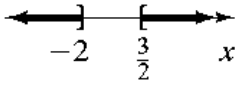
$4x + 1 \leq -7 \quad \text{or} \quad 4x + 1 \geq 7$

$4x \leq -8 \qquad\qquad 4x \geq 6$

$x \leq -2 \qquad\qquad x \geq \frac{3}{2}$

Solution set: $\left\{x \mid x \leq -2 \text{ or } x \geq \frac{3}{2}\right\}$

Interval notation: $(-\infty, -2] \cup \left[\frac{3}{2}, \infty\right)$



10. a. $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$= \sqrt{(3-(-2))^2 + (-5-(-3))^2}$

$= \sqrt{(3+2)^2 + (-5+3)^2}$

$= \sqrt{5^2 + (-2)^2} = \sqrt{25+4}$

$= \sqrt{29}$

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b. $M = \left(\dfrac{x_1 + x_2}{2}, \dfrac{y_1 + y_2}{2}\right)$

$= \left(\dfrac{-2+3}{2}, \dfrac{-3+(-5)}{2}\right)$

$= \left(\dfrac{1}{2}, -4\right)$

c. $m = \dfrac{y_2 - y_1}{x_2 - x_1} = \dfrac{-5-(-3)}{3-(-2)} = \dfrac{-2}{5} = -\dfrac{2}{5}$

11. $3x - 2y = 12$

x-intercept:

$3x - 2(0) = 12$

$3x = 12$

$x = 4$

The point $(4, 0)$ is on the graph.

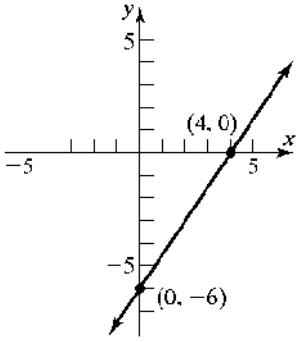
y-intercept:

$3(0) - 2y = 12$

$-2y = 12$

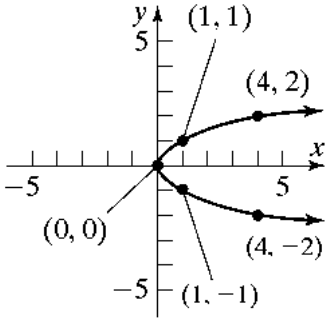
$y = -6$

The point $(0, -6)$ is on the graph.



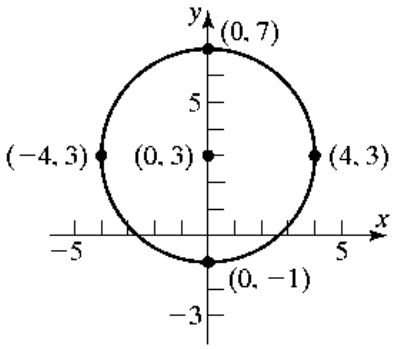
12. $x = y^2$

y	$x = y^2$	(x, y)
-2	$x = (-2)^2 = 4$	$(4, -2)$
-1	$x = (-1)^2 = 1$	$(1, -1)$
0	$x = 0^2 = 0$	$(0, 0)$
1	$x = 1^2 = 1$	$(1, 1)$
2	$x = 2^2 = 4$	$(4, 2)$



13. $x^2 + (y-3)^2 = 16$

This is the equation of a circle with radius $r = \sqrt{16} = 4$ and center at $(0, 3)$. Starting at the center we can obtain some points on the graph by moving 4 units up, down, left, and right. The corresponding points are $(0, 7)$, $(0, -1)$, $(-4, 3)$, and $(4, 3)$, respectively.



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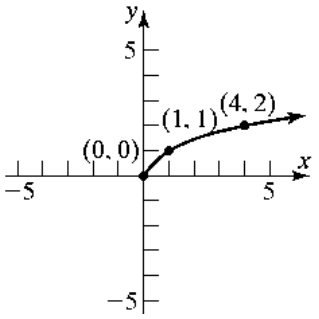
14. $y=\sqrt{x}$

x	$y=\sqrt{x}$	(x,y)
0	$y=\sqrt{0}=0$	$(0,0)$
1	$y=\sqrt{1}=1$	$(1,1)$
4	$y=\sqrt{4}=2$	$(4,2)$



15. $3x^2-4y=12$

x-intercepts:

$3x^2-4(0)=12$

$3x^2=12$

$x^2=4$

$x=\pm 2$

y-intercept:

$3(0)^2-4y=12$

$-4y=12$

$y=-3$

The intercepts are $(-2,0)$, $(2,0)$, and $(0,-3)$.

Check x-axis symmetry:

$3x^2-4(-y)=12$

$3x^2+4y=12$ different

Check y-axis symmetry:

$3(-x)^2-4y=12$

$3x^2-4y=12$ same

Check origin symmetry:

$3(-x)^2-4(-y)=12$

$3x^2+4y=12$ different

The graph of the equation has y-axis symmetry.

16. First we find the slope:

$$m=\frac{8-4}{6-(-2)}=\frac{4}{8}=\frac{1}{2}$$

Next we use the slope and the given point $(6,8)$ in the point-slope form of the equation of a line:

$y-y_1=m(x-x_1)$

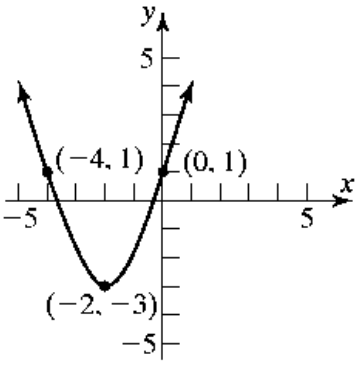
$y-8=\frac{1}{2}(x-6)$

$y-8=\frac{1}{2}x-3$

$y=\frac{1}{2}x+5$

17. $f(x)=(x+2)^2-3$

Starting with the graph of $y=x^2$, shift the graph 2 units to the left $\left[y=(x+2)^2\right]$ and down 3 units $\left[y=(x+2)^2-3\right]$.



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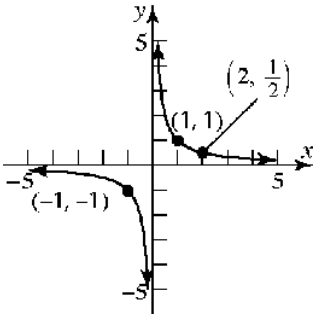
18. $f(x)=\dfrac{1}{x}$

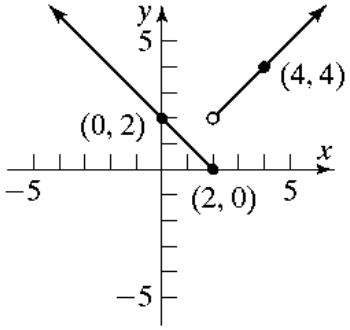
x	$y=\dfrac{1}{x}$	(x,y)
-1	$y=\dfrac{1}{-1}=-1$	$(-1,-1)$
1	$y=\dfrac{1}{1}=1$	$(1,1)$
2	$y=\dfrac{1}{2}$	$\left(2,\dfrac{1}{2}\right)$



19. $f(x)=\begin{cases}2-x & \text{if } x\le 2\\ |x| & \text{if } x>2\end{cases}$

Graph the line $y=2-x$ for $x\le 2$. Two points on the graph are $(0,2)$ and $(2,0)$.

Graph the line $y=x$ for $x>2$. There is a hole in the graph at $x=2$.



Chapter 2 Projects

Project I – Internet-based Project – Answers will vary

Project II

1. Silver: $C(x)=20+0.16(x-200)=0.16x-12$

$$C(x)=\begin{cases}20 & 0\le x\le 200\\ 0.16x-12 & x>200\end{cases}$$

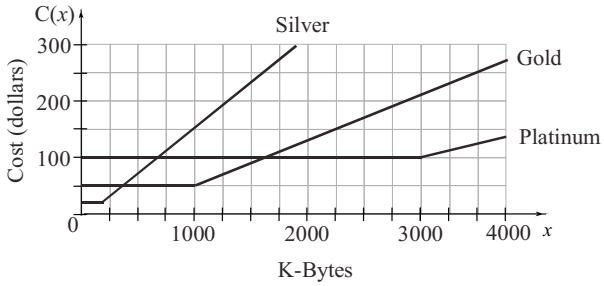
Gold: $C(x)=50+0.08(x-1000)=0.08x-30$

$$C(x)=\begin{cases}50.00 & 0\le x\le 1000\\ 0.08x-30 & x>1000\end{cases}$$

Platinum: $C(x)=100+0.04(x-3000)$

$$=0.04x-20$$

$$C(x)=\begin{cases}100.00 & 0\le x\le 3000\\ 0.04x-20 & x>3000\end{cases}$$



3. Let y = #K-bytes of service over the plan minimum.

Silver: $20+0.16y\le 50$

$$0.16y\le 30$$

$$y\le 187.5$$

Silver is the best up to $187.5+200=387.5$ K-bytes of service.

Gold: $50+0.08y\le 100$

$$0.08y\le 50$$

$$y\le 625$$

Gold is the best from 387.5 K-bytes to $625+1000=1625$ K-bytes of service.

Platinum: Platinum will be the best if more than 1625 K-bytes is needed.

4. Answers will vary.

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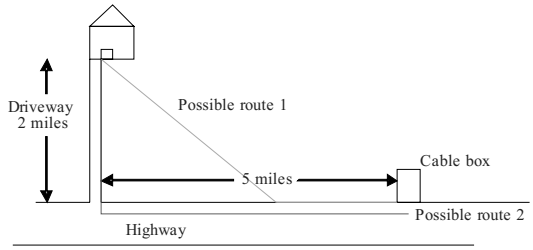
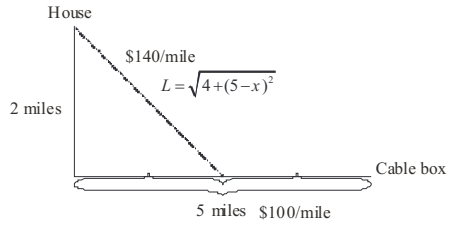
Project III

1.



2.



$C(x) = 100x + 140L$

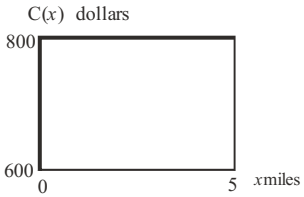
$C(x) = 100x + 140\sqrt{4+(5-x)^2}$

3.

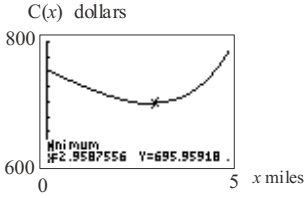
x	$C(x)$
0	$100(0)+140\sqrt{4+25} \approx \$753.92$
1	$100(1)+140\sqrt{4+16} \approx \$726.10$
2	$100(2)+140\sqrt{4+9} \approx \$704.78$
3	$100(3)+140\sqrt{4+4} \approx \$695.98$
4	$100(4)+140\sqrt{4+1} \approx \$713.05$
5	$100(5)+140\sqrt{4+0} = \$780.00$

The choice where the cable goes 3 miles down the road then cutting up to the house seems to yield the lowest cost.

4. Since all of the costs are less than \$800, there would be a profit made with any of the plans.



Using the MINIMUM function on a graphing calculator, the minimum occurs at $x \approx 2.96$.



The minimum cost occurs when the cable runs for 2.96 mile along the road.

6. $C(4.5) = 100(4.5) + 140\sqrt{4+(5-4.5)^2}$

$\approx \$738.62$

The cost for the Steven's cable would be \$738.62.

7. 5000(738.62) = \$3,693,100 State legislated
5000(695.96) = \$3,479,800 cheapest cost
It will cost the company \$213,300 more.

Project IV

1. $A = \pi r^2$

2. $r = 2.2t$

3. $r = 2.2(2) = 4.4$ ft

$r = 2.2(2.5) = 5.5$ ft

4. $A = \pi(4.4)^2 = 60.82 \text{ ft}^2$

$A = \pi(5.5)^2 = 95.03 \text{ ft}^2$

5. $A = \pi(2.2t)^2 = 4.84\pi t^2$

6. $A = 4.84\pi(2)^2 = 60.82 \text{ ft}^2$

$A = 4.84\pi(2.5)^2 = 95.03 \text{ ft}^2$

7. $\dfrac{A(2.5)-A(2)}{2.5-2} = \dfrac{95.03-60.82}{0.5} = 68.42$ ft/hr

8. $\dfrac{A(3.5)-A(3)}{3.5-3} = \dfrac{186.27-136.85}{0.5} = 98.84$ ft/hr

9. The average rate of change is increasing.

10. 150 yds = 450 ft

$r = 2.2t$

$t = \dfrac{450}{2.2} = 204.5$ hours

11. 6 miles = 31680 ft
Therefore, we need a radius of 15,840 ft.

$t = \dfrac{15,840}{2.2} = 7200$ hours

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