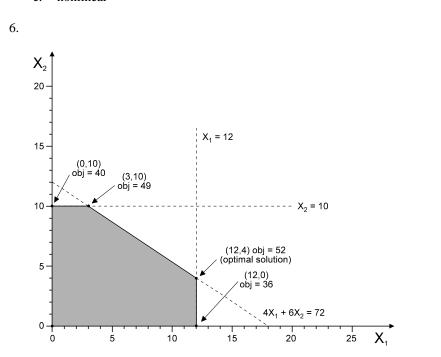
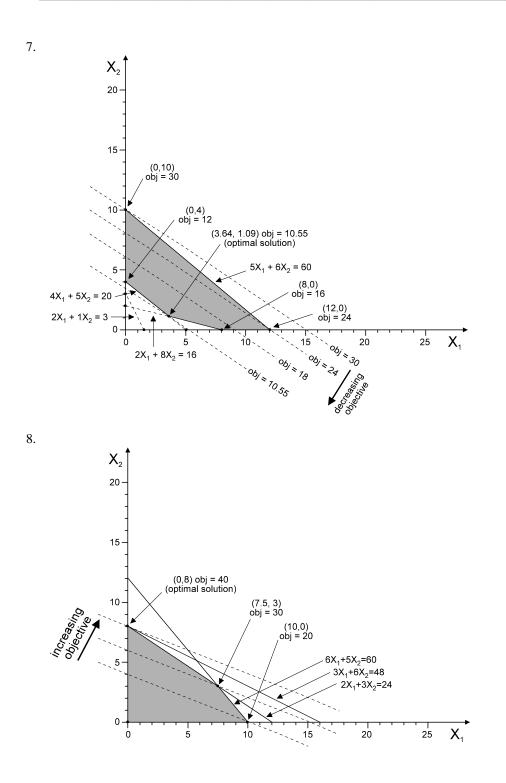
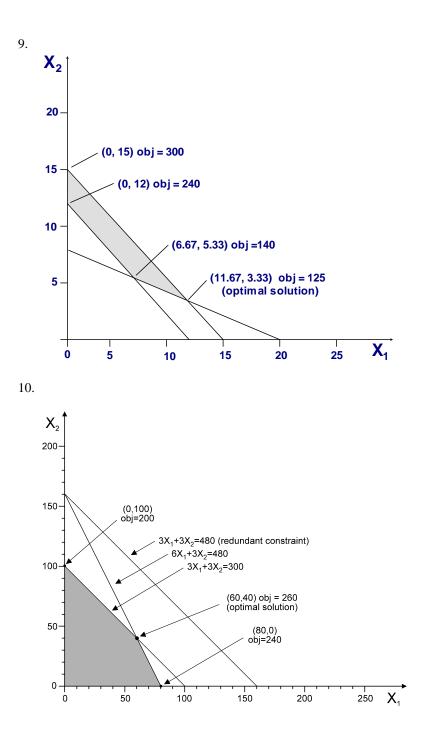
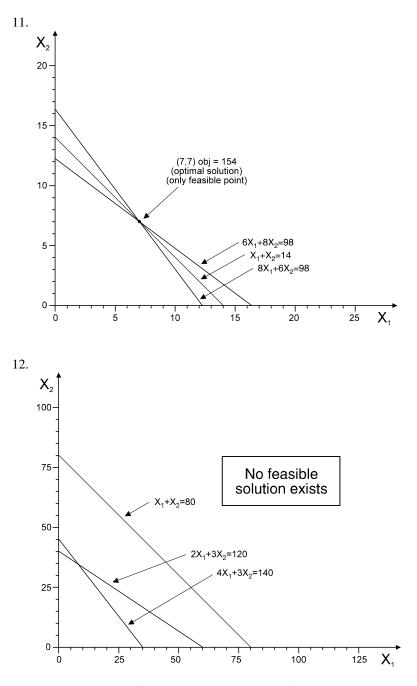
Chapter 2 Introduction to Optimization & Linear Programming

- 1. If an LP model has more than one optimal solution it has an *infinite* number of alternate optimal solutions. In Figure 2.8, the two extreme points at (122, 78) and (174, 0) are alternate optimal solutions, but there are an infinite number of alternate optimal solutions along the edge connecting these extreme points. This is true of all LP models with alternate optimal solutions.
- 2. There is no guarantee that the optimal solution to an LP problem will occur at an integer-valued extreme point of the feasible region. (An exception to this general rule is discussed in Chapter 5 on networks).
- 3. We can graph an inequality as if they were an equality because the condition imposed by the equality corresponds to the boundary line (or most extreme case) of the inequality.
- 4. The objectives are equivalent. For any values of X_1 and X_2 , the absolute value of the objectives are the same. Thus, maximizing the value of the first objective is equivalent to minimizing the value of the second objective.
- 5. a. linear
 - b. nonlinear
 - c. linear, can be re-written as: $4 X_1 .3333 X_2 = 75$
 - d. linear, can be re-written as: 2.1 X₁ + 1.1 X₂ 3.9 X₃ \leq 0
 - e. nonlinear



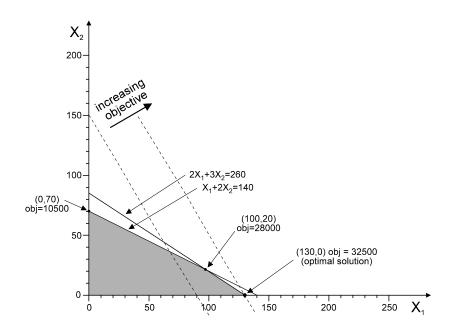




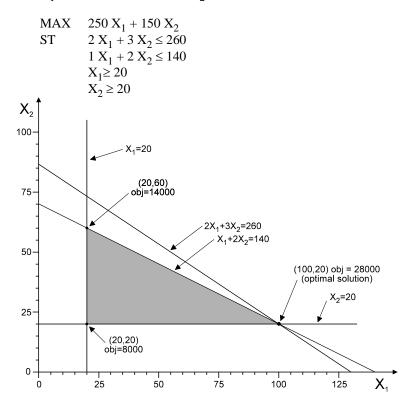


13. X_1 = number of generators, X_2 = number of alternators

 $\begin{array}{ll} \text{MAX} & 250 \ \text{X}_1 + 150 \ \text{X}_2 \\ \text{ST} & 2 \ \text{X}_1 + 3 \ \text{X}_2 \leq 260 \\ 1 \ \text{X}_1 + 2 \ \text{X}_2 \leq 140 \\ \text{X}_1, \ \text{X}_2 \geq 0 \end{array}$



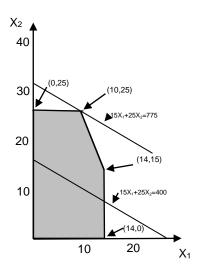
14. X_1 = number of generators, X_2 = number of alternators



d. No, the feasible region would not increase so the solution would not change -- you'd just have extra (unused) wiring capacity.

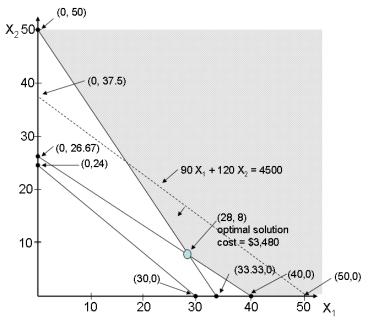
15. $X_1 = #$ of TV spots, $X_2 = #$ of magazine ads

MAX	$15 X_1 + 25 X_2$	(profit)
ST	$5 X_1 + 2 X_2 \le 100$	(ad budget)
	$5 X_1 + 0 X_2 \le 70$	(TV limit)
	$0 X_1 + 2 X_2 \le 50$	(magazine limit)
	$X_1, X_2 \ge 0$	

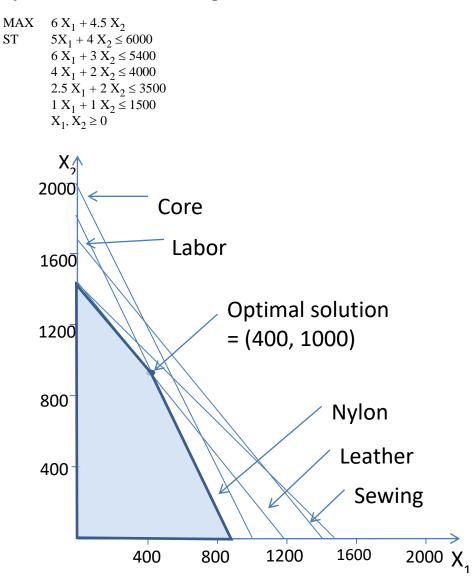


16. $X_1 =$ tons of ore purchased from mine 1, $X_2 =$ tons of ore purchased from mine 2

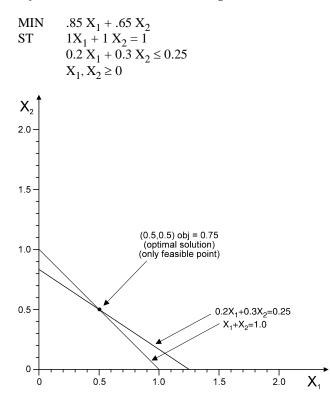
$$\begin{array}{ll} \text{MIN} & 90 \ X_1 + 120 \ X_2 & (\text{cost}) \\ \text{ST} & 0.2 \ X_1 + 0.3 \ X_2 \geq 8 & (\text{copper}) \\ & 0.2 \ X_1 + 0.25 \ X_2 \geq 6 & (\text{zinc}) \\ & 0.15 \ X_1 + 0.1 \ X_2 \geq 5 & (\text{magnesium}) \\ & X_1, \ X_2 \geq 0 \end{array}$$



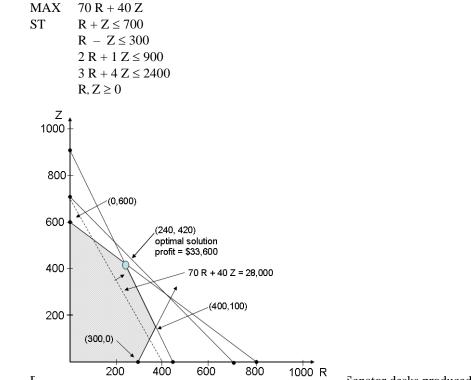
17. X_1 = number of softballs to produce, X_2 = number of baseballs to produce



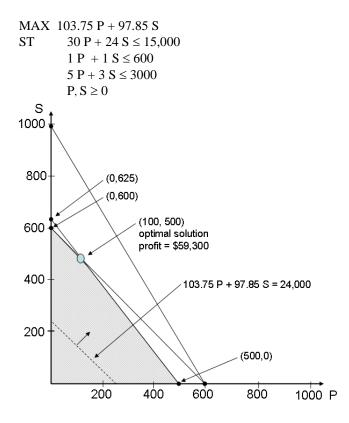
18. X_1 = proportion of beef in the mix, X_2 = proportion of pork in the mix

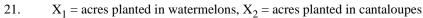


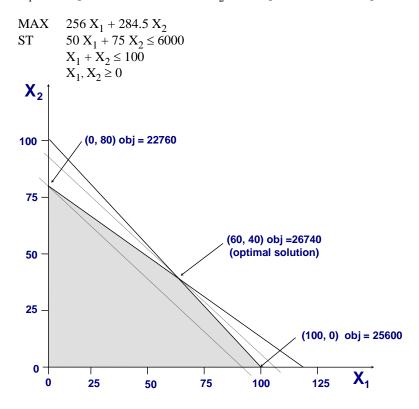
19. R = number of Razors produced, Z = number of Zoomers produced



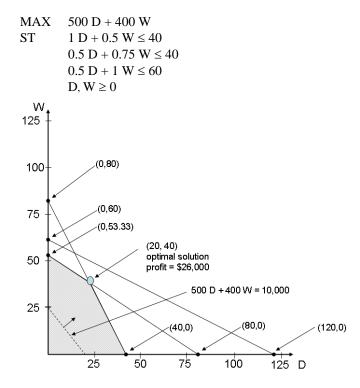
20. F = number of residential desks produced, s = number of Senator desks produced

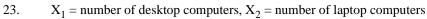


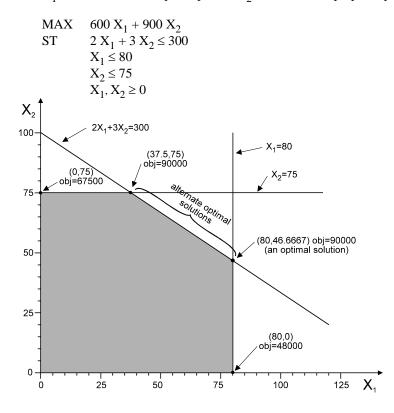




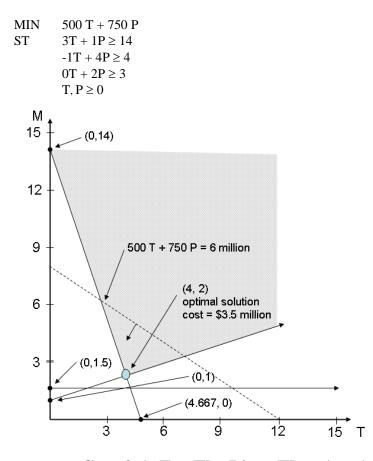
22. D = number of doors produced, W = number of windows produced







24. T = number of TV ads to run, M = number of magazine ads to run



Case 2-1: For The Lines They Are A-Changin'

- 1. 200 pumps, 1566 labor hours, 2712 feet of tubing.
- 2. Pumps are a binding constraint and should be increased to 207, if possible. This would increase profits by \$1,400 to \$67,500.
- 3. Labor is a binding constraint and should be increased to 1800, if possible. This would increase profits by \$3,900 to \$70,000.
- 4. Tubing is a non-binding constraint. They've already got more than they can use and don't need any more.
- 5. 9 to 8: profit increases by \$3,0508 to 7: profit increases by \$8507 to 6: profit increases by \$0
- 6. 6 to 5: profit increases by \$975
 5 to 4: profit increases by \$585
 4 to 3: profit increases by \$390

- 7. 12 to 11: profit increases by \$0 11 to 10: profit increases by \$0 10 to 9: profit increases by \$0
- 16 to 15: profit increases by \$0 15 to 14: profit increases by \$0 14 to 13: profit increases by \$0
- 9. The profit on Aqua-Spas can vary between \$300 and \$450 without changing the optimal solution.
- 10. The profit on Hydro-Luxes can vary between \$233.33 and \$350 without changing the optimal solution.