## CHAPTER 2

## Cost Behavior and Cost Estimation

## Learning Objectives

1. Identify basic cost behavior patterns and explain how changes in activity level affect total cost and unit cost. (Unit 2.1)
2. Estimate a cost equation from a set of cost data and predict future total cost from that equation. (Unit 2.2)
3. Prepare a contribution format income statement. (Unit 2.3)

## Summary of End of Chapter Material

Difficulty: $\quad \mathrm{E}=$ Easy, $\mathrm{M}=$ Moderate, $\mathrm{D}=$ Difficult
Bloom: $\quad \mathrm{K}=$ Knowledge, $\mathrm{C}=$ Comprehension, $\mathrm{AP}=$ Application, $\mathrm{AN}=$ Analysis, $\mathrm{S}=$ Synthesis, $\mathrm{E}=$ Evaluation
IMA: $\quad \mathrm{S}=$ Strategy, planning \& performance, $\mathrm{R}=$ Reporting and control, $\mathrm{T}=$ Technology and analytics, $\mathrm{B}=$ Business acumen \& operations, $\mathrm{L}=$ Leadership, $\mathrm{E}=$ Professional ethics \& values
AICPA ACC: RA = Risk assessment, $M=$ Measurement, $R=$ Reporting, $R S=$ Research, $S=$ System/process management,
T = Technology
AICPA BUS: $\mathrm{S}=$ Strategic, $\mathrm{G}=\mathrm{Global}, \mathrm{P}=$ Process management, $\mathrm{GV}=$ Governance, $\mathrm{C}=$ Customer
AICPA PRO: $\mathrm{E}=$ Ethics, $\mathrm{P}=$ Professional behavior, $\mathrm{D}=$ Decision making, $\mathrm{CO}=$ Collaboration, $\mathrm{L}=$ Leadership,
$\mathrm{C}=$ Communication, $\mathrm{PM}=$ Project Management

| Item | L. O. | Difficulty Level | Minutes to Complete | Bloom's Taxonomy | IMA | $\begin{aligned} & \text { AICPA } \\ & \text { ACC } \end{aligned}$ | AICPA BUS | AICPA PRO | Ethics Coverage |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Unit 2.1 |  |  |  |  |  |  |  |  |  |
| 1 | 1 | M | 2 | C | S | R | S, P | D |  |
| 2 | 1 | M | 4 | C, K | S | R | S, P | D |  |
| 3 | 1 | M | 3 | C, K | S | R | S, P | D |  |
| 4 | 1 | E | 2 | C | S | R | S, P | D |  |
| 5 | 1 | M | 4 | C, K | S | R | S, P | D |  |
| 6 | 1 | M | 4 | C, K | S | R | S, P | D |  |
| Unit 2.2 |  |  |  |  |  |  |  |  |  |
| 1 | 2 | E | 1 | K | S | M | S, P | D |  |
| 2 | 2 | M | 2 | C | S | M | S, P | D |  |
| 3 | 2 | M | 4 | K | S | M | S, P | D |  |
| 4 | 2 | E | 2 | C | S | M | S, P | D |  |
| 5 | 2 | M | 4 | C | S | M | S, P | D |  |
| Unit 2.3 |  |  |  |  |  |  |  |  |  |
| 1 | 3 | E | 1 | K | S | M | S, P | D |  |
| 2 | 3 | E | 2 | K | S | M | S, P | D |  |
| 3 | 3 | D | 3 | C | S | M | S, P | D |  |
| 4 | 3 | D | 3 | C | S | M | S, P | D |  |
| EXERCISES |  |  |  |  |  |  |  |  |  |
| 2-1* | 1 | M | 12 | C | S | R | S, P | D |  |
| 2-2 | 1 | M | 15 | C | S | R | S, P | D |  |
| 2-3* | 1 | M | 12 | AP | S | M | S, P | D |  |
| 2-4* | 1 | M | 15 | AP, C | S | M | S, P | D |  |
| 2-5* | 1 | M | 15-20 | AP, AN | S | M | S, P | D |  |
| 2-6 | 1 | D | 5-7 | AN | S | M | S, P | D |  |


| Item | L. O. | Difficulty Level | Minutes to Complete | Bloom's Taxonomy | IMA | AICPA ACC | AICPA BUS | AICPA PRO | Ethics Coverage |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2-7* | 1 | D | 8 | AP, AN | S | M | S, P | D |  |
| 2-8 | 2 | M | 15-20 | AP, AN | S | M | S, P | D |  |
| 2-9 | 2 | M | 20 | AP, AN | S | M | S, P | D |  |
| 2-10*+ | 2 | M | 12 | AP, AN | S | M | S, P | D |  |
| 2-11* | 2 | D | 20 | AP | S | M | S, P | D |  |
| 2-12* | 2 | D | 10-15 | AP | S | M | S, P | D |  |
| 2-13*+ | 3 | M | 10-15 | AP | S | M | S, P | D |  |
| 2-14 | 3 | E | 10-15 | AN | S | M | S, P | D |  |
| 2-15* | 3 | D | 10-15 | AP | S | M | S, P | D |  |
| 2-16*+ | 3 | M | 15 | AP | S | M | S, P | D |  |
| 2-17 | 3 | E | 15 | AP | S | M | S, P | D |  |
| 2-18* | 3 | E | 10 | AP | S | M | S, P | D |  |
| PROBLEMS |  |  |  |  |  |  |  |  |  |
| 2-19 | 1 | E | 20-25 | AP, AN | S | M | S, P | D |  |
| 2-20* | 2 | M | 20-25 | AP, AN | S | M | S, P | D |  |
| 2-21* | 2 | D | 15-20 | AP, AN | S | M | S, P | D |  |
| 2-22* | 2 | M | 20-25 | AP, AN | S | M | S, P | D |  |
| 2-23 | 2 | D | 30-35 | AP, AN | S | M | S, P | D |  |
| 2-24 | 1,3 | D | 20-25 | AP | S | M | S, P | D |  |
| 2-25* | 2, 3 | D | 20 | AP | S | M | S, P | D |  |
| 2-26* | 3 | D | 20-25 | AP | S | M | S, P | D |  |
| C\&C CONTINUING CASE |  |  |  |  |  |  |  |  |  |
| 2-27* | 1 | E | 5-7 | C | S | M | S, P | D |  |
| 2-28* | 2, 3 | M | 10 | AP, AN | S | M | S, P | D |  |
| CASES |  |  |  |  |  |  |  |  |  |
| 2-29* | 1 | D | 20-25 | AP | S | M | S, P | D |  |
| 2-30 |  | M | 10-15 | AN | E | R | S, P | E | $\checkmark$ |
| DATA ANALYTICS PROBLEMS |  |  |  |  |  |  |  |  |  |
| 2-31 | 2 | M | 30-40 | AP, AN, E | T, S | T, M | S, P | D |  |
| 2-32 ${ }^{\text {n }}$ | 2 | M | 30-40 | $\begin{gathered} \text { AP, AN, S, } \\ \mathrm{E} \end{gathered}$ | T, S | T, M | S, P | D |  |

* Revised problem in $4^{\text {th }}$ edition
+ Lightboard video solution available
${ }^{n}$ New problem


## SOLUTIONS TO GUIDED UNIT PREPARATION

## Unit 2.1

1. Managers must be able to predict the financial results of their various decisions. The only way to predict results is to know how costs will change or "behave" with changes in activity.
2. A variable cost is a cost that varies in total in proportion to a business activity. Within the relevant range, variable cost per unit is constant. As the level of activity increases, the total cost increases by the same proportion. Examples include commissions, cost of bicycle tires for a bicycle manufacturer, and cost of postage for a direct mail advertiser.
3. A fixed cost is a cost that does not change in total with the activity level. Within the relevant range, the total fixed cost remains constant as the activity level changes. However, the cost per unit varies inversely with changes in activity level. Examples include monthly rent, a manager's salary, and property taxes.
4. Discretionary fixed costs are fixed costs that can be changed over the short run. Committed fixed costs cannot be changed over the short run.
5. A mixed cost is a cost that has both fixed and variable components. As the level of activity increases, the total cost increases and the cost per unit decreases. Examples include electricity cost, party hall rental when the charge includes a flat fee plus a cost per guest, and t-shirt printing when the charge includes a set-up fee plus a charge for each t-shirt printed.
6. A step cost is a cost that is fixed over a small range of activity. Total cost will not change as activity levels increase if the level of activity is within a certain range. However, once the activity level exceeds this range, total cost will increase. Examples include maintenance costs when a new maintenance worker is needed per 10 machines, nurse salaries per 5 patients on a hospital floor, and hotel room rates per 4 students on a class trip.

## Unit 2.2

1. $\mathrm{TC}=(\mathrm{VC} \times \mathrm{x})+\mathrm{FC}$
2. With a scattergraph, a line is drawn to best fit the data points. The point at which the line intersects the $y$-axis is the value for fixed costs. The slope of the line, change in total cost divided by change in activity, is the variable cost per unit.
3. The high-low method uses the highest and lowest points within a data range to construct a total cost line. The variable cost per unit is calculated by dividing the change in total cost by the change in activity. The fixed cost is calculated by plugging the variable cost in the formula $\mathrm{TC}=(\mathrm{VC} \times \mathrm{x})+\mathrm{FC}$ and using either the high point or low point of activity.
4. Regression analysis is preferable as it produces a line with the least amount of error and is relatively easy to use in Excel or other another spreadsheet softwareapplication.
5. The relevant range is the normal level of operating activity. The relevant range applies to the whole company and is valid for all cost relationships. The steps in a step cost are ranges that are only valid for that particular cost. The steps in the range are smaller than the relevant range.

## Unit 2.3

1. Contribution margin is the difference between sales and variable cost.
2. Contribution margin ratio is the contribution margin divided by sales. The variable cost ratio is 1 minus the contribution margin ratio. The larger the variable cost ratio, the smaller the contribution margin will be, since the two ratios must add to $100 \%$.
3. If the variable cost per unit increases and the selling price decreases, the contribution margin per unit will decrease. The change in fixed cost has no bearing on the contribution margin.
4. A product's contribution margin can be increased by increasing the selling price per unit or decreasing variable costs per unit. Total contribution margin can be increased by selling more units.

## SOLUTIONS TO EXERCISES

## Exercise 2-1

a. fixed
e. step
b. variable
f. variable
c. fixed
g. mixed
d. fixed

## Exercise 2-2

a. variable
f. fixed
b. fixed
g. mixed
c. step
h. variable
d. mixed
i. variable
e. variable
j. fixed

## Exercise 2-3

a. $\operatorname{TC}(200$ returns $)=(200 \times \$ 12$ per return $)+\$ 650$ fee $=\$ 3,050$

TC(325 returns $)=(325 \times \$ 12$ per return $)+\$ 650$ fee $=\$ 4,550$
TC(500 returns $)=(500 \times \$ 12$ per return $)+\$ 650$ fee $=\$ 6,650$
b. Cost per unit (200) $=\$ 3,050 \div 200=\$ 15.25$

Cost per unit (325) $=\$ 4,550 \div 325=\$ 14.00$
Cost per unit $(500)=\$ 6,650 \div 500=\$ 13.30$
c. As the number of returns increased from 200 to 500 , the fixed cost of $\$ 650$ decreased on a per unit basis.

## Exercise 2-4

| Balloons | Answer  <br> variable  | Reasoning <br> The total cost increases as activity <br> increases and the cost per unit remains <br> constant at \$2.50 per bouquet. |
| :--- | :--- | :--- |
| Insurance | fixed | The total cost remains constant across all <br> activity levels. |
| Delivery | variable | The total cost increases as activity <br> increases and the cost per unit remains <br> constant at \$6.00 per delivery. |
| Employee | mixed | The total cost increases as activity <br> increases and the cost per unit decreases <br> as activity increases. |
| Advertising | fixed | The total cost remains constant across all <br> activity levels. |

Per unit costs (variable and mixed costs only):
$\underline{2,000} \quad \underline{4,000} \quad \underline{6,000}$

| Balloons | $\frac{\$ 5,000}{2,000 \text { bouquets }}=\$ 2.50$ | $\frac{\$ 10,000}{4,000 \text { bouquets }}=\$ 2.50$ | $\frac{\$ 15,000}{6,000 \text { bouquets }}=\$ 2.50$ |
| :--- | :--- | :--- | :--- |
| Delivery | $\frac{\$ 12,000}{2,000 \text { bouquets }}=\$ 6.00$ | $\frac{\$ 24,000}{4,000 \text { bouquets }}=\$ 6.00$ | $\frac{\$ 36,000}{6,000 \text { bouquets }}=\$ 6.00$ |
| Employee <br> compensation | $\frac{\$ 15,000}{2,000 \text { bouquets }}=\$ 7.50$ | $\frac{\$ 23,000}{4,000 \text { bouquets }}=\$ 5.75$ | $\frac{\$ 29,000}{6,000 \text { bouquets }}=\$ 4.83$ |

## Exercise 2-5

|  |  | Home Visits |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
|  | $\underline{F, V, M}$ | $\underline{15,000}$ | $\underline{20,000}$ | $\underline{25,000}$ | $\underline{30,000}$ |
| Employee wages | variable | $\$ 225,000$ | $\$ 300,000$ | $\$ 375,000$ | $\$ 450,000$ |
| Billing services | mixed | $\$ 62,000$ | $\$ 82,000$ | 102,000 | $\$ 122,000$ |
| Medical supplies | variable | $\$ 120,000$ | $\$ 160,000$ | 200,000 | $\$ 240,000$ |
| Insurance | fixed | $\$ 15,000$ | $\$ 15,000$ | $\$ 15,000$ | $\$ 15,000$ |

Variable cost per unit:
Employee wages:

$$
\frac{\$ 450,000-\$ 300,000}{30,000-20,000}=\$ 15 \text { per visit }
$$

Billing services:

$$
\frac{\$ 122,000-\$ 82,000}{30,000-20,000}=\$ 4 \text { per visit }
$$

Medical supplies:

$$
\frac{\$ 200,000-\$ 120,000}{25,000-15,000}=\$ 8 \text { per visit }
$$

Fixed cost (using the low point):
Employee wages:
$\$ 300,000-(20,000$ visits $\times \$ 15)=\$ 0$
Billing services:
$\$ 82,000-(20,000$ visits $\times \$ 4)=\$ 2,000$
Medical supplies:
$\$ 120,000-(15,000$ visits $\times \$ 8)=\$ 0$

## Exercise 2-5, continued

## Total cost:

Employee wages: $(15,000$ visits $\times \$ 15)+\$ 0=\$ 225,000$

Billing services: $(15,000$ hours-visits $\times \$ 4)+\$ 2,000=\$ 62,000$

Medical supplies:
$(30,000$ hours-visits $\times \$ 8)+\$ 0=\$ 240,000$
Insurance:

$$
\begin{aligned}
& (15,000 \text { visits } \times \$ 0)+\$ 15,000=\$ 15,000 \\
& (30,000 \text { visits } \times \$ 0)+\$ 15,000=\$ 15,000 \\
& \hline
\end{aligned}
$$

## Exercise 2-6

Undoubtedly, some of your costs are fixed and will not change with the number of units sold. For example, you probably pay rent to the mall to set upeach month for your kiosk. Total rent does not change with the number of video games sold. Other costs may be mixed, and these costs will include a fixed component as well. Using the unit cost you calculated, your estimate will be too high if you sell more units next year and too low if you sell fewer games next year.

## Exercise 2-7

a. No effect - total fixed costs do not change with changes in quantity.
b. Decrease - The unit cost would decrease because the increase in accounting quantity would lower the fixed costs per unit, which would lower the unit cost of the 737 Next Generation plane.

NOTE: While the annual report states that these fixed infrastructure costs will not vary with changes in production rates, it is possible that a large increase in volume may push Boeing to a new relevant range. If this shift occurs, total fixed costs will likely increase.

## Exercise 2-8

a.


Note: Students may draw lines that differ from the one above. That will affect the equation they use in the remaining parts of the exercise.
b. The line intersects the $y$-axis at $\$ 50$, representing total fixed costs. The line passes through the point $(520, \$ 260)$, so the slope can be calculated as follows:

$$
\frac{\$ 260-\$ 50}{520-0}=\$ 0.404 \text { per machine hour }
$$

The equation of the line is: $y=(\$ 0.404 \times M H)+\$ 50$
c. Total cost $=(\$ 0.404 \times 750 \mathrm{MH})+\$ 50=\$ 353$
d. The line is merely an estimation of what costs will be. Since the line does not intersect the actual cost at which machine hours is 750 , then the cost estimate will not equal the actual cost.

## Exercise 2-9

a. Variable cost $=\frac{\$ 360-\$ 120}{840-240}=\$ 0.40$ per machine hour
b. Fixed cost using the low point $=\$ 120-(\$ 0.40 \times 240)=\$ 24$ Fixed cost using the high point $=\$ 360-(\$ 0.40 \times 840)=\$ 24$
c. Total cost $=(\$ 0.40 \times \mathrm{MH})+\$ 24$
d. Total cost $=(\$ 0.40 \times 750 \mathrm{MH})+\$ 24=\$ 324$
e. The equation of the line was determined using two points, neither of which was 750 machine hours. Since the line does not intersect the actual cost at which machine hours is 750 , then the cost estimate will not equal the actual cost.

## Exercise 2-10

a. Variable cost $=\frac{\$ 9,900-\$ 6,800}{1,150-750}=\$ 7.75$ per instrument
b. Fixed cost using the low point $=\$ 6,800-(\$ 7.75 \times 750)=\$ 987.50$
c. Total cost $=(\$ 7.75 \times \#$ of instruments $)+\$ 987.50$
d. Total cost $=(\$ 7.75 \times 900$ instruments $)+\$ 987.50=\$ 7,962.50$

## Exercise 2-11

## Answer

Balloons

$$
y=\$ 2.50 x+\$ 0
$$

$$
y=\$ 6,000
$$

Delivery

$$
y=\$ 6.00 x+\$ 0
$$

Employee
$y=\$ 3.50 x+\$ 8,000$
$V C=\frac{\$ 29,000-\$ 15,000}{6,000-2,000}=\$ 3.50$
Compensation

$$
\text { FC }=\$ 29,000-\$ 3.50(6,000)=\$ 8,000
$$

Since the total cost is constant, no calculations are needed.

## Exercise 2-12

a. Current system $=(.04 \times$ sales $)+\$ 50,000$

Salary and $5 \%=(.05 \times$ sales $)+\$ 20,000$
$25 \%$ commission $=.25 \times$ sales
b.

|  | Current system | Salary and 5\% commission | $\begin{gathered} 25 \% \\ \text { commission } \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| Sales revenue | \$900,000 | \$1,100,000 | \$1,300,000 |
| Cost of goods sold ${ }^{\text {a }}$ | 270,000 | 330,000 | 390,000 |
| Gross profit | 630,000 | 770,000 | 910,000 |
| Compensation expense | $86,000^{\text {b }}$ | 75,000 ${ }^{\text {c }}$ | 325,000 ${ }^{\text {d }}$ |
| Operating income | \$544,000 | \$695,000 | \$585,000 |

The salary $+5 \%$ commission results in the most profitable result for the company.

```
a0. }0\times\mathrm{ Sales revenue
听50,000 + ($900,000 < 0.04)
c$20,000 + ($1,100,000 < 0.05)
d$1,300,000 < 0.25
```


## Exercise 2-13

| Sales revenue |  | \$65,000 | Per Unit |
| :---: | :---: | :---: | :---: |
|  |  |  | \$50 |
| Variable expenses: |  |  |  |
| Cost of goods sold | \$20,800 |  | 16 |
| Commissions expense | 3,900 |  | 3 |
| Shipping expense | 2,600 |  | 2 |
| Total variable expenses |  |  | 21 |
|  |  | 27,300 |  |
| Contribution margin |  | 37,700 | \$ 29 |
| Fixed expenses: |  |  |  |
| Salaries expense | 8,000 |  |  |
| Advertising expense | 2,500 |  |  |
| Total fixed expenses |  |  |  |
|  |  | 10,500 |  |
| Operating income |  | \$27,200 |  |

## Exercise 2-14

|  | a. | b. | c. | d. |
| :---: | :---: | :---: | :---: | :---: |
| Sales revenue | \$295,000 | \$425,000 | \$267,000 | \$700,000 |
| Variable expenses | 210,000 | 275,000 | 86,000 | 300,000 |
| Contribution margin | 85,000 | 150,000 | 181,000 | 400,000 |
| Fixed expenses | 58,000 | 70,000 | 120,000 | 200,000 |
| Operating income | 27,000 | 80,000 | 61,000 | 200,000 |
| Income taxes | 16,500 | 18,000 | 16,000 | 55,000 |
| Net income | \$10,500 | \$62,000 | \$45,000 | \$145,000 |

## Exercise 2-15

|  |  | Per Unit |
| :--- | :--- | ---: |
| Sales revenue | $\$ 35,200$ | $\underline{\$ 16.00}$ |
| Variable costs: |  |  |
| $\quad$ Cost of goods sold | $\$ 19,800$ |  |
| $\quad 6,600^{\mathrm{a}}$ |  | $\underline{9.00}$ |
| $\quad$ Operating expenses | $\underline{36,400}$ | $\underline{\underline{12.00}}$ |
| $\quad$ Total variable expenses |  | $\underline{8,800}$ |
| Contribution margin | $\underline{\underline{2,100}}$ | $\underline{\underline{\$ 6,700}}$ |
| Fixed operating expenses |  |  |
| Operating Income |  |  |

[^0]
## Exercise 2-16

a. Sales price
$\$ 10.00$
Less variable costs:
Towel, water, protein shake Contribution margin 2.65 $\$ 7.35$
b. $\frac{\$ 7.35}{\$ 10.00}=73.5 \%$
c.

Sales revenue
Variable expenses:
Towel, water, shake
Contribution margin
Fixed expenses:
Instructor salaries expense $\$ 6,000$
Management salary expense $\quad 6,500$
Rent expense
Depreciation expense
1,800
Utilities \& insurance expense
1,350
Total fixed expenses
Operating Income
$\underline{11,925} \underline{2.65}$
33,075 $\quad \underline{\underline{\$ 7.35}}$

## Exercise 2-17

a.

| Sales revenue |  | $\$ 50,000$ |
| :--- | ---: | ---: |
| Variable expenses: |  |  |
| Cost of goods sold | $\$ 26,250$ |  |
| Selling expense $(75 \%)$ | $6,000^{\mathrm{a}}$ |  |
| Administrative expense (25\%) | $\underline{3,250}$ |  |
| $\quad$ Total variable expenses |  | $\underline{35,500}$ |
| Contribution margin |  | 14,500 |

Fixed expenses:
Selling expense (25\%) 2,000 ${ }^{\text {c }}$
Administrative expense (75\%) 9,750 ${ }^{\text {d }}$
Total fixed expenses
Operating Income

11,750
\$2,750

```
a$8,000 < 0.75
```

${ }^{\mathrm{b}} \$ 13,000 \times 0.25$
c $\$ 8,000 \times 0.25$

- $\$ 13,000 \times 0.75$
b. $\$ 50,000 \div \$ 2$ per cookie $=25,000$ cookies
c. $\$ 14,500 \div 25,000$ cookies $=\$ 0.58$ per cookie
d. $\$ 14,500 \div \$ 50,000=29 \%$


## Exercise 2-18

a. $\frac{\$ 87,000}{\$ 15 \text { per unit }}=5,800$ phone covers
b. $\frac{\$ 37,410}{5,800 \text { units }}=\$ 6.45$ per phone cover
c. $\frac{\$ 6.45}{\$ 15.00}=43 \%$

## SOLUTIONS TO PROBLEMS

## Problem 2-19

a.

| Minutes |  | Cost per minute |  |
| :---: | :---: | :---: | :---: |
|  | $\$ 5.00$ |  | Total Cost |
| 100 |  | $\$ 50$ |  |
| 250 |  | $\$ 0.50$ |  |
| 500 |  | $\$ 0.10$ |  |

b. This is a fixed cost because total cost remains fixed while the cost per minute decreases as minutes used increases.
c. $1,000 \times \$ 0.02=\$ 20$; prefer $\$ 0.02$ per minute instead of $\$ 50$ per month
$3,000 \times \$ 0.02=\$ 60 ;$ prefer $\$ 50$ per month
indifferent where $\$ 50=\$ 0.02 x$

$$
x=2,500 \text { minutes }
$$

d. You should determine which phone plan to buy based on how many minutes you expect to use in one month.

## Problem 2-20

a.


NOTE: Students may draw lines that differ from the one above, which will affect the equation they develop for this part of the solution.

The line intersects the $y$-axis at $\$ 500$, representing total fixed costs. The line passes through the point $(68,000, \$ 6,500)$, so the slope can be calculated as follows:

$$
\frac{\$ 6,500-\$ 500}{68,000-0}=\$ 0.088 \text { per copy }
$$

The equation of the line is: $y=\$ 0.088 / c o p y+\$ 500$
b. Variable cost $=\frac{\$ 7,300-\$ 4,400}{71,000-42,000}=\$ 0.10$ per copy
c. Fixed cost $=\$ 7,300-(\$ .10 \times 71,000)=\$ 200$
d. $y=\$ 0.10 x+\$ 200$
e. September cost $=(\$ 0.10 \times 62,000)+\$ 200=\$ 6,400$. The equation is just an approximation of the relationship between cost and copies. Since the June cost was not one of the points used to construct the line, then it is not surprising that the two figures are not equal.

## Problem 2-21

a. Variable cost $=\frac{\$ 80,000-\$ 59,000}{8,300-3,300}=\$ 4.20$ per labor hour

Fixed cost $=\$ 80,000-(\$ 4.20 \times 8,300)=\$ 45,140$ or
Fixed cost $=\$ 59,000-(\$ 4.20 \times 3,300)=\$ 45,140$
b. Total cost $=(\$ 4.20 \times 4,200)+\$ 45,140=\$ 62,780$
c. Additional overhead $=\$ 4.20 \times 350=\$ 1,470$
d. In regression analysis, the cost equation is calculated using all of the data points. In the high-low method, only two points are used to determine the cost equation. In either case, they are both estimates.

## Problem 2-22

a. Variable cost $=\frac{\$ 8,885-\$ 6,605}{76,900-48,400}=\$ 0.08$ per spike set sold
b. Fixed cost $=\$ 8,885-(\$ 0.08 \times 76,900)=\$ 2,733$ or Fixed cost $=\$ 6,605-(\$ 0.08 \times 48,400)=\$ 2,733$
c. Marketing cost $=(\$ 0.08 \times$ sets sold $)+\$ 2,733$
d. February sales volume and costs are much lower than the others.
e. Variable cost $=\frac{\$ 8,885-\$ 8,265}{76,900-64,500}=\$ 0.05$ per spike set sold

Fixed cost $=\$ 8,885-(\$ 0.05 \times 76,900)=\$ 5,040$ or
Fixed cost $=\$ 8,265-(\$ 0.05 \times 64,500)=\$ 5,040$
Marketing cost $=(\$ 0.05 \times$ sets sold $)+\$ 5,040$
f. The second equation is better for estimating future costs because the endpoints used to estimate the line are more consistent with the normal sales volumes and costs.

## Problem 2-23

a. Passengers:

Variable cost $=\frac{\$ 25,480-\$ 19,990}{2,480-2,030}=\$ 12.20$ per passenger

Fixed cost $=\$ 25,480-(\$ 12.20 \times 2,480)=(\$ 4,776)$
Fuel expense $=(\$ 12.20 \times$ passengers $)-\$ 4,776$

## Passenger miles:

Variable cost $=\frac{\$ 25,459-\$ 22,435}{580,214-361,214}=\$ 0.0138$ per passenger mile
Fixed cost $=\$ 25,459-(\$ 0.0138 \times 580,214)=\$ 17,452$
Fuel expense $=(\$ 0.0138 \times$ passenger miles $)+\$ 17,452$

## Train Miles:

Variable cost $=\frac{\$ 25,459-\$ 22,225}{3,515-3,025}=\$ 6.60$ per train mile
Fixed cost $=\$ 25,459-(\$ 6.60 \times 3,515)=\$ 2,260$
Fuel expense $=(\$ 6.60 \times$ train miles $)+\$ 2,260$
b. The formula based on passengers doesn't make sense as the fixed cost is negative. While this might have some predictive ability, it doesn't help managers understand any causal relationship between the number of passengers and fuel expense.
c. Logically, train miles would seem to have the most predictive ability since the miles a train travels and fuel costs should be directly related. While passenger miles would likely provide information related to the fuel expended due to weight (more passengers, greater weight), it is unlikely that one more passenger mile will have the same impact on fuel expenses that one more train mile will have.

## Problem 2-24

a. Cost of goods sold - variable

Advertising expense - fixed
Salaries and wages expense - mixed
Insurance expense - fixed
Postage expense - variable
b. Sales price $=\$ 3,000 \div 1,000$ windows $=\$ 3.00$ per window

Cost of goods sold $=\$ 1,200 \div 1,000$ windows $=\$ 1.20$ per window
Variable salaries expense $=\frac{\$ 1,100-\$ 700}{3,000-1,000}=\$ 0.20$ per window
Fixed salaries expense $=\$ 1,100-(.2 \times 3,000)=\$ 500$
Postage expense $=\$ 400 \div 1,000$ windows $=\$ 0.40$ per window
Fixed salaries expense $=\$ 1,100-(.2 \times 3,000)=\$ 500$

Sales revenue
$\frac{2,500 \text { windows }}{\$ 7,500}$

Per Unit
$\$ 3.00$
Variable expenses:

| Cost of goods sold | 3,000 |  | 1.20 |
| :--- | ---: | ---: | ---: |
| Salaries expense | 500 |  | 0.20 |
| Postage expense | $\underline{1,000}$ |  | $\underline{0.40}$ |
| Total variable expenses |  | $\boxed{4,500}$ | $\underline{1.80}$ |
| Contribution margin |  | 3,000 | $\underline{\underline{\$ 1.20}}$ |

Fixed expenses:

| Advertising expense | 400 |  |
| :--- | :--- | :--- |
| Salaries expense | 500 |  |
| Insurance expense | $\underline{200}$ |  |
| Total fixed expenses |  | $\underline{1,100}$ |
| Operating Income |  | $\underline{\$ 1,900}$ |

## Problem 2-25

a. coats sold $=\$ 750,000 \div \$ 200=3,750$ units
variable selling expense $=\$ 6.00 \times 3,750$ units $=\$ 22,500$
variable administrative expense $=6 \% \times \$ 750,000=\$ 45,000 \div 3,750$
= \$12 per unit
fixed selling expense $=\$ 41,060-\$ 22,500=\$ 18,560$
fixed administrative expense $=\$ 68,600-\$ 45,000=\$ 23,600$

|  |  | Per Unit |  |
| :--- | ---: | ---: | ---: |
| Sales revenue | $\$ 750,000$ | $\underline{\$ 200.00}$ |  |
| Variable expenses: |  |  | 140.00 |
| Cost of goods sold | 525,000 |  | 6.00 |
| Selling expense | 22,500 |  | 12.00 |
| Administrative expense | 45,000 |  | $\underline{158.00}$ |
| Total variable expenses |  | $\underline{592,500}$ | $\underline{157,500}$ |
| Contribution margin |  | $\underline{\$ 42.00}$ |  |

Fixed expenses:

| Selling expense | 18,560 |  |
| :--- | ---: | ---: |
| Administrative expense | $\underline{23,600}$ |  |
| Total fixed expenses |  | $\underline{42,160}$ |
| Operating Income | $\underline{\$ 115,340}$ |  |

b. Operating expenses $=\$ 158 \mathrm{x}+\$ 42,160$
c. $\$ 42 \times 4,000=\$ 168,000$

## Problem 2-26

a.

|  |  |  | Per Unit |
| :---: | :---: | :---: | :---: |
| Sales revenue |  | \$34,000 | \$40 |
| Variable expenses: |  |  |  |
| Service expense | \$17,000 |  | 20 |
| Bookkeeping expense | 2,550 |  | 3 |
| Total variable expenses |  | 19,550 | 23 |
| Contribution margin |  | 14,450 | \$17 |
| Fixed expenses: |  |  |  |
| Vans expense | 2,000 |  |  |
| Salaries expense | 3,000 |  |  |
| Total fixed expenses |  | 5,000 |  |
| Operating Income |  | \$9,450 |  |

b. $\$ 9,450+(150 \times \$ 17)=\$ 12,000$

Problem 2-26, continued
c.

Current cost: $\$ 3 \times$ customers $\times 12$ months
Option 1: $\$ 20,400+(\$ 1 \times$ customers $\times 12$ months $)$

| 850 | 1,000 | 1,100 |
| :---: | :---: | :---: |
| $\$ 30,600$ | $\$ 36,000$ | $\$ 39,600$ |
| $\$ 30,600$ | $\$ 32,400$ | $\$ 33,600$ |
| $\$ 32,000$ | $\$ 32,000$ | $\$ 32,000$ |

d. Mr. Harris needs to evaluate what he thinks future demand for his services will be. If he thinks he will have more customers, then he should consider switching to option 1 or 2 before prices increase. He also needs to think about the stability of his customer base. If he services fewer than 850 customers, options 1 and 2 will be more expensive than the current arrangement.

## SOLUTIONS TO CASES

## Case 2-27

## Cost

a. Monthly sales staff payroll of $\$ 650$ plus $5 \%$ sales commission on jerseys
b. $\quad \$ 100$ monthly rental for credit card processing equipment
c. Cost of goods sold of $\$ 22.00$ per jersey
d. The cost of price tags attached to each jersey
e. Inventory insurance that costs $\$ 2$ per $\$ 1,000$ of sales
f. Website hosting cost of $\$ 25$ per month
mixed
fixed
variable
variable
step
fixed

## Case 2-28

a. $\$ 30.00 x-\$ 24.00 x-\$ 240,000=$ operating profit
b. $(\$ 24.00 \times 55,000)+\$ 240,000=\$ 1,320,000+\$ 240,000=\$ 1,560,000$
c. Fixed selling expenses will increase by $\$ 20,000$ to $\$ 165,000$, so total fixed expenses will increase by $\$ 20,000$ to $\$ 260,000$.
d.

|  |  |  | Per Unit |
| :--- | ---: | :--- | ---: |
| Sales revenue | $\$ 1,950,000$ | $\underline{\$ 30.00}$ |  |
| Variable expenses: |  |  | 22.00 |
| Cost of goods sold | $\$ 1,430,000$ |  | 1.50 |
| Sales commission expense | 97,500 |  | $\underline{0.50}$ |
| Tags | 32,500 |  | $\underline{\underline{24.00}}$ |
| Total variable expenses |  | $\underline{1,560,000}$ | $\underline{390,000}$ |
| Contribution margin |  |  |  |
| Fixed expenses: |  |  |  |
| Selling expense |  | 95,000 |  |
| Administrative expense |  | $\underline{260,000}$ |  |
| $\quad$ Total fixed expenses |  | $\underline{\$ 130,000}$ |  |
| Operating Income |  |  |  |

## Case 2-29

a.

Ad development \$7,200 Placement ${ }^{\text {a }}$
Click-through
$6,000 \quad(\$ 0.60 \times .01 \times 1,000,000)$
\$14,700
a $\frac{1,000,000 \mathrm{ad} \text { impressions }}{1,000}=1,000$ (impressions are priced per thousand)
b. customers $=1,000,000 \times .01 \times .20=2,000$
$\frac{\$ 14,700}{2,000}=\$ 7.35$ per customer
c. You need to work backwards to solve this problem:

Since only $20 \%$ of those who click through make a purchase, it will take 5 click-throughs to generate one customer ( $1 \div .20$ ).

Since only $1 \%$ of banner ad viewers click through to the site, 500 more banner ads need to be placed (5 $\div .01$ )

Cost of 500 placements $=(500 \div 1,000) \times \$ 1.50$
\$0.75
Cost of 5 click-throughs $=5 \times \$ 0.60$
$\$ 3.00$
\$3.75

## Case 2-30

a. No, it wasn't ethical. The family and friends are not legitimate customers, and they are driving up Bohlander's cost.
b. No, it wouldn't change. While the purchase is an unintended benefit, the motivation behind Sami's actions was fraudulent.
c. As a result of Sami's actions, Bohlander will experience a higher click-through rate and a lower purchase rate than expected. These "artificial" rates could influence future expectations for similar ad campaigns. Additionally, Bohlander will incur increased advertising expenses as a result of the additional click-throughs (\$0.60 per clickthrough).

## SOLUTIONS TO DATA ANALYTICS CASE

## Case 2-31

a.


The dotted line is the linear estimation for pothole repair cost. It appears that as the number of potholes in a work order increases, there is more variability in the total cost to repair those potholes. This variability appears to occur around a volume of 40 potholes.
b. Low point: 1 pothole, $\$ 245$ repair cost

High point: 157 potholes, $\$ 14,519$ repair cost
Variable repair cost $=\frac{\$ 14,519-\$ 245}{157 \text { potholes }-1 \text { pothole }}=\$ 91.50$ per pothole
Fixed repair cost $=\$ 14,519-(\$ 91.50 \times 157)=\$ 153.50$ per work order
Cost estimate $=\$ 153.50+(\$ 91.50 \times$ number of potholes repaired $)$

Case 2-31, continued
c. Slope from Excel = \$90.4453

Intercept from Excel = \$165.5404
Cost function $=\$ 165.5404+(\$ 90.4453 \times$ number of potholes repaired $)$
d. The high-low estimate is similar to the regression estimate. It is possible, however, that these cost equations may not be useful when the number of potholes in a repair order exceeds 40, since the data shows greater variability at that point.
e. It is possible that repair materials, as well as worker speed, may vary with the outside temperature, so including that temperature may provide additional explanatory power and improve future cost estimates, provided forecasted temperatures are available when estimates are made. If temperature is added to the prediction model, average past daily temperatures could be used until updated weather forecasts are available.

Another possible factor of interest is the type of repair material. For instance, some repairs may be asphalt while others may be concrete.

The size and skill level of the work crew will also have an impact on the repair costs.

## Case 2-32

a.



Case 2-32, continued
There is a strong linear relationship between trip distance in miles and base fare. While there appears to be a linear relationship between trip length in seconds and base fare, there is more variation than with miles. There are trips of zero distance and/or zero time. There appear to be some trips that are likely outliers.
b. $\quad$ Fare $=(\$ 2.19 \times$ miles $)+\$ 5.70$
c. $\quad$ Fare $=(\$ 0.01 \times$ seconds $)+\$ 2.45$
d. $\quad 2.5$ miles: $(\$ 2.19 \times 2.5$ miles $)+\$ 5.70=\$ 11.18$ 850 seconds: $(\$ 0.01 \times 850$ seconds $)+\$ 2.45=\$ 10.95$
e. $\quad$ Fare $=(\$ 2.25 \times$ miles $)+\$ 4.87$

Fare $=(\$ 0.01 \times$ seconds $)+\$ 2.29$
2.5 miles: $(\$ 2.25 \times 2.5$ miles $)+\$ 4.87=\$ 10.50$ 850 seconds: $(\$ 0.01 \times 850$ seconds $)+\$ 2.2 \underline{9} 7=\$ 10.79$
f. Consider using multiple regression with both miles and seconds as independent variables.
g. Answers will vary depending on the locations students choose.


[^0]:    Units sold $=\$ 35,200$ sales revenue $\div \$ 16.00$ per unit $=2,200$ units
    a2,200 units $\times \$ 3$ per unit
    ${ }^{\mathrm{b}} \$ 8,700$ total operating costs expenses $-\$ 6,600$ variable cost

